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Impact of the reflection model on the estimate of the properties of accreting black holes

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ABSTRACT

Relativistic reflection features in the X-ray spectra of black hole binaries and active galactic nuclei originate from illumination of the inner part of the accretion disc by a hot corona. In the presence of high quality data and with the correct astrophysical model, X-ray reflection spectroscopy can be quite a powerful tool to probe the strong gravity region, study the morphology of the accreting matter, measure black hole spins, and even test Einstein's theory of general relativity in the strong field regime. There are a few relativistic reflection models available today and developed by different groups. All these models present some differences and have a number of simplifications introducing systematic uncertainties. The question is whether different models provide different measurements of the properties of black holes and how to arrive at a common model for the whole X-ray astronomy community. In this paper, we start exploring this issue by analysing a Suzaku observation of the stellar-mass black hole in GRS 1915+105 and simultaneous XMM-Newton and NuSTAR observations of the supermassive black hole in MCG-6-30-15. The relativistic reflection component of these sources is fitted with RELCONV × REFLIONX, RELCONV × XILLVER, and RELXILL. We discuss the differences and the impact on the study of accreting black holes.

Key words: accretion, accretion discs – black hole physics.

1 INTRODUCTION

Relativistic reflection features are commonly observed in the X-ray spectra of black hole binaries and active galactic nuclei (AGNs; Fabian et al. 1989; Tanaka et al. 1995; Nandra et al. 2007; Walton et al. 2013; Reynolds 2014; Bambi 2018). For an Eddington-scaled disc luminosity of \sim 10 per cent and a large angular momentum of the accreting gas, a black hole is surrounded by a geometrically thin and optically thick accretion disc. The gas in the disc is in local thermal equilibrium, every point of the disc has a blackbody-like spectrum, and the whole disc has a multitemperature blackbody-like spectrum (Shakura & Sunyaev 1973; Page & Thorne 1974). The thermal spectrum of the accretion disc is peaked in the soft X-ray band for stellar-mass black holes and in the optical/UV bands for supermassive black holes. The 'corona' is some hotter (\sim 100 keV), often compact and optically thin, electron cloud near the black hole (Galeev, Rosner & Vaiana 1979). Thermal photons from the disc can inverse Compton scatter off free electrons in the corona, generating a power-law spectrum with a high energy cut-off (Sunyaev & Truemper 1979). Comptonized photons can illuminate the accretion disc, producing a reflection spectrum (George & Fabian 1991). The latter is characterized by some fluorescent emission lines, notably the iron K α complex in the soft X-ray band, and the Compton hump peaked at 20-30 keV. The reflection features in the X-ray spectra of black holes are affected by the accretion disc geometry and the strong gravitational field around the compact object (Fabian et al. 1989; Laor 1991). In the presence of high quality data and with the correct astrophysical model, the analysis of these reflection features can be

In the past 5–10 yr, there has been significant progress in the development of the analysis of these features, thanks to both more sophisticated astrophysical models and new observational data. Today there are a few available reflection models that have been developed by different groups. While these models are the state of the art in the field, they are based on a number of simplifications that introduce systematic uncertainties in the final measurements of the parameters of the system. Depending on the quality of the data, such systematic uncertainties may be negligible or lead to biased estimates of the properties of accreting black holes.

Systematic uncertainties related to the theoretical model¹ can be grouped into four classes:

(i) Accretion disc. The accretion disc is normally described by the Novikov-Thorne model (Novikov & Thorne 1973; Page & Thorne 1974) (Keplerian disc on the plane perpendicular to the black hole spin) and approximated as infinitesimally thin. The inner edge of the disc is at the innermost stable circular orbit (ISCO) or at a larger radius, and there is no emission from the plunging region, namely the region between the black hole and the inner edge of the disc. However, a real accretion disc has a finite thickness and some radiation is also emitted from the plunging gas (see for instance, Fabian et al. 2020), two effects that have some impact

used to study accreting black holes, investigate the properties of the accretion discs, measure black hole spins, and even test Einstein's theory of general relativity in the strong field regime (Reynolds 2014; Bambi 2017).

¹Here, we ignore systematic uncertainties of other origin, such as those caused by instrumental effects (calibration and energy resolution) or data analysis softwares.

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on the estimate of the model parameters (Reynolds & Fabian 2008; Taylor & Reynolds 2018; Cárdenas-Avendaño, Zhou & Bambi 2020; Wilkins, Reynolds & Fabian 2020). Moreover, it is common to use these thin-disc reflection models even to fit the spectra of sources with high-mass accretion rate, and this can lead to a significant bias in the estimates of some properties of the system (Riaz et al. 2020a, b). Most models assume that the density and the ionization parameter are constant over the radial coordinate of the disc, but this has been argued to produce modelling bias in the estimate of some parameters (Svoboda et al. 2012; Kammoun et al. 2019) and thus some of the most recent models include the possibility for ionization gradients with some prescription for the density profile (see for instance, Ingram et al. 2019).

(ii) Corona. The morphology of the corona is not well understood as of now, and it is likely that it changes as the source moves to different spectral states (Wilkins & Gallo 2015b). The coronal geometry determines the emissivity profile of the reflection spectrum over the disc, and the choice of the emissivity profile model can have quite remarkable impacts on the measurements of the parameters of the system (Zhang et al. 2019). The emissivity profile from coronae of arbitrary geometry is normally modelled with a simple power law or a broken power law. These are clearly approximations that can introduce important biases in the presence of high quality data. For coronae with specific geometry, the most popular choice is the lamppost set-up, where the corona is approximated as a point-like source along the black hole spin axis (Dauser et al. 2013). There are only a few studies of coronae with more complicated geometries (Wilkins & Fabian 2012; Dauser et al. 2013).

(iii) Reflection spectrum. Illumination of the accretion disc by a hot corona generates the reflection spectrum. Calculations of the reflection spectrum in the rest frame of the gas in the disc involves atomic physics and all the available models assume a number of simplifications that introduce systematic uncertainties on the final measurements of the system. Current models assume a cold accretion disc. REFLIONX and XILLVER carry a 1D calculation assuming a plane-parallel slab, and the density is assumed to be constant in the vertical direction (see, however, Różańska et al. 2002; Ballantyne, Turner & Blaes 2004, where the density in the vertical direction is self-consistently calculated). The electron density of the angleresolved reflection model RELXILLD is allowed to vary between 10¹⁵ and 10¹⁹ cm⁻³ (García et al. 2016), while higher densities, which would be expected in the discs of black hole binaries, are possible with the angle-averaged model REFLIONX (Tomsick et al. 2018; Jiang et al. 2019a, b). Photons from the corona illuminate the disc at a fixed inclination angle. Only the iron abundance is free to vary during the fitting, while the abundances for all other elements are fixed to their solar values.

(iv) Relativistic effects. Some relativistic effects occurring in the strong gravity region are ignored even by the current more sophisticated reflection models. Returning radiation, namely the radiation emitted by the disc and returning to the disc because of the strong light bending near the black hole, is ignored in the available models and its effect may not be negligible (Niedźwiecki & Zdziarski 2018; Riaz et al. 2020c). Higher order disc images, namely radiation emitted by the disc and circling the black hole one or more times, is ignored but its impact is also very weak (Zhou et al. 2020). The exact coronal spectrum illuminating the disc is determined by the gravitational redshift between the location of the corona and the point on the disc, and it can only be calculated if the coronal geometry is known.

The next generation of X-ray missions (e.g. XRISM, eXTP, Athena, and STROBE-X) promises to provide unprecedented high

quality data, which will necessarily require more accurate synthetic reflection spectra than those available today and a better knowledge of the physical properties of these systems.

In this paper, we start exploring the issue of whether the current reflection models provide different measurements of the parameters of accreting black holes and how to arrive at a common model for the whole X-ray astronomy community. As a first step to this direction, we analyse some high quality data by fitting the reflection components of two sources with different models. We consider a 117 ks observation of *Suzaku* of the black hole binary GRS 1915+105 and a set of simultaneous observations with *XMM–Newton* and *NuSTAR* of the AGN MCG-6-30-15.

We chose these sources/data to have a black hole binary and an AGN, one observed from a high viewing angle and the other one from a low viewing angle. As for GRS 1915+105, *Suzaku* provides both a good energy resolution near the iron line and data up to ~50 keV to see the Compton hump. That particular *Suzaku* observation shows a simple spectrum with strong relativistic reflection features and no disc thermal component, so the disc temperature was presumably low and this is consistent with the assumption of cold disc used in the reflection models. We are not aware of any *NuSTAR* observation of GRS 1915+105 with such properties. In the case of MCG-6-30-15, the source is a very bright AGN with a prominent and broad iron line, so it is quite a common source for testing reflection models. Here we have a good energy resolution from the *XMM*–*Newton* data and we can observe the Compton hump with *NuSTAR*.

We employ the reflection models RELCONV \times REFLIONX, RELCONV \times XILLVER, and RELXILL. The three models provide the same measurements for GRS 1915+105 while show some discrepancy for MCG-6-30-15. We discuss the origin of the discrepancies and the impact on the analysis of future observations. We stress that, considering the complexity of current reflection models, it is not an easy task to understand their systematic uncertainties. The choices of the sources, observations, and models may combine in a quite complicated way and it is difficult to arrive at very general conclusions on these reflection models. Additional work is thus necessary for a complete comprehension of this issue.

The content of this paper is as follows. In Section 2, we review the reflection models employed in our study, pointing out their differences. In Section 3, we present the analysis of a $2012 \, Suzaku$ observation of the black hole binary GRS 1915+105 and we fit the relativistic reflection component with RELCONV \times REFLIONX, RELCONV \times XILLVER, and RELXILL. In Section 4, we present a similar analysis of some simultaneous observations with XMM-Newton and NuSTAR of the AGN MCG-6-30-15. We discuss our results in Section 5.

2 RELATIVISTIC REFLECTION MODELS

The calculations of the reflection spectrum of the accretion disc of a black hole are normally split into two parts: (i) the calculations of the reflection spectrum in the rest frame of the gas, and (ii) the calculations of the spectrum at the detection point far from the source for a given spectrum at the emission point on the accretion disc. Part (i) depends on atomic physics (particle scattering, atomic energy levels, elemental abundance, etc.) and on some assumption about the material of the disc (e.g. density profile in the vertical direction), while does not directly depend on the actual geometry of the whole disc and the space—time metric. In other words, only microphysics is involved. Part (ii) concerns the macrophysics: the geometry of the accretion disc, the disc emissivity profile (which depends on

the coronal geometry), and the space–time metric (which affects the motion of the gas in the disc and determines all the relativistic effects).

Calculations of parts (i) and (ii) are connected employing the formalism of the transfer function (Cunningham 1975; Speith, Riffert & Ruder 1995; Bambi et al. 2017). The observed reflection spectrum can be written as

$$F_{\rm o}(\nu_{\rm o}) = \int g^3 I_{\rm e}(r_{\rm e}, \vartheta_{\rm e}) \, \mathrm{d}X \mathrm{d}Y \,, \tag{1}$$

where $g = v_o/v_e$ is the redshift factor, v_o and v_e are, respectively, the photon frequency at the detection point and at the emission point in the rest frame of the gas, I_e is the specific intensity of the radiation at the emission point in the rest frame of the gas, r_e is the emission radius, θ_e is the emission angle (i.e. the angle between the photon direction and the disc normal at the emission point in the rest frame of the gas), and X and Y are the Cartesian coordinates on the observer's plane. Introducing the transfer function, the observed reflection spectrum can be written as

$$F_{\rm o}(\nu_{\rm o}) = \frac{1}{D^2} \int_{R_{\rm in}}^{R_{\rm out}} \int_0^1 \frac{\pi r_{\rm e} g^2 f(g^*, r_{\rm e}, i)}{\sqrt{g^* (1 - g^*)}} I_{\rm e}(r_{\rm e}, \vartheta_{\rm e}) \, \mathrm{d}g^* \mathrm{d}r_{\rm e}, \qquad (2)$$

where $R_{\rm in}$ and $R_{\rm out}$ are, respectively, the inner and outer edges of the accretion disc, g^* ranges from 0 to 1 and is the relative redshift factor defined as

$$g^* = \frac{g - g_{\min}}{g_{\max} - g_{\min}},\tag{3}$$

where $g_{\text{max}} = g_{\text{max}}(r_{\text{e}}, i)$ and $g_{\text{min}} = g_{\text{min}}(r_{\text{e}}, i)$ are, respectively, the maximum and minimum redshift for photons emitted from the radius r_{e} and a disc's inclination angle i (i.e. the angle between the normal to the disc and the line of sight of the distant observer). The transfer function is

$$f(g^*, r_e, i) = \frac{g\sqrt{g^*(1 - g^*)}}{\pi r_e} \left| \frac{\partial (X, Y)}{\partial (g^*, r_e)} \right|, \tag{4}$$

where $|\partial(X, Y)/\partial(g^*, r_e)|$ is the Jacobian. For infinitesimally thin discs in Kerr space–times, for given values of r_e and i the transfer function is a closed curve parametrized by g^* . There is only one point with $g^* = 0$ and only one point with $g^* = 1$. There are two curves connecting these two points and there are thus two branches of the transfer function, say $f^{(1)}(g^*, r_e, i)$ and $f^{(2)}(g^*, r_e, i)$. We can thus rewrite F as

$$\begin{split} F_{\rm o}(\nu_{\rm o}) &= \frac{1}{D^2} \int_{R_{\rm in}}^{R_{\rm out}} \int_0^1 \frac{\pi r_{\rm e} g^2 f^{(1)}(g^*, r_{\rm e}, i)}{\sqrt{g^*(1-g^*)}} \, I_{\rm e}(r_{\rm e}, \vartheta_{\rm e}^{(1)}) \, {\rm d}g^* {\rm d}r_{\rm e} \\ &= \frac{1}{D^2} \int_{R_{\rm in}}^{R_{\rm out}} \int_0^1 \frac{\pi r_{\rm e} g^2 f^{(2)}(g^*, r_{\rm e}, i)}{\sqrt{g^*(1-g^*)}} \, I_{\rm e}(r_{\rm e}, \vartheta_{\rm e}^{(2)}) \, {\rm d}g^* {\rm d}r_{\rm e} \,. \end{split} \tag{5}$$

Note that $\vartheta_e^{(1)}$ and $\vartheta_e^{(2)}$ are the emission angles in the branches 1 and 2. In the general case of non-isotropic emission, the local specific intensity I_e depends on the photon emission angle and this requires to calculate the two integrals separately. For isotropic emission, equation (5) reduces to equation (2) with $f = f^{(1)} + f^{(2)}$. Note that in general $i \neq \vartheta_e^{(1)} \neq \vartheta_e^{(2)}$ because of the light bending of the space–time.

In the rest of the paper, we will employ the two most popular models for the calculation of the reflection spectrum at the emission point in the rest frame of the gas, namely REFLIONX (Ross & Fabian 2005) and XILLVER (García & Kallman 2010; García et al. 2013). These two models are used to calculate the shape of the local specific intensity $I_{\rm e}$, while the normalization of the spectrum is determined by the emissivity profile of the disc, which should depend on the coronal geometry. We note that XILLVER provides an angle-resolved reflected flux, while REFLIONX only provides the angle-averaged reflection intensity. XILLVER also incorporates a richer atomic data

Table 1. Summary of the observations analysed in this work. The total counts refer to the energy range used in the analysis and specified in the text for every instrument. Note that in the case of MCG-6-30-15, the data are rearranged in four flux states and the total counts refer to the sum of all flux states.

Source	Satellite	Obs. ID	Total counts (10 ⁶)
GRS 1915+105	Suzaku	402071010	2.43 (XIS1) 1.36 (HXD/PIN)
MCG-6-30-15	XMM–Newton	0693781201 0693781301 0693781401	1.74 (EPIC-Pn)
	NuSTAR	60001047002 60001047003 60001047005	0.147 (FPMA) 0.141 (FPMB)

base than REFLIONX (see García et al. 2013). As a convolution model, we will use RELLINE/RELCONV (Dauser et al. 2010, 2013), in which the disc is described by an infinitesimally thin Novikov-Thorne disc and the space-time is described by the Kerr metric. We will thus consider three possible relativistic reflection models: RELCONV × REFLIONX, RELCONV × XILLVER, and RELXILL. RELCONV × REFLIONX and RELCONV × XILLVER are, respectively, the reflection spectra calculated with REFLIONX and XILLVER and convolved with RELCONV. The two models only differ from the calculation of the reflection spectrum in the rest frame of the gas and employ the same convolution model. In particular, both models assume that $i = \vartheta_{\alpha}^{(1)} = \vartheta_{\alpha}^{(2)}$, which is an approximation and does not take the position-dependent photon emission angle into account. Indeed, because of light bending $\vartheta_e^{(1)}$ and $\vartheta_e^{(2)}$ should change at every point on the disc and be different from i, but when we apply RELCONV to REFLIONX or XILLVER we ignore such a difference (angle-averaged models). RELXILL (Dauser et al. 2013; García et al. 2014) employs the reflection model XILLVER and is equivalent to RELCONV × XILLVER but without the assumption $i = \vartheta_e^{(\hat{1})} = \vartheta_e^{(2)}$ (angle-resolved model). Note that such an approximation is justified by the fact that relativistic effects (Doppler boosting) are very sensitive to the inclination angle of the disc i, while the local specific intensity I_e is not so much sensitive to the exact photon emission angle θ_e .

3 REFLECTION SPECTRUM OF GRS 1915+105

GRS 1915+105 is a black hole binary with some peculiar properties. While it is a low-mass X-ray binary, it is a persistent X-ray source since 1992, when it went into outburst and was discovered by the WATCH instrument on board of the *Granat* satellite (Castro-Tirado, Brandt & Lund 1992). The most recent estimates of the source distance and black hole mass are, respectively, $D = 8.6^{+2.0}_{-1.6}$ kpc and $M = 12.4^{+2.0}_{-1.8}$ M $_{\odot}$ (Reid et al. 2014). GRS 1915+105 is a very variable source across all bands of the electromagnetic spectrum (Belloni et al. 2000) and is often considered as the archetype of microquasars (Mirabel & Rodríguez 1999). The black hole spin has been estimated either using the continuum-fitting method (McClintock et al. 2006) and X-ray reflection spectroscopy (Blum et al. 2009; Miller et al. 2013; Zhang et al. 2019; Abdikamalov et al. 2020), and all studies agree that the black hole is rotating very fast, with a spin parameter a_* close to 1.

3.1 Observation and data reduction

Suzaku observed GRS 1915+105 on 2007-5-7 for approximately 117 ks (obs. ID 402071010), see Table 1, while the source was in a low/hard flux state. The first analysis of this observation was reported

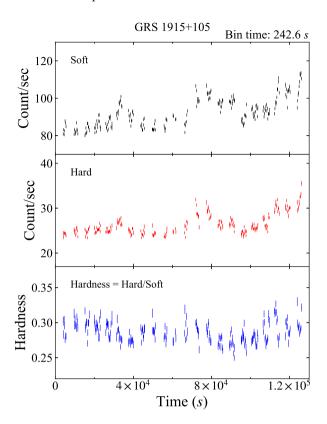


Figure 1. GRS 1915+105 – Light curves of the *Suzaku*/XIS1 data (0.2–12 keV, upper panel), *Suzaku*/HXD data (10–70 keV, central panel), and temporal evolution of the hardness of the spectrum (bottom panel). From Zhang et al. (2019).

in Blum et al. (2009), where the authors find $a_*=0.98\pm0.01$ (1σ confidence) in the analysis of the full broad-band spectrum. As in Blum et al. (2009), here we only use the data from the XIS1 and HXD/PIN instruments. Two other XIS units were turned off during the observation to preserve telemetry. The fourth unit was run in a special timing mode.

For the data reduction of both instruments, we follow Blum et al. (2009) and here we only report the main steps. Unfiltered event files of XIS1 are processed following the Suzaku Darta Reduction ABC Guide with aepipeline to create a clean event file using XIS CALDB version 20151005. Since XIS1 data are affected by pile up, the source region is an annulus (inner radius 78 arcsec, outer radius 208 arcsec). For the background region, we select an annulus with inner radius 208 arcsec and outer radius 278 arcsec. Redistribution matrix file and ancillary response file are created using the tools xisrmfgen and xissimarfgen available in the HEASOFT version 6.26.1 data reduction package. After all efficiencies and screening, the net exposure time is around 29 ks. Data are grouped using grppha to a minimum of 25 counts per bin. We only analyse the 2.3–10.0 keV energy band to avoid calibration problems near the Si K edge and because of the low number of photons at low energies due to the high absorption. For the HXD/PIN data, we proceed in a similar way. We use aepipeline and hxdpinxbpi with CALDB version 20110913. After all efficiencies and screening, the net exposure time is around 53 ks. Data are grouped using grppha to a minimum of 25 counts per bin. We analyse the 12.0-55.0 keV energy band. The cross-calibration constant between XIS1 and HXD/PIN data is left free, because the XIS data are affected by pile-up.

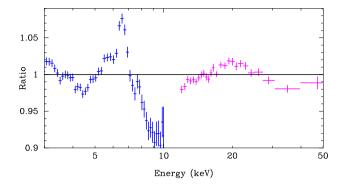


Figure 2. GRS 1915+105 – Data to best-fitting model ratio for TBABS \times CUTOFFPL. Blue crosses are used for Suzaku/XIS1 data and magenta crosses are used for Suzaku/HXD data.

While GRS 1915+105 is normally a very variable source, its hardness was quite stable during this *Suzaku* observation, so the spectral analysis does not require any particular treatment to take the source variability into account. The light curves of the XIS1 and HXD/PIN data and the temporal evolution of the hardness of the source are shown in Fig. 1.

3.2 Spectral analysis

We use XSPEC v 12.10.1f (Arnaud 1996). The data can be fitted with an absorbed coronal and relativistic reflection components and no other components seem to be necessary (Blum et al. 2009; Zhang et al. 2019). In XSPEC language, the model is $TBABS \times (CUTOFFPL + RR)$.

TBABS models the Galactic absorption (Wilms, Allen & McCray 2000), and its hydrogen column density $N_{\rm H}$ is left free in the fit. CUTOFFPL describes a power-law component (photon index Γ) with a high energy exponential cut-off (E_{cut}). We have three free parameters from this component in the fit: $\Gamma,\,E_{\rm cut},$ and the normalization of the component. If we fit the data with the model TBABS × CUTOFFPL, we find the data to best-fitting model ratio shown in Fig. 2, where we can clearly see relativistic reflection features, with a broad iron line in the soft X-ray band and the Compton hump in the hard X-ray band. RR indicates a relativistic reflection component and we employ three models: RELCONV × REFLIONX, RELCONV × XILLVER, and RELXILL. We model the emissivity profile of the disc with a broken power law and we have eight free parameters: black hole spin (a_*) , inclination angle of the disc (i), inner emissivity index (q_{in}), outer emissivity index (q_{out}) , breaking radius (R_{br}) , iron abundance (A_{Fe}) , ionization parameter (ξ) , and normalization of the component. When we use RELCONV × XILLVER and RELXILL, the reflection fraction is frozen to -1 because the coronal spectrum is described with CUFOFFPL. The photon index and the high energy cut-off of the radiation illuminating the disc are tied to Γ and $E_{\rm cut}$ in CUFOFFPL.

Fig. 3 shows the best-fitting models and the data to best-fitting model ratios of the three scenarios. The best-fitting values are reported in Table 2. Figs 4 and 5 show, respectively, the constraints on the black hole spin a_* and the inclination angle of the disc i and on the inner emissivity index $q_{\rm in}$ and the inclination angle of the disc i. The red, green, and blue curves correspond, respectively, to the 68 per cent, 90 per cent, and 99 per cent confidence level limits for two relevant parameters. A quick look already sees that the fit with RELCONV \times REFLIONX is slightly worse, but all the measurements of the three models are perfectly consistent among them. A more detailed discussion on these fits is postponed to Section 5.

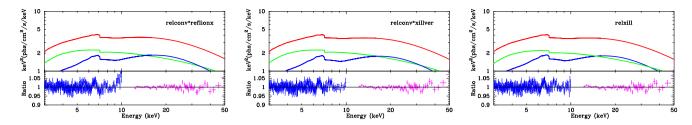


Figure 3. GRS 1915+105 – Best-fitting models (top quadrants) and data to best-fitting model ratios (bottom quadrants) for the models RELCONV × REFLIONX (left-hand panel), RELCONV × XILLVER (central panel), and RELXILL (right-hand panel). The red, blue, and green curves correspond, respectively, to the total spectrum, the relativistic reflection component, and the power-law component.

Table 2. GRS 1915+105 – Summary of the best-fitting values for the models RELCONV × REFLIONX, RELCONV × XILLVER, and RELXILL. The reported uncertainties correspond to the 90 per cent confidence level for one relevant parameter ($\Delta \chi^2 = 2.71$). ξ in units of erg cm s⁻¹. In REFLIONX, the fitting parameter is ξ , not $\log \xi$ as in XILLVER and RELXILL, but it is converted into $\log \xi$ in the table in order to facilitate the comparison with the other models. See the text for the details.

Model	$RELCONV \times REFLIONX$	$RELCONV \times XILLVER$	RELXILL	
TBABS				
$N_{\rm H}/10^{22}~{\rm cm}^{-2}$	$5.16^{+0.10}_{-0.03}$	$5.25^{+0.03}_{-0.03}$	$5.19^{+0.07}_{-0.03}$	
CUTOFFPL				
Γ	$2.145^{+0.027}_{-0.003}$	$2.200^{+0.018}_{-0.017}$	$2.197^{+0.009}_{-0.003}$	
$E_{\rm cut}$ [keV]	$58.7^{+0.8}_{-1.4}$	$71.7^{+1.6}_{-6.0}$	$70.7^{+1.7}_{-4.0}$	
$N_{ m CUTOFFPL}$	$3.99^{+0.10}_{-0.09}$	$3.93^{+0.36}_{-0.15}$	$3.82^{+0.29}_{-0.07}$	
$q_{ m in}$	$10.00_{-0.24}$	$9.9^{+(P)}_{-0.3}$	$10.0_{-1.6}$	
$q_{ m out}$	$0.0^{+0.3}$	$0.00^{+0.22}$	$0.00^{+0.21}$	
$R_{\rm br} [M]$	$5.84^{+0.47}_{-0.16}$	$6.3^{+0.3}_{-0.3}$	$6.27^{+0.47}_{-0.13}$	
a_*	$0.9945^{+0.0013}_{-0.0048}$	$0.991^{+0.004}_{-0.003}$	$0.9908^{+0.0015}_{-0.0017}$	
i [deg]	$77.1^{+0.6}_{-1.9}$	$73.5^{+1.0}_{-1.9}$	$73.8^{+0.8}_{-0.4}$	
$\log \xi$	$2.80^{+0.03}_{-0.03}$	$2.74^{+0.03}_{-0.05}$	$2.77^{+0.05}_{-0.03}$	
A_{Fe}	$0.46^{+0.03}_{-0.03}$	$0.51^{+0.11}_{-(P)}$	$0.57^{+0.07}_{-0.05}$	
N_{REFLIONX}	90^{+4}_{-5}	=	-	
$N_{\rm XILLVER}~(10^{-3})$	-	156^{+10}_{-21}	-	
$N_{\rm RELXILL}~(10^{-3})$	-	-	$20.9_{-1.2}^{+0.5}$	
χ^2/dof	2350.55/2210 = 1.06360	2335.56/2210 = 1.05682	2328.70/2210 = 1.05371	

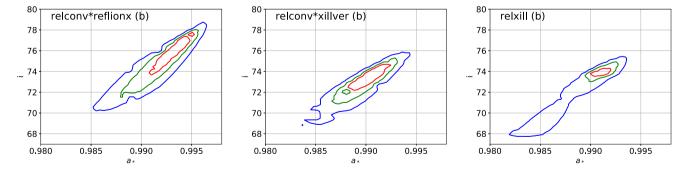


Figure 4. GRS 1915+105 – Constraints on the black hole spin parameter a_* and the inclination angle of the disc i for the models RELCONV × REFLIONX (left-hand panel), RELCONV × XILLVER (central panel), and RELXILL (right-hand panel). The red, green, and blue curves correspond, respectively, to the 68 per cent, 90 per cent, and 99 per cent confidence level limits for two relevant parameters.

4 REFLECTION SPECTRUM OF MCG-6-30-15

MCG-6-30-15 is a very bright Seyfert 1 galaxy at redshift z = 0.007749. This source has been studied by many authors with different observations and different X-ray missions (see e.g. Iwasawa

et al. 1996; Guainazzi et al. 1999; Fabian et al. 2002; Brenneman & Reynolds 2006; Miniutti et al. 2007; Marinucci et al. 2014). It is the source in which a relativistically broadened iron line was unambiguously detected for the first time (Tanaka et al. 1995). Indeed its spectrum often shows a very broad and prominent iron K α line.

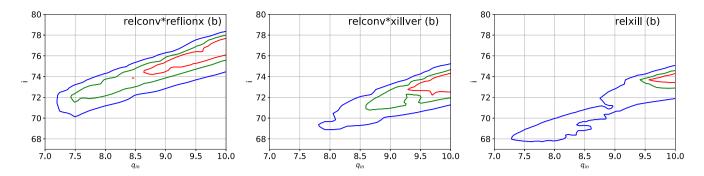


Figure 5. GRS 1915+105 – Constraints on the inner emissivity index q_{in} and the inclination angle of the disc i for the models RELCONV × REFLIONX (left-hand panel), RELCONV × XILLVER (central panel), and RELXILL (right-hand panel). The red, green, and blue curves correspond, respectively, to the 68 per cent, 90 per cent, and 99 per cent confidence level limits for two relevant parameters.

This makes MCG-6-30-15 an excellent candidate for a number of studies of relativistic reflection spectra. The source is very variable, so the data analysis requires some special attention. There are a few measurements in literature of the spin of the black hole in MCG-6-30-15 and they all agree in a very high value of the spin parameter a_* (Brenneman & Reynolds 2006; Marinucci et al. 2014; Tripathi et al. 2019).

4.1 Observations and data reduction

XMM–*Newton* and *NuSTAR* observed simultaneously MCG-6-30-15 from 2013-1-29 for a total time of \sim 315 and \sim 360 ks, respectively (obs. ID 0693781201, 0693781301, and 0693781401 for *XMM*–*Newton* and obs. ID 60001047002, 60001047003, and 60001047005 for *NuSTAR*); see Table 1. The first study of these data was reported in Marinucci et al. (2014), where the estimates of the spin parameter and the inclination angle of the disc are, respectively, $a_* = 0.91^{+0.06}_{-0.07}$ and $i = 33^{\circ} \pm 3^{\circ}$.

For the data reduction, we follow Tripathi et al. (2019). Here, we only outline the main passages. For the XMM-Newton data, we only use Pn data because they are of higher quality, while the MOS data are significantly affected by pile up. We use SAS version 16.0.0 to convert raw data into event files. The latter are combined into a single FITS file using the ftool fmerge; good time intervals (GTIs) are generated using tabtigen and then used to filter the event files. The source region is a circle of radius 40 arcsec and the background region is a circle of radius 50 arcsec. Spectra are rebinned to oversample the instrumental resolution by at least a factor of 3 and have at least 50 counts in each background subtracted bin. As for the NuSTAR data, we use the HEASOFT task nupipeline with CALDB version 20180312 to generate the event files. The source region is a circle of radius 70 arcsec and the background region is a circle of radius 100 arcsec. Spectra are rebinned to guarantee at least 70 counts per bin.

MCG-6-30-15 is very variable and it is thus necessary to use simultaneous data in order to properly take the variability into account. Here, we use the ftool mgtime to find the common GTIs of the two telescopes.

4.2 Spectral analysis

Since the source is very variable during the *XMM*–*Newton* and *NuSTAR* observations, see the light curves in Fig. 6, we proceed as in Tripathi et al. (2019). We arrange the data into four groups according to the flux state of the source (low, medium, high, and

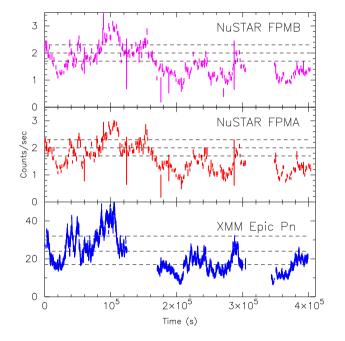


Figure 6. MCG-6-30-15 – *NuSTAR*/FPMA, *NuSTAR*/FPMB, and *XMM*–*Newton*/EPIC-Pn light curves. The dashed horizontal lines separate the different flux states (low, medium, high, and very-high).

very-high flux states) requiring similar spectral data count for every flux state. We use XSPEC v 12.10.1f (Arnaud 1996).

The *XMM*–*Newton* data show a spurious emission around 2 keV (Marinucci et al. 2014). This is interpreted as an effect of the golden edge in the response file due to miscalibration in the long-term charge transfer inefficiency. We cannot fit this feature with an ad hoc Gaussian because, otherwise, this would modify the way in which warm absorbers and ionized reflectors reproduce the data. We thus ignore the 1.5–2.5 keV energy band in the *XMM*–*Newton* data.

The search for the model is described in Tripathi et al. (2019). If we fit the data with an absorbed power law, we clearly see typical relativistic reflection features: a broad iron line peaked around 6 keV, a soft excess below 1 keV, and a Compton hump peaked at 20–30 keV, see Fig. 7.

The final model is TBABS \times WARMABS₁ \times WARMABS₂ \times DUSTYABS \times (CUTOFFPL + RR + NR + ZGAUSS + ZGAUSS). TBABS describes the Galactic absorption and we fix the column density $N_{\rm H} = 3.9 \times 10^{20}~{\rm cm}^{-2}$ (Dickey & Lockman 1990). WARMABS₁ and

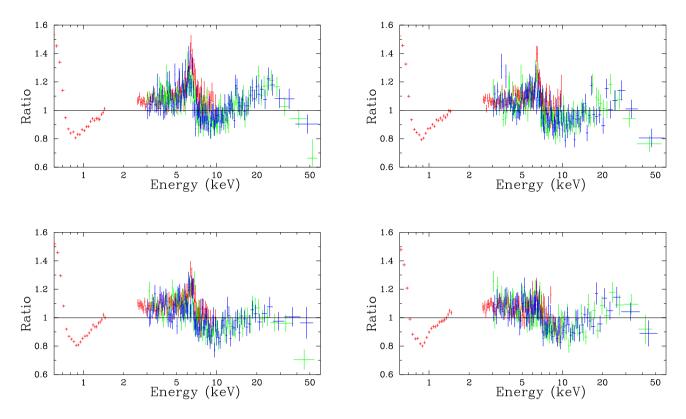


Figure 7. MCG-6-30-15 – Data to best-fitting model ratio for TBABS \times CUTOFFPL for the low flux state (top left panel), medium flux state (top right panel), high flux state (bottom left panel), and very-high flux state (bottom right panel). Red crosses are used for *XMM–Newton* data, green crosses are used for *NuSTAR*/FPMB.

WARMABS₂ describe two ionized absorbers; their tables are generated with XSTAR v2.41. DUSTYABS describes a neutral absorber and only modifies the soft X-ray band (Lee et al. 2001). CUTOFFPL describes the direct spectrum from the corona. RR and NR indicate, respectively, a relativistic and a non-relativistic reflection component. When we use REFLIONX, we have RR = RELCONV × REFLIONX and NR = REFLIONX. When RR is either RELCONV × XILLVER or RELXILL, NR is XILLVER. The non-relativistic reflection component is interpreted as some cold material faraway from the black hole, so we set its ionization parameter to the minimum value allowed by the model. We model the emissivity profile of the accretion disc either with a simple power law [indicated with (s) in our tables and figures] and a broken power law [indicated with (b) in our tables and figures]. ZGAUSS is used to describe a narrow emission line around 0.8 keV, which is interpreted as an oxygen line, and a narrow absorption line at 1.2 keV, interpreted as blueshifted oxygen absorption caused by the presence of relativistic outflows (Leighly et al. 1997).

Note that some model parameters cannot vary on a time-scale of a few days and therefore their value should be the same over different flux states. These are the black hole spin a_* , the inclination angle of the disc i, and the iron abundance $A_{\rm Fe}$ as well as all the model parameters related to material at larger radii and appearing in DUSTYABS, NR, and ZGAUSS.

The best-fitting values are reported in Table 3 (RELCONV \times REFLIONX), Table 4 (RELCONV \times XILLVER), and Table 5 (RELXILL). In every table, we show the fit with the emissivity profile of the disc modelled by a simple power law (left) and by a broken power law (right). For every model, there are four columns, corresponding to the low, medium, high, and very-high flux states, respectively. Fig. 8 shows the best-fitting models of the low flux states and the data to best-fitting model ratios. Fig. 9 is for the constraints on

the spin parameter a_* and the inclination angle of the disc i for the six scenarios considered in our analysis. Unlike the analysis of the Suzaku observation of GRS 1915+105, here we see some differences and the best-fitting values from different models are not always consistent.

5 DISCUSSION AND CONCLUSIONS

Previous studies have already investigated the performance of the reflection model RELXILL in the analysis of X-ray reflection spectra of accreting black holes. In general, it is found that reliable spin measurements can only be obtained if the corona illuminates well the inner part of the accretion disc (within the lamppost set-up, this requires that the corona height is low) and if the spin parameter is high (see Bonson & Gallo 2016; Choudhury et al. 2017; Kammoun, Nardini & Risaliti 2018; Barret & Cappi 2019). This work is focused on the differences between the reflection models RELCONV × REFLIONX, RELCONV × XILLVER, and RELXILL and we have analysed a Suzaku observation of the high viewing angle black hole binary GRS 1915+105 and simultaneous XMM-Newton and *NuSTAR* observations of the low viewing angle AGN MCG-6-30-15. Both sources are usually thought to host a fast rotating black hole [GRS 1915+105: Miller et al. (2013), MCG-6-30-15: Marinucci et al. (2014)]. The steep emissivity of GRS 1915+105 also implies a corona that illuminates well the inner part of the disc, which is a required ingredient for a reliable measurement.

For the *Suzaku* observation of GRS 1915+105, the three models provide quite similar fits. The estimates of the model parameters are consistent, with only some minor discrepancy in the estimate of the high energy cut-off $E_{\rm cut}$ of the coronal spectrum. We find a high

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Table 3. MCG-6-30-15 – Summary of the best-fitting values for the models RELCONV × REFLIONX (s) and RELCONV × REFLIONX (b). The reported uncertainties correspond to the 90 per cent confidence level for one relevant parameter ($\Delta \chi^2 = 2.71$). ξ, ξ', ξ_1 , and ξ_2 in units of erg cm s⁻¹. In REFLIONX, the fitting parameter is ξ , not $\log \xi$ as in XILLVER and RELXILL, but it is converted into $\log \xi$ in the table in order to facilitate the comparison with the other models. See the text for the details.

Model	$RELCONV \times REFLIONX (s)$			RELCONV × REFLIONX (b)					
Flux state	1	2	3	4	1	2	3	4	
TBABS $N_{\rm H}/10^{22}~{\rm cm}^{-2}$	0.039*				0.039*				
WARMABS ₁ $N_{\rm H1}/10^{22}~{\rm cm}^{-2}$ $\log \xi_1$	$0.323^{+0.015}_{-0.014} \\ 2.258^{+0.029}_{-0.023}$	$0.426^{+0.023}_{-0.022} \\ 2.391^{+0.024}_{-0.024}$	$0.388^{+0.021}_{-0.020}$ $2.397^{+0.026}_{-0.025}$	$0.09_{-0}^{+0.05}$ $1.38_{-0.30}^{+0.22}$	$0.33_{-0.06}^{+0.05} \\ 2.23_{-0.08}^{+0.10}$	$0.44^{+0.06}_{-0.07}$ $2.33^{+0.07}_{-0.07}$	$0.39_{-0.07}^{+0.09} \\ 2.35_{-0.10}^{+0.10}$	$0.38^{+0.09}_{-0.05}$ $2.45^{+0.11}_{-0.07}$	
WARMABS ₂ $N_{\rm H2}/10^{22}~{\rm cm}^{-2}$ $\log \xi_2$	$2.58^{+0.16}_{-0.15}$ $3.347^{+0.012}_{-0.012}$	$1.29^{+0.11}_{-0.13}$ $3.324^{+0.020}_{-0.021}$	$1.45^{+0.11}_{-0.10}$ $3.291^{+0.020}_{-0.019}$	$0.386^{+0.036}_{-0.021}$ $2.40^{+0.03}_{-0.03}$	$1.9^{+0.5}_{-0.4}$ $3.28^{+0.05}_{-0.05}$	$1.7^{+0.9}_{-0.4}$ $3.32^{+0.06}_{-0.05}$	$1.9^{+0.4}_{-0.4}$ $3.29^{+0.05}_{-0.05}$	$1.8^{+1.1}_{-0.9}$ $3.41^{+0.06}_{-0.10}$	
DUSTYABS $log (N_{Fe}/10^{21} cm^{-2})$		17.663	$2^{+0.0030}_{-0.0033}$			17.628 ^{+0.019} _{-0.017}			
CUTOFFPL Γ $E_{\rm cut} \ [{\rm keV}]$ $N_{\rm CUTOFFPL} \ (10^{-3})$	$1.8571^{+0.0025}_{-0.0025}$ 207^{+26}_{-19} $8.42^{+0.13}_{-0.13}$	$1.8711^{+0.0025}_{-0.0025}$ 96^{+6}_{-5} $12.47^{+0.15}_{-0.15}$	$1.9269^{+0.0026}_{-0.0026}$ 90^{+5}_{-4} $18.03^{+0.20}_{-0.20}$	$1.961^{+0.003}_{-0.003}$ 90^{+5}_{-4} $26.93^{+0.20}_{-0.09}$	$1.843^{+0.012}_{-0.013}$ 218^{+74}_{-56} $7.8^{+0.6}_{-0.4}$	$1.868^{+0.012}_{-0.011}$ 114^{+32}_{-20} $11.8^{+0.5}_{-0.5}$	$1.924_{-0.012}^{+0.012}$ 108_{-19}^{+28} $16.7_{-0.8}^{+0.8}$	$1.948^{+0.013}_{-0.014}$ 147^{+63}_{-34} $23.2^{+1.2}_{-1.1}$	
RELCONV q _{in}	$3.03^{+0.04}_{-0.20}$	$2.71^{+0.05}_{-0.05}$	$2.79^{+0.05}_{-0.05}$	$2.5^{+0.3}_{-0.3}$	5 ^{+(P)} _{-(P)}	$3.6^{+0.6}_{-0.6}$	$4.4^{+5.2}_{-1.1}$	$6.0^{+2.3}_{-1.2}$	
q_{out} $R_{\text{br}}[M]$ $i [\text{deg}]$	$=q_{\mathrm{in}}$	=q _{in} -	$=q_{\rm in}$ $ 2^{+1.6}_{-1.7}$	=q _{in} -	$2.65_{-0.23}^{+0.22} 4.3_{-2.2}^{+2.2}$	$1.9_{-0.4}^{+0.7}$ 20_{-13}	$2.3_{-0.8}^{+0.4} \\ 9_{-4}^{+(P)}$	$1.8_{-0.7}^{+0.6} \\ 9_{-4}^{+(P)}$	
a_*			2-1.7 +0.03 -0.04		$19^{+5}_{-5} \\ 0.88^{+0.04}_{-0.08}$				
REFLIONX Z	0.012		7749*	10 047	10.04		7749*	10.06	
$\log \xi$ A_{Fe}	$2.744^{+0.012}_{-0.003}$		$2.505^{+0.051}_{-0.025}$ $^{+0.08}_{-0.07}$	$2.094^{+0.047}_{-0.017}$	$2.78^{+0.04}_{-0.04}$		$\begin{array}{c} 2.74^{+0.04}_{-0.03} \\ ^{+0.4}_{-0.4} \end{array}$	$2.80^{+0.06}_{-0.05}$	
$N_{\text{REFLIONX}} (10^{-6})$ REFLIONX	$0.111^{+0.059}_{-0.013}$	$0.236^{+0.033}_{-0.019}$	$0.370^{+0.043}_{-0.025}$	$1.38^{+0.03}_{-0.09}$	$0.133^{+0.016}_{-0.015}$	$0.195^{+0.021}_{-0.018}$	$0.30^{+0.04}_{-0.05}$	$0.33^{+0.04}_{-0.04}$	
$\log \xi'$ $N'_{\text{REFLIONX}} (10^{-6})$	0* 69 ⁺⁴			0* 59 ⁺⁸ ₋₈					
ZGAUSS E_{line} [keV]	$1.261^{+0.006}_{-0.012}$			$1.260^{+0.011}_{-0.010}$					
χ^2/dof		3171.36/269	01 = 1.17850			3130.26/268	33 = 1.16670		

inclination angle ($i \approx 70^{\circ}$) is always needed to fit the data, which is consistent with previous studies with NuSTAR observations (e.g. Miller et al. 2013; Shreeram & Ingram 2020). All models require a very high inner emissivity index q_{in} and an outer emissivity index qout close to zero. Such an emissivity profile was already found for GRS 1915+105 in a *NuSTAR* observation of 2012 (Miller et al. 2013), as well as for other black hole binaries, such as in the 2015 NuSTAR observation of GS 1354-645 analysed in El-Batal et al. (2016). A similar emissivity profile can be explained by a ring-like or disc-like corona above the accretion disc and with the axis parallel to the black hole spin (Miniutti et al. 2003; Wilkins & Fabian 2011; Wilkins & Gallo 2015b). As shown in Fig. 5, there is a correlation between $q_{\rm in}$ and i. Such a high value for q_{in} imposes a strong gravitational redshift to the iron line, and a way to compensate such an extreme redshift is a high viewing angle i, permitting a strong Doppler blueshift and moving the blue side of the iron line to higher energies. A similar effect was reported in García et al. (2018) for the black hole binary

in XTE J1752–223; in that case, a lamppost model was able to reproduce the data with a significantly lower viewing angle, and we may wonder whether a lamppost profile may reduce the value of the viewing angle and provide a better fit even here for GRS 1915+105. If we replace RELXILL with RELXILLLP and we refit the *Suzaku* data of GRS 1915+105, we find a very low viewing angle $i \approx 30^\circ$, which has never been reported for this source, a higher χ^2 ($\Delta \chi^2 \approx 65$ with respect to the broken power-law profile), and the spin cannot be constrained. The lamppost set-up does not seem the correct model for this observation and we prefer the previous interpretation of a ring-like or disc-like corona.

Another issue concerns the possibility of the presence of a distant reflector, as we see some unresolved features in the ratio plots in Fig. 3 and a distant reflector was reported previously for this source (e.g. Shreeram & Ingram 2020). However, if we add a non-relativistic reflection component to the Suzaku observation, the fit only improves marginally: χ^2 is only a bit lower (for example, in the

Table 4. MCG-6-30-15 – Summary of the best-fitting values for the models RELCONV × XILLVER (s) and RELCONV × XILLVER (b). The reported uncertainties correspond to the 90 per cent confidence level for one relevant parameter ($\Delta \chi^2 = 2.71$). ξ, ξ', ξ_1 , and ξ_2 in units of erg cm s⁻¹. See the text for the details.

Model		RELCONV × XILLVER (s)				RELCONV × XILLVER (b)			
Flux state	1	2	3	4	1	2	3	4	
TBABS N _H /10 ²² cm ⁻²	0.039*				0.039*				
WARMABS ₁ $N_{\rm HI}/10^{22}~\rm cm^{-2}$ $\log \xi_1$	$0.25^{+0.07}_{-0.04}$ $1.91^{+0.18}_{-0.09}$	$1.18^{+0.09}_{-0.07} \\ 2.005^{+0.023}_{-0.021}$	$1.36_{-0.06}^{+0.07} 2.01_{-0.021}^{+0.022}$	$1.10^{+0.07}_{-0.09}$ $1.982^{+0.025}_{-0.033}$	$0.669^{+0.012}_{-0.030}$ $1.843^{+0.043}_{-0.010}$	$0.10^{+0.19}_{-(P)}$ $1.84^{+0.53}_{-0.25}$	$1.03_{-0.06}^{+0.06} \\ 1.914_{-0.019}^{+0.031}$	$0.64_{-0.07}^{+0.05}$ $1.77_{-0.05}^{+0.04}$	
WARMABS ₂ $N_{\rm H2}/10^{22}~{\rm cm}^{-2}$ $\log \xi_2$	$1.00_{-0.10}^{+0.11} 2.00_{-0.05}^{+0.05}$	$0.060^{+0.008}_{-0.004} \\ 2.14^{+0.08}_{-0.38}$	$0.23_{-0.16}^{+0.43} \\ 3.20_{-0.19}^{+0.27}$	$0.06^{+0.10}_{-(P)} \\ 2.7^{+(P)}_{-0.4}$	$0.487^{+0.031}_{-0.011} \\ 1.86^{+0.06}_{-0.03}$	$1.07^{+0.08}_{-0.07} \\ 1.900^{+0.037}_{-0.024}$	$0.59_{-0.19}^{+0.23}$ $3.25_{-0.08}^{+0.06}$	$0.32_{-0.06}^{+0.08} \\ 2.51_{-0.14}^{+0.11}$	
DUSTYABS $\log (N_{\text{Fe}}/10^{21} \text{ cm}^{-2})$	$17.391^{+0.030}_{-0.022}$					17.4	$1^{+0.03}_{-0.04}$		
CUTOFFPL Γ $E_{\rm cut}$ [keV] $N_{\rm CUTOFFPL}$ (10^{-3})	$1.949^{+0.009}_{-0.016}$ 193^{+57}_{-44} $8.8^{+0.4}_{-0.5}$	$1.973_{-0.007}^{+0.013}$ 142_{-28}^{+50} $13.24_{-0.5}^{+0.3}$	$2.045^{+0.009}_{-0.012}$ 193^{+92}_{-51} $19.7^{+0.8}_{-1.3}$	$2.056^{+0.007}_{-0.009}$ 500_{-183} $27.3^{+1.9}_{-1.7}$	$1.968^{+0.014}_{-0.015}$ $344^{+(P)}_{-109}$ $8.7^{+0.4}_{-0.4}$	$1.987^{+0.013}_{-0.013}$ 183^{+61}_{-39} $12.9^{+0.5}_{-0.7}$	$2.025^{+0.013}_{-0.015}$ 162^{+46}_{-35} $17.8^{+1.0}_{-1.2}$	$2.029_{-0.014}^{+0.014}$ 201_{-47}^{+84} $23.9_{-1.8}^{+1.6}$	
RELCONV $q_{ m in}$ $q_{ m out}$ $R_{ m br}$ [M]	$2.91^{+0.18}_{-0.16}$ = $q_{\rm in}$	$2.87^{+0.19}_{-0.13} = q_{\text{in}}$	$ 2.86^{+0.21}_{-0.22} \\ = q_{\text{in}} \\ - $	$2.9_{-0.3}^{+0.3} = q_{\text{in}}$	$0.9_{-(P)}^{+3.2}$ $2.86_{-0.35}^{+0.15}$ $3_{-(P)}^{+7}$	$3.9^{+1.4}_{-2.5}$ $2.6^{+0.4}_{-0.7}$ $7^{+(P)}_{-(P)}$	$4.1_{-0.5}^{+0.6}$ $1.6_{-0.5}^{+0.8}$ $19_{-7}^{+(P)}$	$10.0_{-1.7} 2.7^{+0.3}_{-0.3} 3.6^{+3.1}_{-0.4}$	
i [deg] a_*	$\begin{array}{c} 29.0^{+2.2}_{-2.3} \\ 0.90^{+0.06}_{-0.07} \end{array}$				$30.7_{-2.5}^{+2.2} 0.915_{-0.030}^{+0.024}$				
XILLVER z $\log \xi$ A_{Fe}	$2.85^{+0.13}_{-0.04}$	$2.87^{+0.14}_{-0.04}$	7749^{*} $2.94^{+0.15}_{-0.12}$ $^{+0.6}_{-0.6}$	$3.056^{+0.021}_{-0.056}$	$2.92^{+0.09}_{-0.11}$	$2.93^{+0.08}_{-0.09}$	7749* 3.010 ^{+0.023} -0.151 -0.4	$3.04^{+0.04}_{-0.03}$	
$N_{\text{XILLVER}} (10^{-3})$	$0.088^{+0.008}_{-0.008}$	$0.104^{+0.009}_{-0.010}$	$0.136^{+0.017}_{-0.015}$	$0.141^{+0.021}_{-0.021}$	$0.108^{+0.009}_{-0.010}$	$0.128^{+0.012}_{-0.013}$	$0.183^{+0.018}_{-0.016}$	$0.25^{+0.03}_{-0.03}$	
XILLVER $\log \xi'$ $N'_{\text{XILLVER}} (10^{-3})$	0^{\star} $0.059^{+0.010}_{-0.009}$				0^{\star} $0.054^{+0.011}_{-0.010}$				
ZGAUSS E _{line} [keV]	$0.8237^{+0.0018}_{-0.0004}$			$0.8050^{+0.0022}_{-0.0021}$					
ZGAUSS E_{line} [keV]	$1.241^{+0.010}_{-0.010}$			$1.224^{+0.011}_{-0.012}$					
χ^2/dof	3094.68/2689 = 1.15087			3079.54/2681 = 1.14865					

model with RELXILL, we find $\Delta\chi^2\approx-3$), the normalization of the non-relativistic reflection component is very low, and the unresolved features in the ratio plot remain without significant changes. Once again, we are instead tempted to argue that the interpretation of the ring-like corona is more convincing. Indeed, in the presence of a ring-like corona above the accretion disc, we should expect the Comptonization of the relativistic reflection component. When such a reflection Comptonization is not included in the model, we find residuals similar to those appearing in Fig. 3 (Wilkins & Gallo 2015a).

The fact that we obtain very similar results with RELCONV \times XILLVER and RELXILL suggests that the angle dependence of the spectrum emitted from every point of the accretion disc does not play any appreciable role in the *Suzaku* data of GRS 1915+105. Since we find similar estimates of the model parameters from RELCONV \times REFLIONX and RELCONV \times XILLVER, we conclude that even the

choice of the reflection model does not affect the estimate of the properties of the system. Since REFLIONX and XILLVER have been developed independently by different groups, we would be tempted to conclude that systematic uncertainties in the calculation of the reflection spectrum in the rest frame of the gas in the disc (which are presumably different in REFLIONX and XILLVER) are under control and negligible for the quality of the available data.

The case of MCG-6-30-15 is a bit different. The spectrum of the source is more complicated and there are more components, which makes the comparison among different models not as direct as in the case of GRS 1915+105. For every relativistic reflection model, we show both the fit with the disc emissivity profile modelled by a simple power law and by a broken power law. For example, when we use RELCONV \times XILLVER the quality of the two fits is quite similar ($\Delta \chi^2 = 15$), while for RELXILL there is more difference ($\Delta \chi^2 = 57$). In general, the choice of the emissivity profile is thought to

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Table 5. MCG-6-30-15 – Summary of the best-fitting values for the models RELXILL (s) and RELXILL (b). The reported uncertainties correspond to the 90 per cent confidence level for one relevant parameter ($\Delta \chi^2 = 2.71$). ξ, ξ', ξ_1 , and ξ_2 in units of erg cm s⁻¹. See the text for the details.

Model	RELXILL (s)				RELXILL (b)			
Flux state	1	2	3	4	1	2	3	4
TBABS $N_{\rm H}/10^{22}~{\rm cm}^{-2}$	0.039*				0.039*			
$\begin{array}{c} \mathrm{WARMABS_1} \\ N_{\mathrm{HI}}/10^{22}~\mathrm{cm^{-2}} \\ \log \xi_1 \end{array}$	$0.67^{+0.10}_{-0.31} \\ 1.842^{+0.050}_{-0.011}$	$1.06_{-0.07}^{+0.07} 1.90_{-0.03}^{+0.03}$	$1.03^{+0.06}_{-0.05} \\ 1.912^{+0.019}_{-0.021}$	$0.65_{-0.06}^{+0.06} \\ 1.77_{-0.04}^{+0.03}$	$0.49^{+0.29}_{-0.12}$ $1.844^{+0.086}_{-0.017}$	$1.02_{-0.08}^{+0.06}$ $1.92_{-0.04}^{+0.04}$	$0.95_{-0.07}^{+0.05} 1.92_{-0.03}^{+0.03}$	$0.58^{+0.05}_{-0.06} \\ 1.77^{+0.04}_{-0.05}$
$\begin{array}{l} {\rm WARMABS_2} \\ N_{\rm H2}/10^{22}~{\rm cm}^{-2} \\ {\rm log}\xi_2 \end{array}$	$0.49^{+0.30}_{-0.11}$ $1.85^{+0.11}_{-0.03}$	0.01* 2.00*	$0.48^{+0.19}_{-0.19} \\ 3.22^{+0.07}_{-0.11}$	$0.32^{+0.06}_{-0.07} \\ 2.50^{+0.11}_{-0.11}$	$0.63_{-0.15}^{+0.09} \\ 1.88_{-0.05}^{+0.06}$	0.01* 2.00*	$0.59^{+0.24}_{-0.17}$ $3.26^{+0.06}_{-0.08}$	$0.32_{-0.08}^{+0.07} \\ 2.50_{-0.12}^{+0.11}$
DUSTYABS $log (N_{Fe}/10^{21} cm^{-2})$	$17.428^{+0.022}_{-0.039}$				$17.43^{+0.03}_{-0.04}$			
CUTOFFPL Γ $E_{\text{cut}} \text{ [keV]}$ $N_{\text{CUTOFFPL}} (10^{-3})$	$1.981^{+0.014}_{-0.014} \\ 340^{+157}_{-116} \\ 8.9^{+0.4}_{-0.5}$	$1.997^{+0.012}_{-0.013}$ 183^{+59}_{-41} $13.3^{+0.6}_{-0.6}$	$2.035_{-0.013}^{+0.011}$ 158_{-39}^{+50} $18.5_{-0.7}^{+0.7}$	$2.047^{+0.016}_{-0.011} 212^{+125}_{-49} 26.1^{+1.5}_{-1.3}$	$1.950^{+0.018}_{-0.015} 293^{+134}_{-75} 7.9^{+0.6}_{-1.0}$	$1.969^{+0.011}_{-0.020}$ 175^{+44}_{-35} $11.6^{+1.2}_{-1.6}$	$1.997^{+0.016}_{-0.023}$ 162^{+37}_{-32} $13.6^{+2.2}_{-2.7}$	$1.999^{+0.023}_{-0.013}$ 199^{+65}_{-43} 18^{+4}_{-3}
RELXILL qin qout	$3.01_{-0.15}^{+0.17}$ $= q_{\rm in}$	$3.03_{-0.17}^{+0.17}$ $= q_{\rm in}$	$3.26_{-0.23}^{+0.25}$ $= q_{\rm in}$	$3.6_{-0.4}^{+0.3} = q_{\text{in}}$	$6.1_{-2.5}^{+(P)}$ $2.78_{-0.15}^{+0.15}$ $3.3_{-0.9}^{+3.6}$	$4.6_{-1.0}^{+2.4}$ $2.4_{-0.8}^{+0.4}$ 7_{-3}^{+10}	$6.4_{-1.2}^{+1.7}$ $2.7_{-0.3}^{+0.3}$ $4.4_{-1.1}^{+2.0}$	$6.8_{-1.0}^{+1.4}$ $2.6_{-0.5}^{+0.4}$ $4.9+2.5$
$R_{ m br}$ [M] i [deg] a_* z					$3.3^{+3.6}_{-0.9}$ 7^{+10}_{-3} $4.4^{+2.0}_{-1.1}$ $4.8^{+2.5}_{-1.2}$ $28.7^{+2.1}_{-1.0}$ $0.962^{+0.019}_{-0.017}$ 0.007749^*			
$\log \xi$ A_{Fe}	$2.91^{+0.09}_{-0.09}$	$2.91^{+0.10}_{-0.08}$ 3.4	$3.00^{+0.03}_{-0.19}$ +0.5 -0.5	$3.01^{+0.04}_{-0.14}$	$3.00^{+0.03}_{-0.10}$	$3.01^{+0.03}_{-0.16}$ 2.9	$3.07^{+0.06}_{-0.04}$ $^{+0.3}_{-0.3}$	$3.13^{+0.08}_{-0.05}$
$N_{\text{RELXILL}} (10^{-3})$ XILLVER	$0.048^{+0.004}_{-0.004}$	$0.055^{+0.004}_{-0.004}$	$0.079^{+0.007}_{-0.006}$	$0.096^{+0.010}_{-0.013}$	$0.057^{+0.010}_{-0.010}$	$0.069^{+0.012}_{-0.010}$	$0.114^{+0.020}_{-0.008}$	$0.16^{+0.03}_{-0.03}$
$\log \xi'$ $N'_{\text{XILLVER}} (10^{-3})$	0^{\star} $0.065^{+0.009}_{-0.005}$				0^{\star} $0.046^{+0.011}_{-0.010}$			
ZGAUSS E_{line} [keV]	$0.8044^{+0.0023}_{-0.0017}$				$0.806^{+0.003}_{-0.003}$			
ZGAUSS E_{line} [keV]	$1.224^{+0.010}_{-0.009}$				$1.222^{+0.012}_{-0.015}$			
χ^2 /dof	3081.74/2691 = 1.14520				3024.46/2683 = 1.12727			

play an important role and can affect the estimate of the model parameters; see for example, Liu et al. (2019) and Zhang et al. (2019). However, if we see the best-fitting tables, and in particular Fig. 4, we can realize that here the choice of the relativistic reflection model is more important than the choice between simple and broken power law. Note that using different relativistic reflection models may affect also the choice of the total model. In particular, when we employ RELCONV \times REFLIONX we do not need ZGAUSS to describe the emission line at 0.8 keV (see Table 3). When we use RELXILL, we do not need the second warm absorber in the medium flux state ($N_{\rm H_2}$ is frozen to the minimum value 0.01 in Table 5).

The differences between the fits of RELCONV × REFLIONX and RELCONV × XILLVER arise from the different reflection model, namely REFLIONX or XILLVER. Note that the differences between REFLIONX are XILLVER are larger for intermediate levels of ionization, say $2 < \log \xi < 3$, which is the case of the accretion disc of MCG-6-30-15, while for lower or higher values of $\log \xi$ the differences in the predicted spectra are smaller (García et al. 2013). We see that

the values of the black hole spin parameter a_* and the inclination angle of the disc i inferred with REFLIONX are slightly lower than the values found with XILLVER. Employing a simple power-law profile for the disc emission, the ionization of the accretion disc decreases as the flux of the source increases with REFLIONX, while we see a ionization parameter that increases as the flux of the source increases with XILLVER. In the case of a broken power law, both models require a relatively constant ionization parameter. While all these trends are possible, they require different coronal geometries.

From the comparison of the fits of RELCONV \times XILLVER and RELXILL we can evaluate the impact of the proper calculations of the angle dependence of the reflection spectrum at the emission point. The angle-resolved model was introduced in García et al. (2014), where the authors showed that angle-averaged models can overestimate the iron abundance by up to a factor of 2. Moreover, in the case of a steep emissivity and high ionization, a high spin will be underestimated if viewed at low inclinations ($\theta < 50^{\circ}$) and modelled with angle-averaged models. Lohfink et al. (2016) point out this issue

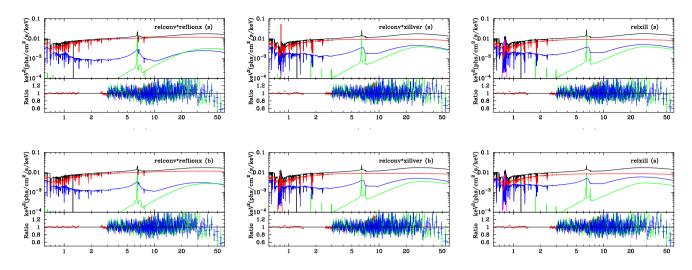


Figure 8. MCG-6-30-15 – Best-fitting models of the low flux state (top quadrants) and data to best-fitting model ratios (bottom quadrants) for the models RELCONV × REFLIONX (left-hand panels), RELCONV × XILLVER (central panels), and RELXILL (right-hand panels), employing an emissivity profile described by a simple power law (top panels) and a broken power law (bottom panels). In every panel, the total spectrum is in black, the power-law component from the corona is in red, the relativistic reflection component from the disc is in blue, and the non-relativistic reflection component from cold material is in green.

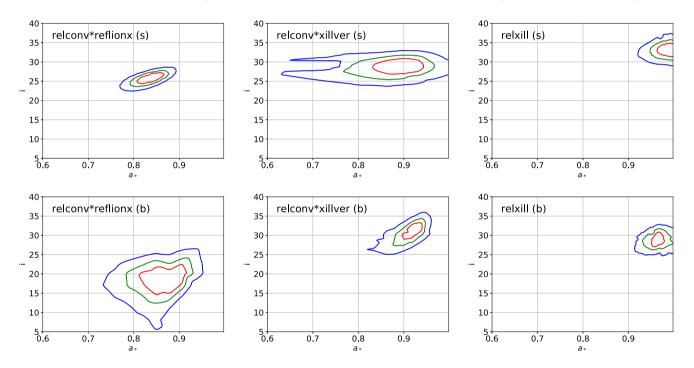


Figure 9. MCG-6-30-15 – Constraints on the black hole spin parameter a_* and the inclination angle of the disc i for the models RELCONV × REFLIONX (left-hand panels), RELCONV × XILLVER (central panels), and RELXILL (right-hand panels), employing an emissivity profile described by a simple power law (top panels) and a broken power law (bottom panels). The red, green, and blue curves correspond, respectively, to the 68 per cent, 90 per cent, and 99 per cent confidence level limits for two relevant parameters.

about angle-averaged and angle-resolved models in the discussion of different spin measurements of Fairall 9.

Lastly, we want to estimate the impact of the choice of the reflection model in the case of future observations of a source like GRS 1915+105, as in our analysis we do not see an appreciable difference among the three models employed. To address this point, we simulate a 20 ks observation with the X-IFU instrument on board of *Athena* (Nandra et al. 2013). Barret & Cappi (2019) conducted comprehensive simulations with the model RELXILL and found that the instrument X-IFU is capable to accurately recover the

input parameters. The input model for our simulation is TBABS \times (CUTOFFPL + RELXILL) and the input parameters are the best-fitting values in Table 2 found with RELXILL. The observation is generated with the fakeit command in XSPEC and then analysed with the three models already used in Section 3. The results of our fits are shown in Table 6. RELCONV \times XILLVER and RELXILL provide very similar results, and the fits are good. We can thus conclude that the difference between the best-fitting parameters of GRS 1915+105 using the angle-averaged and angle-resolved models will remain negligible even for Athena. However, the choice of the reflection

Table 6. Summary of the best-fitting values of the 20 ks simulated observation with X-IFU/Athena fitted with the models RELCONV × REFLIONX, RELCONV × XILLVER, and RELXILL. The reported uncertainties correspond to the 90 per cent confidence level for one relevant parameter ($\Delta \chi^2 = 2.71$). ξ in units of erg cm s⁻¹. In REFLIONX, the fitting parameter is ξ , not $\log \xi$ as in XILLVER and RELXILL, but it is converted into $\log \xi$ in the table in order to facilitate the comparison with the other models. See the text for the details.

Model	RELCONV × REFLIONX	RELCONV × XILLVER	RELXILL		
TBABS					
$N_{\rm H}(10^{22}~{\rm cm}^{-2})$	$5.243^{+0.009}_{-0.011}$	$5.1936^{+0.0011}_{-0.0011}$	$5.1942^{+0.005}_{-0.0013}$		
CUTOFFPL					
Γ	$2.289^{+0.005}_{-0.006}$	$2.1973^{+0.0007}_{-0.0015}$	$2.1974^{+0.006}_{-0.0015}$		
$E_{\rm cut}~({\rm keV})$	>490	$68.3_{-0.9}^{+0.7}$	$68.8^{+1.0}_{-2.0}$		
$N_{ m cutoffpl}$	$4.036^{+0.014}_{-0.027}$	$3.860^{+0.05}_{-0.018}$	$3.821^{+0.028}_{-0.016}$		
$q_{ m in}$	$8.63^{+0.07}_{-0.06}$	>9.9	$9.925^{+0.05}_{-0.027}$		
$q_{ m out}$	$0.0^{+0.016}$	$0.0^{+0.05}$	$0.0^{+0.13}$		
$R_{\rm br}$	$7.47^{+0.09}_{-0.10}$	$6.334^{+0.03}_{-0.019}$	$6.310^{+0.019}_{-0.04}$		
a_*	$0.998_{-0.00005}$	$0.9910^{+0.0002}_{-0.0009}$	$0.9910^{+0.0003}_{-0.0006}$		
i (deg)	$74.56^{+0.25}_{-0.19}$	$73.87^{+0.08}_{-0.06}$	$73.85^{+0.08}_{-0.06}$		
$\log \xi$	$2.760^{+0.006}_{-0.003}$	$2.763^{+0.005}_{-0.005}$	$2.769^{+0.004}_{-0.010}$		
A_{Fe}	$0.601^{+0.007}_{-0.016}$	$0.579^{+0.004}_{-0.005}$	$0.575^{+0.007}_{-0.004}$		
$N_{\rm reflionx}~(10^{-4})$	$2.15^{+0.10}_{-0.11}$	_	_		
N_{xiller}	_	$0.1533^{+0.0015}_{-0.004}$	_		
$N_{\rm relxill} \ (10^{-2})$	_	_	$2.106^{+0.013}_{-0.025}$		
χ^2/ν	13729/7888 = 1.741	7960.6/7888 = 1.009	7896.06/7888 = 1.001		

model will be somewhat important. With RELCONV × REFLIONX, the fit is not good, as $\chi^2/\nu=1.7$, which means the differences in the calculations of REFLIONX and XILLVER can be clearly detected with *Athena*. This should not be surprising, as even here we have $2 < \log \xi < 3$, which is the ionization range for which the differences in the predicted spectra of REFLIONX are XILLVER are larger (García et al. 2013). Despite that, it is quite remarkable that the measurements of most parameters of the system are consistent. A clear discrepancy is only found in the estimate of $E_{\rm cut}$. We have some minor discrepancy even in the estimates of a_* and i, but the differences are small and we may expect that systematic uncertainties in the description of the accretion disc and the corona are large enough to make the measurements of a_* and i from the three models still consistent.

In conclusion, in this work we have shown that the choice of the relativistic reflection model may have an impact on the estimate of some properties of an accreting black hole already with the available X-ray data. We have employed the most commonly used reflection models among the X-ray astronomy community, namely REFLIONX, XILLVER, and the angle-resolved model RELXILL. Because of the complexity of these systems, it is not straightforward to generalize our results for generic sources and X-ray missions. The particular choice of the source, of its spectral state, of the total XSPEC model, instrumental effects, etc. can combine together in a quite complicated way. In our analysis of the Suzaku observation of GRS 1915+105, we have not found discrepancies in the analysis with different models and between angle-averaged and angle resolved models. Simulating a future observation of GRS 1915+105 with Athena, we have found some minor differences between REFLIONX and XILLVER/RELXILL. In the case of the simultaneous XMM-Newton and NuSTAR observations of MCG-6-30-15, we have seen the difference between angle-averaged and angle-resolved models, which shows the importance of taking the exact emission angle into account as already noted in García et al. (2014).

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DATA AVAILABILITY

The *Suzaku*, *XMM-Newton*, and *NuSTAR* raw data analysed in this work are available to download at the HEASARC Data Archive website.²

REFERENCES

Abdikamalov A. B., Ayzenberg D., Bambi C., Dauser T., García J. A., Nampalliwar S., Tripathi A., Zhou M., 2020, ApJ, 899, 80

Arnaud K. A., 1996, ASP Conf. Ser. Vol. 101, Astronomical Data Analysis Software and Systems V. Astron. Soc. Pac., San Francisco, p. 17

Ballantyne D. R., Turner N. J., Blaes O. M., 2004, ApJ, 603, 436

Bambi C., 2017, Rev. Mod. Phys., 89, 025001

Bambi C., 2018, Ann. Phys., 530, 1700430

Bambi C., Cárdenas-Avendaño A., Dauser T., García J. A., Nampalliwar S., 2017, ApJ, 842, 76

Barret D., Cappi M., 2019, A&A, 628, A5

Belloni T., Klein-Wolt M., Méndez M., van der Klis M., van Paradijs J., 2000, A&A, 355, 271

²https://heasarc.gsfc.nasa.gov/docs/archive.html

Blum J. L., Miller J. M., Fabian A. C., Miller M. C., Homan J., van der Klis M., Cackett E. M., Reis R. C., 2009, ApJ, 706, 60

Bonson K., Gallo L. C., 2016, Astron. Nachr., 337, 423

Brenneman L. W., Reynolds C. S., 2006, ApJ, 652, 1028

Cárdenas-Avendaño A., Zhou M., Bambi C., 2020, Phys. Rev. D, 101, 123014

Castro-Tirado A. J., Brandt S., Lund N., 1992, IAU Circ., No. 5590, 2

Choudhury K., García J. A., Steiner J. F., Bambi C., 2017, ApJ, 851, 57

Cunningham C. T., 1975, ApJ, 202, 788

Dauser T., Wilms J., Reynolds C. S., Brenneman L. W., 2010, MNRAS, 409,

1534
Dauser T., Garcia J., Wilms J., Böck M., Brenneman L. W., Falanga M., Fukumura K., Reynolds C. S., 2013, MNRAS, 430, 1694

Dickey J. M., Lockman F. J., 1990, ARA&A, 28, 215

El-Batal A. M. et al., 2016, ApJ, 826, L12

Fabian A. C., Rees M. J., Stella L., White N. E., 1989, MNRAS, 238, 729

Fabian A. C. et al., 2002, MNRAS, 335, L1

Fabian A. C. et al., 2020, MNRAS, 493, 5389

Galeev A. A., Rosner R., Vaiana G. S., 1979, ApJ, 229, 318

García J., Kallman T. R., 2010, ApJ, 718, 695

García J., Dauser T., Reynolds C. S., Kallman T. R., McClintock J. E., Wilms J., Eikmann W., 2013, ApJ, 768, 146

García J. et al., 2014, ApJ, 782, 76

García J. A., Fabian A. C., Kallman T. R., Dauser T., Parker M. L., McClintock J. E., Steiner J. F., Wilms J., 2016, MNRAS, 462, 751

García J. A. et al., 2018, ApJ, 864, 25

George I. M., Fabian A. C., 1991, MNRAS, 249, 352

Guainazzi M. et al., 1999, A&A, 341, L27

Ingram A., Mastroserio G., Dauser T., Hovenkam P., van der Klis M., García J. A., 2019, MNRAS, 488, 324

Iwasawa K. et al., 1996, MNRAS, 282, 1038

Jiang J., Fabian A. C., Wang J., Walton D. J., García J. A., Parker M. L., Steiner J. F., Tomsick J. A., 2019a, MNRAS, 484, 1972

Jiang J. et al., 2019b, MNRAS, 489, 3436

Kammoun E. S., Nardini E., Risaliti G., 2018, A&A, 614, A44

Kammoun E. S. et al., 2019, MNRAS, 485, 239

Laor A., 1991, ApJ, 376, 90

Lee J. C., Ogle P. M., Canizares C. R., Marshall H. L., Schulz N. S., Morales R., Fabian A. C., Iwasawa K., 2001, ApJ, 554, L13

Leighly K. M., Mushotzky R. F., Nandra K., Forster K., 1997, ApJ, 489, L25
 Liu H., Abdikamalov A. B., Ayzenberg D., Bambi C., Dauser T., García J.
 A., Nampalliwar S., 2019, Phys. Rev. D, 99, 123007

Lohfink A. M. et al., 2016, ApJ, 821, 11

Marinucci A. et al., 2014, ApJ, 787, 83

McClintock J. E., Shafee R., Narayan R., Remillard R. A., Davis S. W., Li L.-X., 2006, ApJ, 652, 518

Miller J. M. et al., 2013, ApJ, 775, L45

Miniutti G., Fabian A. C., Goyder R., Lasenby A. N., 2003, MNRAS, 344, 122

Miniutti G. et al., 2007, PASJ, 59, 315

Mirabel I. F., Rodríguez L. F., 1999, ARA&A, 37, 409

Nandra K., O'Neill P. M., George I. M., Reeves J. N., 2007, MNRAS, 382, 194

Nandra K. et al., 2013, preprint(arXiv:1306.2307)

Niedźwiecki A., Zdziarski A. A., 2018, MNRAS, 477, 4269

Novikov I. D., Thorne K. S., 1973, in DeWitt C., DeWitt B. S., eds, Black Holes (les Astres Occlus), Gordon & Breach, New York (New York, US), p. 343

Page D. N., Thorne K. S., 1974, ApJ, 191, 499

Reid M. J., McClintock J. E., Steiner J. F., Steeghs D., Remillard R. A., Dhawan V., Narayan R., 2014, ApJ, 796, 2

Reynolds C. S., 2014, Space Sci. Rev., 183, 277

Reynolds C. S., Fabian A. C., 2008, ApJ, 675, 1048

Riaz S., Ayzenberg D., Bambi C., Nampalliwar S., 2020a, MNRAS, 491,

Riaz S., Ayzenberg D., Bambi C., Nampalliwar S., 2020b, ApJ, 895, 61

Riaz S., Szanecki M., Niedzwiecki A., Ayzenberg D., Bambi C., 2020c, preprint(arXiv:2006.15838)

Ross R. R., Fabian A. C., 2005, MNRAS, 358, 211

Różańska A., Dumont A.-M., Czerny M., Collin S., 2002, MNRAS, 332, 799

Shakura N. I., Sunyaev R. A., 1973, A&A, 500, 33

Shreeram S., Ingram A., 2020, MNRAS, 492, 405

Speith R., Riffert H., Ruder H., 1995, Comput. Phys. Commun., 88, 109

Sunyaev R. A., Truemper J., 1979, Nature, 279, 506

Svoboda J., Dovčiak M., Goosmann R. W., Jethwa P., Karas V., Miniutti G., Guainazzi M., 2012, A&A, 545, A106

Tanaka Y. et al., 1995, Nature, 375, 659

Taylor C., Reynolds C. S., 2018, ApJ, 855, 120

Tomsick J. A. et al., 2018, ApJ, 855, 3

Tripathi A. et al., 2019, ApJ, 875, 56

Walton D. J., Nardini E., Fabian A. C., Gallo L. C., Reis R. C., 2013, MNRAS, 428, 2901

Wilkins D. R., Fabian A. C., 2011, MNRAS, 414, 1269

Wilkins D. R., Fabian A. C., 2012, MNRAS, 424, 1284

Wilkins D. R., Gallo L. C., 2015a, MNRAS, 448, 703

Wilkins D. R., Gallo L. C., 2015b, MNRAS, 449, 129

Wilkins D. R., Reynolds C. S., Fabian A. C., 2020, MNRAS, 493, 5532

Wilms J., Allen A., McCray R., 2000, ApJ, 542, 914

Zhang Y., Abdikamalov A. B., Ayzenberg D., Bambi C., Nampalliwar S., 2019, ApJ, 884, 147

Zhou M., Ayzenberg D., Bambi C., Nampalliwar S., 2020, Phys. Rev. D, 101, 043010

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