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3D mapping of the Crab Nebula with SITELLE - I. Deconvolution and kinematic reconstruction

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ABSTRACT

We present a hyperspectral cube of the Crab Nebula obtained with the imaging Fourier transform spectrometer SITELLE on the Canada–France–Hawaii telescope. We describe our techniques used to deconvolve the 310 000 individual spectra (R = 9600) containing Hα, [N II] λλ6548, 6583, and [S II] λλ6716, 6731 emission lines and create a detailed 3D reconstruction of the supernova (SN) remnant (SNR) assuming uniform global expansion. We find that the general boundaries of the 3D volume occupied by the Crab are not strictly ellipsoidal as commonly assumed, and instead appear to follow a 'heart-shaped' distribution that is symmetrical about the plane of the pulsar wind torus. Conspicuous restrictions in the bulk distribution of gas consistent with constrained expansion coincide with positions of the dark bays and east-west band of He-rich filaments, which may be associated with interaction with a pre-existing circumstellar disc. The distribution of filaments follows an intricate honeycomblike arrangement with straight and rounded boundaries at large and small scales that are anticorrelated with distance from the centre of expansion. The distribution is not unlike the large-scale rings observed in SNRs 3C 58 and Cassiopeia A, where it has been attributed to turbulent mixing processes that encouraged outwardly expanding plumes of radioactive ⁵⁶Ni-rich ejecta. These characteristics reflect critical details of the original SN of 1054 CE and its progenitor star, and may favour a low-energy explosion of an iron-core progenitor. We demonstrate that our main findings are robust despite regions of non-homologous expansion driven by acceleration of material by the pulsar wind nebula.

Key words: instrumentation: interferometers - methods: data analysis - techniques: imaging spectroscopy - supernovae: general – ISM: supernova remnants.

1 INTRODUCTION

Young supernova remnants (SNR, <3000 yr) in the Milky Way and Magellanic Clouds provide rare opportunities to probe the explosion mechanisms and progenitor systems of SNe with observations capable of producing 3D reconstructions. Their proximity (from a few to less than a hundred kpc) and high expansion velocity (a few thousand km s⁻¹) allow not only to disentangle the different Doppler components with relatively modest spectral resolutions, but also to determine the tangential velocity of their filaments using images obtained decades apart (or sometimes a few years apart using the Hubble Space Telescope; HST). Asymmetries in chemical or ionization structure, expansion velocity or density can then be probed with much greater precision than what is possible for unresolved extragalactic objects (Milisavljevic & Fesen 2017). Such reconstructions, made for SNRs including Cassiopeia A (Cas A, DeLaney et al. 2010; Milisavljevic & Fesen 2013; Alarie, Bilodeau & Drissen 2014; Milisavljevic & Fesen 2015; Grefenstette et al. 2017), 1E 0102.2-7219 (Vogt & Dopita 2010; Vogt et al. 2018), and N132D

(Law et al. 2020), are critical for establishing strong empirical links between SNe and SNRs that can be compared to state-of-the-art simulations evolving from core collapse to remnant (Orlando et al. 2015, 2016, 2020; Ono et al. 2020).

Among the most studied yet still enigmatic remnants deserving of 3D reconstruction is the Crab Nebula (SN 1054, NGC 1952). Despite decades of investigation, the progenitor star's initial mass and the properties governing the SN explosion remain uncertain (Davidson & Fesen 1985; Hester 2008). The total mass of its ejecta (2–5 M_{\odot} , Fesen, Shull & Hurford 1997) is much less than the plausible mass of the progenitor (8–13 M_{\odot} , Nomoto 1987), and although SN 1054 was more luminous than a normal Type II SN (-18 mag versus -15.6mag, Clark & Stephenson 1977), its kinetic energy (\approx 7 × 10⁴⁹ erg) is surprisingly low compared to the canonical $\sim 10^{51}$ erg. The standard explanation is that most of the mass and 90 per cent of the kinetic energy of SN 1054 reside in an invisible freely expanding envelope of cold and neutral ejecta travelling \sim 5000 km s⁻¹ far outside the Crab (Chevalier 1977). However, this theorized outer envelope has never been robustly detected to remarkably low upper limits (Fesen et al. 1997; Lundqvist & Tziamtzis 2012). A weak C IV λ1550 absorption feature observed in a far-ultraviolet HST spectrum of the Crab pulsar is suggestive of an ionized outer envelope (Sollerman et al. 2000; Downloaded from https://academic.oup.com/mnras/article/502/2/1864/6103938 by guest on 24 April 2024

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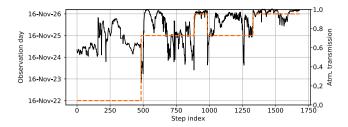


Figure 1. Atmospheric transmission as a function of the step index. The date when each part of the cube was obtained is shown as an orange dotted line.

Hester 2008), but only extending out to \sim 2500 km s⁻¹ and tracing a relatively small amount of material (\sim 0.3 M $_{\odot}$).

Models and observations generally support a low-energy SN origin potentially associated with an O-Ne-Mg core that collapses and explodes as electron-capture supernova (ECSN, Nomoto et al. 1982; Hillebrandt 1982; Kitaura, Janka & Hillebrandt 2006). However, such explosions are generally faint $(M_V > -15 \text{ mag})$ and thus inconsistent with the brightness of SN 1054 estimated from historical records. Fesen et al. (1997) and Chugai & Utrobin (2000) suggested that SN 1054 was a low-energy SN with additional luminosity provided by circumstellar interaction. Smith (2013) supports this view and identified potential Crab-like analogues in many recent Type IIn events. Tominaga, Blinnikov & Nomoto (2013) found that the high peak luminosity could instead be related to the large extent of the progenitor star and not necessarily associated with strong circumstellar interaction. Gessner & Janka (2018) questioned the appropriateness of an ECSN origin for the Crab, as their simulations found that hydrodynamic neutron star kicks associated with O-Ne-Mg core progenitors are much below the \sim 160 km s⁻¹ measured for the Crab pulsar (Kaplan et al. 2008). Yang & Chevalier (2015) found the Crab's overall properties to be consistent with expectations from a pulsar wind nebula evolving inside a freely expanding low-energy SN.

There have been multiple attempts at mapping the 3D structure of the Crab. However, the large angular size of the Crab (~6 arcmin) and complexity of its numerous overlapping filamentary structures presents many challenges. Lawrence et al. (1995) created 3D spatial models of the line-emitting [O III] $\lambda\lambda4959$, 5007 gas in the Crab with Fabry-Perot imaging spectroscopy. Čadež, Carramiñana & Vidrih (2004) created a 3D representation using long-slit spectroscopy at low- and high-resolution configurations rotated at a series of position angles. Charlebois et al. (2010) used the imaging Fourier transform spectrometer (FTS) SpIOMM to create a 3D view of the Crab and emission-line ratios of the filaments. Black & Fesen (2015) mapped the Crab's northern ejecta jet with moderate-resolution [OIII] line emission spectra. Generally, these investigations have highlighted the north-south bipolar asymmetry in the abundance, geometry, and velocity distribution of the bright filaments. A band of heliumrich material runs in the east-west direction (Uomoto & MacAlpine 1987), which is associated with pinched velocities (MacAlpine et al. 1989), potentially associated with constrained expansion due to interaction with a circumstellar disc left behind from pre-SN mass loss (Fesen, Martin & Shull 1992). To date, there does not exist a complete mapping of individual emission lines throughout the remnant sensitive to faint emission on fine scales.

In this paper, we introduce a hyperspectral cube of the Crab obtained with the imaging FTS SITELLE (Drissen et al. 2019). SITELLE has a field of view of $11 \, \text{arcmin} \times 11 \, \text{arcmin}$, high sensitivity down to $350 \, \text{nm}$, and is especially powerful for observing emission-line sources above a low continuum background (Bennett 2000; Maillard et al. 2013). Together, these characteristics make

SITELLE uniquely suited to meet the challenges of observing the Crab.

In this paper, we describe preliminary SITELLE observations and associated analysis of the Crab obtained in a passband covering 647–685 nm with spectral resolution 9600. These data are the highest resolution ever obtained with SITELLE on an astrophysical target and a spectacular opportunity to demonstrate the full potential of this new technology. We also describe the techniques used to deconvolve the spectra and produce a 3D reconstruction of the SNR. A more detailed analysis of these data in combination with planned complementary observations at other wavelengths will follow in a subsequent paper.

2 DATA

2.1 SITELLE data

The data were obtained using the SITELLE instrument mounted to Canada–France–Hawaii telescope (CFHT) during the course of an engineering run spanning the nights of 2016 November 22, 25, and 26. SITELLE combines a 2D imaging detector with a Michelson interferometer. Two complementary interferometric data cubes are obtained by recording images, on two $2k \times 2k$ CCD detectors, at different positions of the moving mirror inside the Michelson. Fourier transforms are then used to convert these cubes into a single spectral data cube. Spectral resolution is set by the maximum path difference between the two arms of the interferometer, reached by displacing its moving mirror through a series of steps of several hundred nanometers each. The spectral range is selected by using interference filters; SITELLE covers the 350-850 nm range with a series of eight filters, tailored to specific needs. Spatial sampling is $0.32\,\mathrm{arcsec\,pixel^{-1}}$, leading to a field of view of 11 arcmin \times 11 arcmin and over 4 million spectra.

Our raw data for the Crab consist in an interferometric cube of 1682 steps (with a step size of 2843 nm) with an exposure time of 5.3 s per step (followed by an overhead of 3.8 s for CCD readout and concurrent mirror movement and stabilization), leading to an integration time of 2.48 h over a 4.25 h total data acquisition time. The median seeing, measured on the image obtained from the combination of all detrended and aligned interferometric images, was 1.17 ± 0.04 arcsec. This engineering data were aimed at testing SITELLE's high-resolution capabilities with a target resolution of $10\,000$ in the SN3 filter (647–685 nm passband: H α , [N II] $\lambda\lambda$ 6548,6584, and [S II] $\lambda\lambda$ 6717,6731). It was obtained under extremely varying atmospheric conditions (see Fig. 1). Some data obtained on November 25 (around steps 900–1000) were deemed to be of too poor quality and were therefore taken again at the end of the following night.

We thus have been able to test the stability of the instrument in terms of absolute positioning of the moving mirror and the impact of the observed modulation efficiency loss at high optical path difference (OPD, Baril et al. 2016).

These data were reduced with the pipeline reduction software ORBS (Martin, Drissen & Joncas 2012; Martin 2015) without any special treatment with respect to the rest of the data obtained during the same run. As an example of the quality of the reduction, we present in Fig. 2 the raw interferogram of the pulsar, obtained with an aperture of 1.6 arcsec radius, before and after the correction for the sky transmission. Any error on this correction on the interferograms can significantly impact the quality of the calculated spectrum and especially its instrumental line shape (ILS, Martin & Drissen 2016).

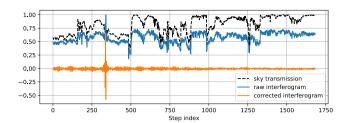


Figure 2. Interferogram of the M1 pulsar before and after the correction for the sky transmission and the varying background (respectively, blue and orange lines). Atmospheric transmission is reported in dotted black. The large oscillation seen at step \sim 325 corresponds to the zero path difference of the interferometer, and is characteristic of a continuum source, while the low-amplitude beating patterns observed along the interferogram are caused by the multiple emission lines of the nebula included within the 1.6 arcsec radius of the aperture.

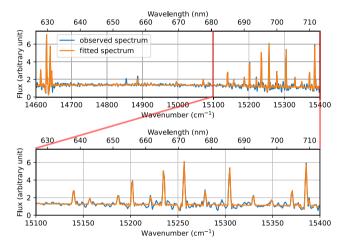
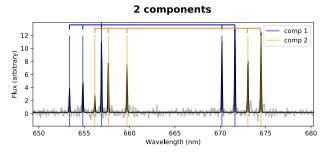


Figure 3. Sky spectrum used to measure the effective resolution ($R = 8870 \pm 20$, blue line) along with the fitted model (orange line). The bottom panel shows an enlarged portion of the top panel around H α (15237 cm⁻¹).

We have measured the effective resolution by fitting a model on a spectrum of the sky (dominated by OH lines in this spectral range) integrated over a small region of the cube (a circular aperture with a 100 pixels radius) with the analysis software ORCS (Martin, Drissen & Joneas 2015). In order to take into account the modulation efficiency loss at high OPD, which may broaden the observed ILS, we have modellized the ILS as the convolution of a sinc (the natural ILS of an FTS) with a Gaussian (resulting from the broadening of the observed sky lines by the modulation efficiency loss) and used the sincgauss model described in Martin, Prunet & Drissen (2016, see fig. 3). The measured full width at half-maximum (FWHM) of the sky lines was $1.718 \pm 0.05 \,\mathrm{cm}^{-1}$ which leads to a resolving power $R = 8870 \pm 20$ @ H α (Martin et al. 2016). From the parameters of the cube, the theoretical resolution which we should have been measured at the same position is 9640. We can conclude that the effect of the modulation efficiency loss at high OPD is at most of the order of 10 per cent at a resolution of 9640.

3 MAPPING THE CRAB NEBULA IN $H\alpha$, [N II], AND [S II]

The Crab Nebula is long known to display a very complex filamentary structure that remains interpreted as the result of Rayleigh-Taylor



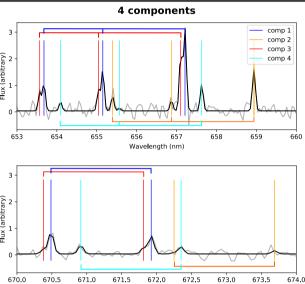


Figure 4. Two examples of spectra containing multiple components and their fit. Two components panel: a spectrum with two non-overlapping components, obtained near the centre of the nebula. Four components panel: a spectrum with four overlapping components obtained in a complex filamentary region of the nebula. The plot is split in two parts to help distinguish all four components. Note that if only four of the components have been found by the algorithm, additional dim components may exist. This example demonstrates at the same time the quality and the limitations of our algorithm.

(RT) instabilities at the interface of the synchrotron nebula and the thermal ejecta (Hester et al. 1996; Hester 2008). This filamentary structure, ionized by the shock of the expanding synchrotron nebula, shows's particularly strong emission in H α , [N II], and [S II]. Multiple components of filamentary emission are visible along any line of sight with velocities ranging from -1500 to $1500 \, \mathrm{km \, s^{-1}}$ (see Fig. 4) that must be separated in order to compute the correct mapping of the flux and velocity of the observed emission lines. The emission covers a circular surface of \sim 6 arcmin in diameter, which spans approximately one million of the four million spectra contained in the data cube.

Inspired by the algorithms developed by Čadež et al. (2004) and Charlebois et al. (2010) on similar data sets, we have written an algorithm to automate detection and fitting of overlapping emission components observed in the spectra. This algorithm analyses each spectrum individually in three steps (see Fig. 5):

- (i) evaluation of the probability, as a score, of having one component at a given velocity;
- (ii) enumeration of all the individual velocity components along the line of sight;

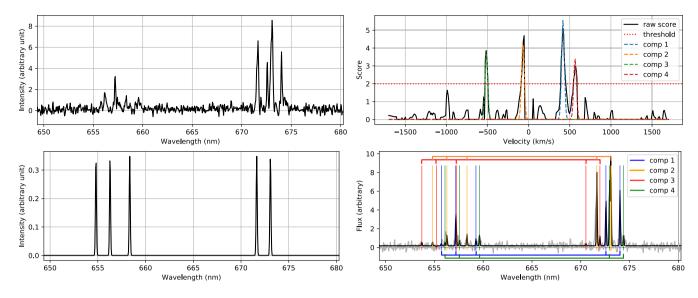


Figure 5. The fitting process. Top left: example of a raw spectrum extracted from a complex filamentary region of the nebula containing at least four components. Bottom left: example of a five emission-lines comb-like spectrum which would be convolved with the analysed spectrum. In fact, the spectrum is convolved with the individual lines of the comb. All lines of the comb have the same intensity. The apparent difference comes from the function sampling. Top right: mitigated correlation score obtained after the first step of the analysis (black) with the four fitted components detected at the second step. The detection threshold used for the enumeration of the brightest components of the score (see Section 3.2) is shown in dotted red. Bottom right: fit realized on the spectrum shown in the top left panel; the positions of the five fitted emission lines are shown for each of the four fitted components.

(iii) fit of the spectrum with a model combining all the velocity components at the same time.

3.1 Step 1: computation of the score

The first step is based on the convolution of the analysed spectrum $S(\lambda)$ with a comb-like spectrum $K(v, \lambda)$ made of a subset of the emitting lines of each component: H α , the [N II] doublet, and the [S II] doublet (see bottom left panel of Fig. 5). All lines of the comb have the same amplitude. The calculated score C(v) is simply:

$$C(v) = \int S(\lambda)K(v,\lambda)d\lambda. \tag{1}$$

C(v) is maximum when the position of the modelled emission lines of $K(v, \lambda)$ coincides with the position of the emission lines of the spectrum.

Ideally, if the explored velocity range is not too large and no line of the comb is matched with another emission line, each velocity component of the spectrum will produce one peak with an approximately Gaussian shape. The centroid of the peak gives the component velocity and its amplitude scales with the integral of the flux in the lines present in *K*.

However, the biggest challenge with this approach appears when the comb and the analysed spectrum contains multiple lines within the range of velocity scanned. For example, one line of the comb (e.g. $\text{H}\alpha$) may coincide with the position of a neighbouring line at a different velocity (e.g. [N II]). In this case, even with only one component along the line of sight, C(v) will show multiple peaks; the highest being the real one because it reflects the velocity at which the largest number of lines are coincident. With multiple components however, if one component is much brighter than the others, the secondary peaks in C(v) created by the brightest component may be even higher than the primary peak of the second components, in which case the correct enumeration of the components is compromised.

Fig. 6 reproduces this issue by showing a synthetic spectrum made of two velocity components, one being five times brighter than the

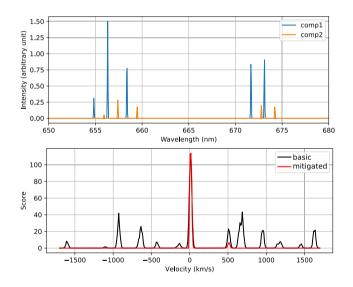


Figure 6. Top: two-components noiseless model spectrum. Bottom: basic and mitigated scores computed from the top-panel spectrum. The numerous lines appearing in the basic score (black line) do not reflect real components or noise. Instead, they correspond to velocities where some lines of the comb coincide with another emission line (e.g. where the $H\alpha$ line of the comb coincides, at a given velocity, with an [NII] line of the spectrum). Applying physical constraints when computing a mitigated score (in red) reduces these aliases, which permits the detection of dimmer velocity components. The addition of noise only contributes small amplitude peaks that are discarded (see top right panel of Fig. 5).

other. The comb used for the analysis contains five emission lines $(H\alpha, [NII], [SII])$ and is shown in the bottom left quadrant of Fig. 5.

Using equation (1) without any special treatment leads to a score C(v) with multiple false peaks (black line) where the peak related to the dimmest component cannot be retrieved.

We mitigate complicating factors with use of equation (1) by adding a number of physically based conditions that must be respected in order to get a non-zero value of C(v). One is to force the presence of all the lines by computing independent scores for each line and compute the product of their probability. Let $K_i(v, \lambda)$ be the kernel for the line $i, i \in \{H\alpha, [N II]\lambda 6548, [N II]\lambda 6548, [N II]\lambda 6583, [S II]\lambda 6716, [S II]\lambda 6731\}$. If we want all five lines to be present in order to have a non-zero score we would rewrite equation (1) as

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$$C_i(v) = \int S(\lambda)K_i(v,\lambda)d\lambda, \qquad (2)$$

$$C(v) = \Pi_i \ C_i(v). \tag{3}$$

However, all five lines are not always detectable. Sometimes only the [S II] or [N II] + H α lines are visible. Thus, we further separate these two groups and put additional physics-based conditions to finally write the mitigated version of the score:

$$C_{[N \text{ II}]} = \sqrt{C_{[N \text{ II}]\lambda6548} \times C_{[N \text{ II}]\lambda6583}},$$
 (4)

$$C_{[S II]} = \sqrt{C_{[S II]\lambda6716} \times C_{[S II]\lambda6731}},$$
 (5)

$$C(v) = C_{\text{H}\alpha} \times C_{[\text{N II}]} + C_{[\text{S II}]}; \tag{6}$$

with the following additional conditions that constrain the [S $\rm II$] and [N $\rm II$] line ratios to be realistic enough,

$$C_{[N \text{ II}]} = 0 \text{ if } C_{[N \text{ II}]\lambda6583} < C_{[N \text{ II}]\lambda6548},$$
 (7)

$$C_{[N \text{ II}]} = 0 \text{ if } C_{[N \text{ II}]\lambda6548} < 0.14 \times C_{[N \text{ II}]\lambda6584},$$
 (8)

$$C_{[S II]} = 0 \text{ if } C_{[S II]\lambda6716} < 0.14 \times C_{[S II]\lambda6731},$$
 (9)

$$C_{[S II]} = 0 \text{ if } C_{[S II]\lambda6731} < 0.14 \times C_{[S II]\lambda6716}.$$
 (10)

The value of 0.14 (\simeq 1/7) has been manually optimized to help reject obviously wrong scores while keeping lower SNR components. This value is necessarily kept lower than the theoretical ratios of [S II] lines (between 0.5 and 1.5) and [N II] lines (2.94 in the low-density regime) (Osterbrock & Ferland 2006) to take into account noise associated with the measured flux.

The results of this mitigated score is drawn on Fig. 6 with a red line. The real peaks are both present and all the false peaks have been removed. A more realistic example of this score is also shown in the top right quadrant of Fig. 5, where the false peaks, if not completely removed, have been attenuated enough so that the four brightest components are clearly visible.

3.2 Step 2: enumeration of the brightest components

Once the score is obtained, we must go through a peak detection process to enumerate the brightest components and evaluate their velocity, which is done by measuring the centroid of each detected peak. As the components may have similar velocities, their peaks may overlap, which complicates the detection.

We have used an iterative detection procedure not unlike the CLEAN algorithm (H''ogbom 1974). At each iteration, only the brightest peak is detected, fitted, and removed before moving on to the next iteration until no peaks can be detected above a threshold. The threshold was manually adjusted to keep the number of false detections negligible at the expense of loosing some of the dimmest components. An example of the resulting detection is shown in the top right quadrant of Fig. 5, where only four of the possibly five components are bright

enough to be considered. Since the noise of an FTS spectrum is distributed over all the channels and proportional to the total flux of the source, using a variable threshold based on our knowledge of the noise level for each spectrum may help in detecting components in dimmer regions of the Crab. This possibility will be explored in future versions of our algorithm.

At the end of this step we detected emission in 310 000 pixels (of the \sim 1 million spectra analysed). 73.2 per cent of them have only one component along the line of sight, 20.7 per cent contain two components, 4.95 per cent contain three components, and less than 1 per cent contain more than three components.

3.3 Step 3: fit of the spectrum

Once all the components are enumerated, a fit of the whole spectrum is attempted. This fit is done with ORCS, a PYTHON module designed especially to fit the spectra obtained with SITELLE (Martin et al. 2015). Given that the effective resolution is 10 per cent smaller than the theoretical resolution, the secondary lobes of the sinc ILS are small enough that a simple Gaussian model can be used. Five emission lines are fitted for each component: H α , the [N II] $\lambda\lambda6548$, 6583 doublet, and the [S II] λλ6716, 6731 doublet. Emission lines are fitted with a complete spectrum model at a fixed velocity for each component. The FWHM is fixed at the measured effective resolution. The flux ratio between the [NII] lines is also fixed at 3. Consequently, only five parameters are fitted for each component: 1 for the amplitude of the [NII] doublet, 3 for the amplitudes of the other lines, and 1 for the velocity of all five lines. An example of the resulting fit is shown in the bottom right quadrant of Fig. 5. We can see that most lines are well-fitted except for a possible fifth component which was neglected at the enumeration step because the threshold has been kept high enough to minimize the risks of false

The data obtained after the automatic fitting procedure is a set of 25 flux maps (5 emission lines \times 5 components, as no more than five components were clearly detected along the line of sight and only in a few cases) and five velocity maps (one for each component, since each set of emission lines were considered to share the same velocity parameter). Fig. 7 shows the velocity mapping and the relative total emitted flux in all the lines. All the components have been combined in the same image but, for the sake of clarity, when components are overlapping, only the front component is shown.

3.4 Step 4: mapping the Crab Nebula in Euclidean space

The remarkable work of Trimble (1968) demonstrated that proper motion velocity vectors of filaments all share the same origin both in position and time, and that the expansion velocity is approximately proportional to the radius. Subsequent analyses have come to similar conclusions (Wyckoff & Murray 1977; Nugent 1998; Kaplan et al. 2008; Bietenholz & Nugent 2015), though their results on the location of the explosion centre or the mean expansion velocity differ by a few arcseconds (Kaplan et al. 2008) (see Table 1). The expansion model we adopt is based on three parameters: the right ascension and declination (α_c , δ_c) of the expansion centre and the expansion factor e (e.g. Bietenholz & Nugent 2015):

$$\mu_{\alpha} = e(\alpha - \alpha_c),\tag{11}$$

$$\mu_{\delta} = e(\delta - \delta_c),\tag{12}$$

where α and δ are the coordinates of the filament and μ_{α} , μ_{δ} denote the proper motion along the right ascension and declination axes.

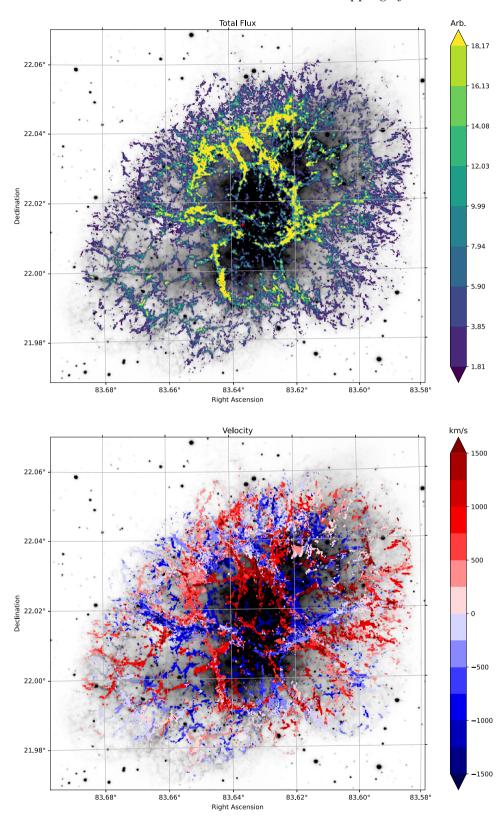


Figure 7. Integral of the emission in all five emission lines (top) and velocity (bottom) maps obtained. When components are overlapping, only the front component is displayed. The colour mapping has been discretized for the sake of clarity, but it does not reflect the actual precision of the values. The red cross indicates the centre of expansion computed by Kaplan et al. (2008). The velocity uncertainty is shown in Fig. A1. The background is the integral of the flux measured (emission lines + continuum) in the whole filter.

Table 1. Comparison of the expansion parameters computed by several authors. Most of the data comes from table 4 of Nugent (1998) and table 3 of Kaplan et al. (2008). Following Kaplan et al. (2008), $\Delta\alpha$ and $\Delta\delta$ are the offset in right ascension and declination between the centre of the explosion and the star 5 arcsec to the north-east of the pulsar (which was first used by Trimble 1968 as a reference given its proximity to the centre and its small proper motion). The coordinates of the reference star $\alpha = 05^{\rm h}34^{\rm m}32.1827^{\rm s}$, $\delta = +22^{\circ}00^{'}56.002^{''}$ come from the *Gaia* DR2 catalogue (Brown et al. 2018).

Reference	$\Delta \alpha$ (arcsec)	$\Delta\delta$ (arcsec)	Outburst Date (CE)
Trimble (1968)	7.6(1.7)	-8.5(1.4)	1140(15)
Wyckoff & Murray (1977)	8.2(2.7)	-8.6(3.6)	1120(7)
Nugent (1998)	9.4(1.7)	-8.0(1.3)	1130(16)
Kaplan et al. (2008)	8.4(0.4)	-8.1(0.4)	

It has long been known that when the measured expansion velocity is projected back to the origin, the computed outburst date lies around 1130 CE, which is nearly a hundred years after the recorded outburst date of 1054 CE (Stephenson & Green 2002). This is attributed to material having been accelerated by the Crab's pulsar wind nebula. Thus, we can expect some sort of signature of this acceleration preferentially near the centre of the explosion. From the preliminary results of a new analysis of the proper motion of the Crab (Martin et al., in preparation), we believe that there indeed might be an accelerated expansion near the centre, which means that the expansion factor is higher near the centre than it would be if following a purely linear model. However, as a first approximation we choose to consider a simple linear model and use the expansion factor e = $1.160(15) \times 10^{-3} \text{ yr}^{-1}$ computed by Nugent (1998) along with the expansion centre $\alpha = 05^{\text{h}}34^{\text{m}}32.74(03)^{\text{s}}, \delta = +22^{\circ}00^{'}47.9(0.4)^{''}$ determined by Kaplan et al. (2008) from their study of the pulsar proper motion. The validity of this hypothesis is discussed in more detail in Section 4.1.1.

To construct a 3D mapping of the Crab Nebula we require an estimate of its distance. We adopt 2 kpc, computed by Trimble (1973), who estimates it to lie between 1.7 and 2.4 kpc from prior morphological considerations. This distance has not been improved since then and is still in use in recent articles (see e.g. Hester 2008;

Kaplan et al. 2008). At this distance 1 arcsec = 9.696×10^{-3} pc and the radial distance d to the expansion centre can be computed from the radial velocity v_r via the expansion factor (Ng & Romani 2004):

$$d = \frac{v_r}{e} \tag{13}$$

Knowing the expansion factor and the distance to the Crab makes it possible to obtain a mapping of our data in the Euclidean space (in parsecs) as shown in Fig. 8 and Appendix B. Given the complexity of our data we have created an interactive visualization in PYTHON accessible through a Jupyter Notebook. It may be found at https://github.com/thomasorb/M1_paper. The 3D visualization program can also be run directly in any html browser at https://mybinder.org/v2/gh/thomasorb/M1_paper/master and does not require any particular computing knowledge.

Two movies have been created with the help of PANDA3D, an opensource framework for 3D rendering (Goslin & Mine 2004). They are available online as Supporting Information. Both show the total flux emitted in all five emission lines. Each data point is represented as a small cube and corresponds to one velocity component at a given pixel. No data points have been added by interpolation. The thickness of some of the brightest filaments along the line of sight comes from the fact that they could be resolved and fitted with two components instead of one. The Milky Way background has been adequately positioned to simulate what would be the typical perspective of someone moving around the nebula. The Milky Way map has been created by the NASA/Goddard Space Flight Center Scientific Visualization Studio (https://svs.gsfc.nasa.gov/4851) based in part on the data obtained with Gaia (Brown et al. 2018). One of the movies shows a glowing sphere at the centre to simulate the blue continuum emitted by the pulsar wind nebula with an intensity to roughly match that observed in the composite HST image presented by Loll et al. (2013). The soundtrack is a sonification of the data set. Using the interferograms directly as a sound wave, we have mixed multiple samples played at different rates. The volume of the samples is related to the square of the distance to the nebula and the playing speed is related to the velocity of the observer with respect to the nebula. A second movie highlights the geometry of the Crab Nebula. The obtained data are shown with the inner and outer envelopes

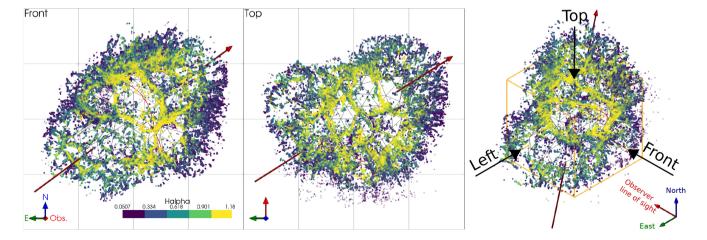


Figure 8. Front (as seen from Earth) and top view of the H α emission. The right-hand panel displays an isometric representation of the nebula showing the different viewpoints considered in the paper. The central part is filled with the inner envelope (see section 4.1.2) so that the rear-facing components are obscured. The red arrow represents the pulsar torus axis and the red line shows the intersection of the inner surface with the pulsar torus plane as fitted by Ng & Romani (2004). All axes are in parsecs and the spatial grid of the left-hand and central panels has a 1 pc stepping. The orientation symbol is colour coded: east is green, north is blue, and the line-of-sight direction is red.

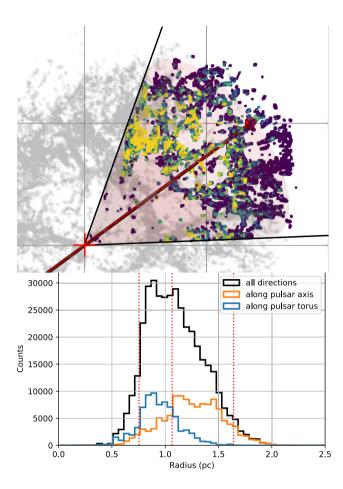


Figure 9. Representation of the emitting material contained in a solid angle originating from the explosion centre and aligned along the pulsar axis. All axes are in parsecs and the spatial grid has a 1 pc stepping.

described in the next section. The pulsar axis and the plane of the pulsar torus are indicated.

4 MORPHOLOGY OF THE CRAB NEBULA

4.1 Inner and outer envelopes

4.1.1 Outer envelope

Each of the H α , [N II] $\lambda\lambda$ 6548, 6584, and [S II] $\lambda\lambda$ 6716, 6731 3D maps we have created is a collection of volume elements (voxels) that occupy the same volume in space and for which we can measure an emission-line flux. This volume is bounded by the surface of 1 pixel at the distance of the nebula (0.32 arcsec at 2 kpc, i.e. 3.1×10^{-3} pc) and an element of spectral resolution along the line of sight (35 km s⁻¹, i.e. 3.1×10^{-2} pc), which yields a voxel volume of 3.0×10^{-7} pc³.

Representing our observations as voxels in this way provides a detailed representation of the Crab's complex distribution of material and permits an investigation of its morphology at small and large scales. For example, it is worth testing whether or not the Crab is an ellipsoid, as long suspected (e.g. Hester 2008). To this end, we can analyse the radial distribution of the emitting material contained in a solid angle originating from the explosion centre and obtain the radial extent of the nebula by computing the outer limit of this distribution in all directions. To illustrate, we show in Fig. 9 the distribution of material integrated over all directions along the pulsar torus axis. We see that no material extends beyond 2 pc.

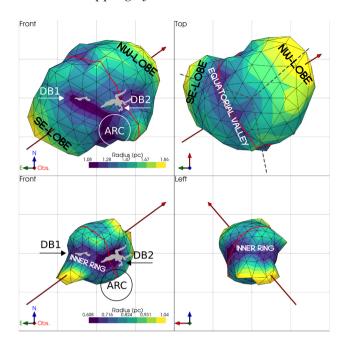


Figure 10. Top: outer envelope enclosing 97 per cent of the material emitting in $H\alpha$. The binning angle covers 22.5° . Bottom: inner envelope enclosing 8 per cent of the material emitting in $H\alpha$. The binning angle covers 45° . The positions of the dark bays (Fesen et al. 1992) and the arcade region (Dubner et al. 2017) are shown as well as the High-Helium bands first observed by Uomoto & MacAlpine (1987, in grey). We have also reported the topologic features referenced in the text. Other details are the same as Fig. 8.

Because the emission $I(H\alpha)$ is very roughly proportional to the square of the ionized hydrogen density n_p (at a constant temperature along the line of sight), $I(H\alpha) \propto n_p^2$, we choose to weight this distribution by $\sqrt{I(H\alpha)}$ in order to approximately sample the distribution of the material density.

We define the outer limit of the nebula in one particular direction as the radius that encompasses 97 per cent of the material emitting in $H\alpha$ which is contained in a solid angle of 22.5° . We repeat this procedure over all directions, using the coordinates of the vertices of a 320-faced icosphere which ensures an homogeneous distribution of the probing directions (see Appendix C1 for more details). Consequently, we obtain the outer envelope of the emitting material, that is, the dominant shape of the Crab as made up by its visible gas. Two perspectives of this outer limit surface are shown in Fig. 10, and all six perspectives are shown in Fig. B1.

Note that, doing this in the plane of the sky and considering only the red part of the visible spectrum would reveal the well-known elliptical outer envelope of the Crab. But the 3D outer envelope is most surprising since it differs notably from the generally assumed ellipsoidal shape (e.g. Hester 2008). As viewed from the *top*, which we define as being along the axis perpendicular to the observer's line of sight looking from the north toward the south, a conspicuous heart-shaped morphology oriented along the pulsar axis is visible. The most rapidly expanding NW and SE lobes are separated by 120° of each other. The NW lobe is nearly aligned with the pulsar torus axis, but the SE lobe is not.

The potential effects of inhomogeneities of the expansion factor must be considered since this spatial reconstruction is mostly based on a homologous expansion hypothesis (i.e. a constant expansion factor in all directions) which is not absolutely true. Using the data obtained by Trimble (1968), we find that the expansion is

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indeed accelerated towards the north-west direction by a factor of 15 per cent with respect to the median value of the expansion factor $(e = 1.160(15) \times 10^{-3} \text{ yr}^{-1})$ computed by Nugent (1998) and used in this article to derive the 3D model of the nebula (see Fig. 11). Of course, this accelerated expansion is associated with a dilatation of the ellipsoidal shape of the nebula in the same direction. Knowing only the proper motion of the nebula and using a homologous expansion model to compute its shape, one would have exaggerated this dilatation effect, resulting in a nebula with an envelope even more extended towards the north-east direction. We have fitted an ellipsoid to the computed outer envelope and obtained the dilatation ratio. The centre of the ellipsoid coincides with the centre of expansion and its major axis follows the axis of the pulsar torus. As shown in Fig. 11, the dilatation ratio of the SE lobe (which gives its heart shape to the nebula) is around 1.3. It would require an expansion inhomogeneity of the same order to keep the model compatible with an ellipsoid, which is two times larger than what is observed in the celestial plane. Moreover, this expansion inhomogeneity should not be related with any extension of the nebula in this direction, which is in contradiction with the correlation we observed based on Trimble (1968) data. We are thus confident that, if the computed 3D model of the nebula might indeed be exaggerated along the line of sight, the general shape should not differ enough to make it completely compatible with an ellipsoid.

4.1.2 Inner envelope

The Crab shows an intricate complex of filamentary structures going deep under its outer envelope, and it can be difficult to easily identify 3D locations of material. Thus, it is of interest to define the inner extent of this material, that is, the size and the morphology of the central void of ionized gas around the centre of expansion, to distinguish front-facing from rear-facing ejecta. If we look at the distribution of material and integrate over all directions (Fig. 9) we see that no material is located below 0.5 pc. However, we take this a step further by examining the 3D extent of this void in all directions. Using the same procedure as the one used to obtain the outer envelope, we obtained the inner envelope considering a radius enclosing only 8 per cent of the material emitting in H α in a solid angle of 45°. The limit of 8 per cent may seem high but is explained by the relatively high number of spurious detections near the centre. We have thus slowly increased the limit up to the point where the 3D shape of the inner surface was not changing anymore (except for its scale). Two perspectives of this inner limit surface are shown in Fig. 10, and all six perspectives are shown in Fig. B2.

4.1.3 Comparison of the inner and outer envelopes

Comparing the inner and outer envelopes reveals clear trends in the overall morphology of gas. Material around the plane defined by the pulsar torus mapped by Ng & Romani (2004) is much closer to the explosion centre than the material distributed along the pulsar axis. This can be seen as a circular pinched valley running along the pulsar torus plane (labelled *equatorial valley*). On the front of the nebula two small depressions are seen (labelled DB1 and DB2 on the figure) that coincide with the pinched velocity regions observed by MacAlpine et al. (1989) and the helium-rich bands observed by Uomoto & MacAlpine (1987). Another indentation is seen in the general region of the 'arcade of loops' described by Dubner et al. (2017). The two depressions DB1 and DB2 also coincide with the positions of the dark bays (Fesen et al. 1992), also observed in the X-ray (Seward, Tucker & Fesen 2006), and UV (see e.g. Dubner et al.

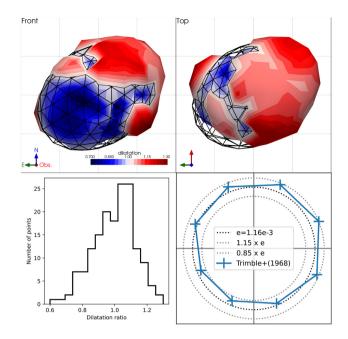


Figure 11. Top: ellipsoid (wire frame) fitted to the outer envelope. The ellipsoid represents the surface of dilatation factor unity. Its centre coincides with the centre of expansion and its major axis follows the axis of the pulsar torus. The colour of the outer envelope represents its dilatation factor. Regions above the ellipsoid are red, while regions below are blue. All axes are in parsecs and the spatial grid has a 1 pc stepping. The orientation symbol is colour coded: east is green, north is blue, and the line-of-sight direction is red. Bottom left: histogram of the dilatation of the outer envelope with respect to the fitted ellipsoid. Bottom right: median of the expansion factor measured by Trimble (1968) along different directions (north is up and east to the left). The circles of homologous expansion are represented with dotted lines. The north-west acceleration appears clearly and can be related to the dilatation along the north-west lobe but there is no acceleration as high as the 1.3 dilatation factor observed in the SE lobe. Even if we consider the largest expansion factor measured in the plane of the sky (1.15), this is not sufficient to explain the factor 1.3 dilatation observed in the south-west lobe.

2017). Interestingly, the locations of the dark bays also coincide with a conspicuous restriction oriented along the east—west plane running along the perimeter of the inner envelope (labelled *inner ring*). Together, these shared features between the inner and outer envelopes strongly suggest a constrained expansion of the nebular material, potentially due to interaction with a pre-existing circumstellar disc left by the progenitor star (Fesen et al. 1992; Smith 2013).

4.2 Filamentary structure

High-resolution images of the Crab show that its filaments exhibit a complex and fine structure (see e.g. Hester et al. 1996; Blair et al. 1997; Sankrit et al. 1998). Many filaments are less than an arcsecond in width and point inward into the centre of the nebula, with lengths ranging from ≈ 1 to 20 arcsec. Filaments are also often connected by arc-like bridges of emission with a 'bubble-and-spike' morphology (Hester 2008). Numerous studies have associated this morphology with RT instabilities (see e.g. Chevalier & Gull 1975; Hester et al. 1996; Bucciantini et al. 2004; Stone & Gardiner 2007; Porth, Komissarov & Keppens 2014). These instabilities are generally characterized by two parameters. (1) Angular size, that is, the wavelength of the perturbations, which is strongly related to the stability of the shell. Numerical magnetohydrodynamic simulations (Bucciantini et al. 2004) show that only perturbations at a scale smaller than $\sim \pi/10$ should give rise to RT instabilities and to the

observed structures with protruding fingers. (2) The size of the filaments, which should also be related to the wavelength of these perturbations.

In Fig. 12, we show the whole structure as if all voxels were at the same radius in a classical Mercator projection, and in Fig. D1 as orthographic projections. All maps are gridded with triangles having sides covering an angle of $16.6^{\circ} (\simeq \pi/11)$, which is helpful to measure the relative sizes of the different structures.

Crab material is largely distributed along boundaries resembling a honeycomb. This structure is hierarchical; that is, larger regions ($\sim \pi/3.5$) have thicker filaments, while other regions, in particular in the high-velocity lobes, exhibit a much smaller and thinner distribution ($\sim \pi/10$). The interior of the largest structures is generally divided into smaller regions that are also at a larger radii. The size of the structures appear to be anticorrelated with the radius; that is, the largest and most conspicuous structures are at smallest radii with smallest expansion velocities. Some of the largest structures, seen clearly on the top and back views of Fig. 12, exhibit a polygonal shape and are found all along the pulsar torus equatorial plane. One also sees these structures when viewing the Crab through narrow slices along different orientations (Fig. 13). The largest regions are localized in the interior with diameters of 0.5–1 pc. Above these at larger radii lie numerous smaller bubbles.

5 DISCUSSION

There exist very few kinematic maps of SNRs detailed enough that a comparison of the shape of their filamentary structure can be studied. Fig. 12 shows a comparison of the Mercator projections of the Crab, 3C 58 (Lopez & Fesen 2018) and Cas A (Milisavljevic & Fesen 2013). Large-scale ejecta rings may be a common phenomenon of young, core-collapse SNRs (Milisavljevic & Fesen 2017). The largest and deepest structures of the Crab are similar both in size and shape as those seen in 3C 58. However, both the Crab and Cas A share small-scale circular formations.

3C 58 has many overlapping properties with the Crab. The Crab Nebula is far brighter and more luminous than 3C 58, but both remnants are bright in both the radio and X-rays in their centre and harbour young, rapidly spinning central pulsars that provide the magnetic field and relativistic particles that generate the observed centre-filled synchrotron radiation. 3C 58 may be connected to the historical event of 1181 CE (Stephenson & Green 2002; Kothes 2013), which would make it only 127 yr younger than the Crab. However, this relatively young age is inconsistent with its overall angular size (6.3 arcmin \times 10.3 arcmin) and proper motion measurements of its expanding ejecta (Fesen, Kirshner & Becker 1988; van den Bergh 1990) that suggest a much older remnant, potentially as old as 2400 ± 500 yr.

Cas A is the youngest known core-collapse remnant with an estimated explosion date of 1681 CE (Fesen et al. 2006). Milisavljevic & Fesen (2013) demonstrated that the bulk of the remnant's main shell ejecta are arranged in several well-defined complete or broken ring-like structures. These ring structures have diameters that can be comparable to the radius of the remnant (\sim 1 pc). Some rings show considerable radial extensions giving them a crown-like appearance, while other rings exhibit a frothy, ring-like substructure on scales of \sim 0.2 pc. A subsequent 3D map of its interior unshocked ejecta made from near-infrared observations sensitive to [S III] $\lambda\lambda$ 9069, 9531 emission lines revealed a bubble-like morphology that smoothly connects with these rings (Milisavljevic & Fesen 2015).

In the case of Cas A, the rings of ejecta have been interested to be the cross-sections of reverse-shock-heated cavities in the remnant's internal ejecta (Milisavljevic & Fesen 2013). A cavityfilled interior is in line with prior predictions for the arrangement of expanding debris created by a post-explosion input of energy from plumes of radioactive ⁵⁶Ni-rich ejecta (Li, McCray & Sunyaev 1993; Blondin, Borkowski & Reynolds 2001). Such plumes can push the nuclear-burning zones located around the Fe core outward, creating dense shells separating zones rich in O, S, and Si from the Ni-rich material. After the SN shock breakout additional energy input from the radioactive decay of ⁵⁶Ni continues to drive inflation of ⁵⁶Ni-rich structures and facilitates mixing between ejecta components. This late time expansion can modify the overall SN ejecta morphology on time-scales of weeks or months. Compression of surrounding nonradioactive material by hot expanding plumes of radioactive ⁵⁶Nirich ejecta generates a 'Swiss cheese'-like structure that is frozen into the homologous expansion when the radio-active power of ⁵⁶Ni is strongest. Gabler, Wongwathanarat & Janka (2020) found that this 'Ni-bubble effect' accelerates the bulk of the nickel in their 3D models and causes an inflation of the initially overdense Ni-rich clumps, which leads to underdense, extended fingers, enveloped by overdense skins of compressed surrounding matter.

Stockinger et al. (2020) recently performed 3D full-sphere simulations of SNe originating from non-rotating progenitors similar to those anticipated to be associated with the SN 1054. Their lowenergy explosions ($\sim 0.5-1.0 \times 10^{50} \, \mathrm{erg}$) are compared in two contrasting scenarios: (1) iron-core progenitors at the low-mass end of the core-collapse SN domain ($\approx 9 \,\mathrm{M}_{\odot}$), and (2) a super-asymptotic giant branch progenitor with an oxygen-neon-magnesium core that collapses and explodes as ECSN. They disfavour associating SN 1054 with an ECSN because the kick experienced by the neutron star is negligible and inconsistent with the observed $\approx 160 \text{ km s}^{-1}$ transverse velocity of Crab pulsar. Instead, they favour simulations with iron-core progenitors with less second dredge-up that result in highly asymmetric explosions with hydrodynamic and neutrinoinduced NS kick of $>40 \text{ km s}^{-1}$ and an NS spin period of $\sim 30 \text{ ms}$, not unlike the Crab pulsar. The resulting distribution of ⁵⁶Ni-rich material from these explosions, which enable efficient mixing and dramatic shock deceleration in the extended hydrogen envelope, is potentially consistent with our mapping of Crab ejecta. However, simulations extending the evolution from ~days to ~1000 yr are needed to verify this extrapolation (see e.g. Orlando et al. 2016).

6 CONCLUSIONS

We have presented a 3D kinematic reconstruction of the Crab Nebula that has been created from a hyperspectral cube obtained with SITELLE. The data are comprised of 310 000 high-resolution ($R=9\,600$) spectra containing H α , [N II], and [S II] line emission, and represent the most detailed homogeneous spectral data set ever obtained of the Crab Nebula.

Our findings can be summarized as follows:

- (i) The general shape of the Crab, as measured by 97 per cent of the material emitting in $H\alpha$, occupies a 'heart-shaped' volume and is symmetrical about the plane of the pulsar wind torus. This morphology runs counter to the generally assumed ellipsoidal volume and is not an artefact of assuming a uniform global expansion. The most rapidly expanding NW and SE lobes are separated by 120° of each other. The NW lobe is nearly aligned with the pulsar torus axis, but the SE lobe is not.
- (ii) Conspicuous restrictions in the distribution of material as mapped by the inner and outer limits of emission is seen along the band of He-rich filaments (Uomoto & MacAlpine 1987; MacAlpine

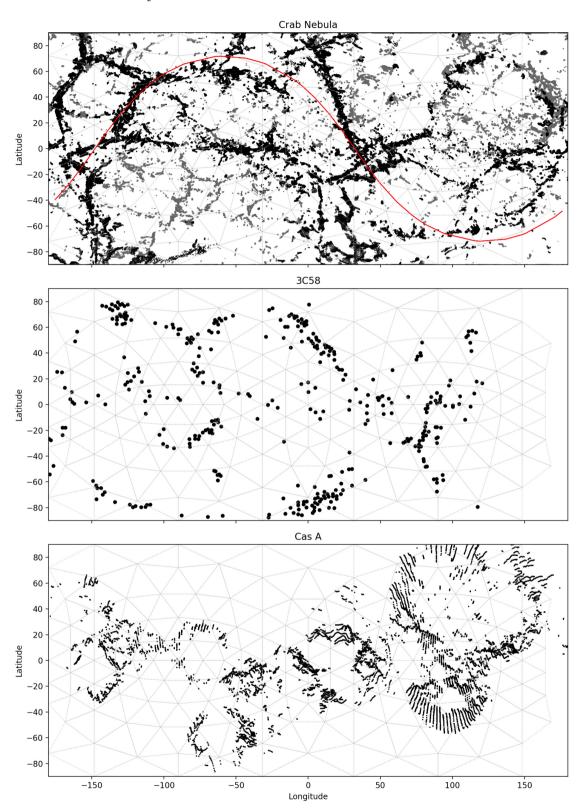


Figure 12. Top: Mercator projection of total flux of the emitting material in the Crab. The densest and deepest buried material (at less than 1.1 pc of the centre) is represented in black, while the faster expanding material is in grey. As the angles are not conserved, we overplot a grid of triangles which vertices sides cover an angle of 16.6° ($\simeq \pi/11$). The red line shows the pulsar torus plane as fitted by Ng & Romani (2004). The centre of the latitude and longitude axes corresponds to the centre of expansion in the face-on view. Longitude increases towards the west. Middle and bottom: Mercator projections of 3C 58 (Lopez & Fesen 2018), and Cas A (Milisavljevic & Fesen 2013), respectively.

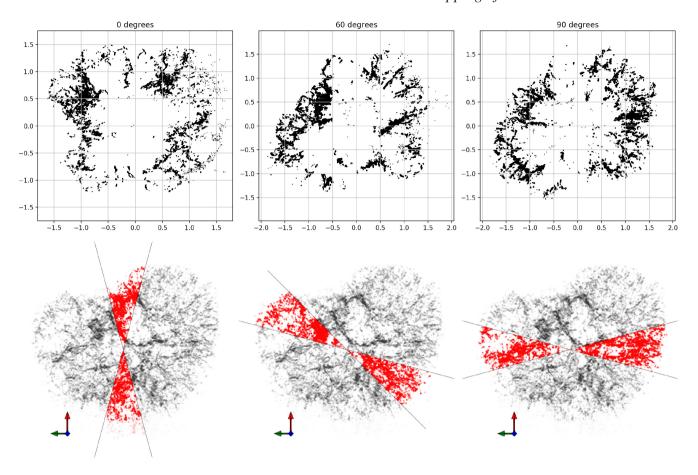


Figure 13. Slices in three different directions with respect to the line of sight direction. The slice at 90° being the canonical point of view perpendicular to the line of sight. All points at $\pm 15^{\circ}$ are merged together so that the angular size of a slice is 30° . A top view of the selected pixels is shown at the bottom. It shows the slice extent used to generate the plots in the corresponding upper panel. Axes are in pc. The orientation symbol is colour coded: east is green, north is blue, and the line-of-sight direction is red.

et al. 1989). Notable depressions are also coincident with the east and west dark bays (Fesen et al. 1992). Together these features are consistent with constrained expansion of Crab ejecta, possibly associated with interaction between the SN and a pre-existing cirumstellar disc.

(iii) The filaments follow a honeycomb-like distribution defined by a combination of straight and rounded boundaries at large and small scales. The scale size is anticorrelated with distance from the centre of expansion; that is, largest features are found at smallest radii. The structures are not unlike those seen in other SNRs, including 3C 58 and Cas A, where they have been attributed to turbulent mixing processes that encouraged outwardly expanding plumes of radioactive ⁵⁶Ni-rich ejecta.

The observed kinematic characteristics reflect critical details concerning the original SN of 1054 CE and its progenitor star, and may favour a low-energy explosion of an iron-core progenitor as opposed to an oxygen-neon-magnesium core that collapses and explodes as an ECSN. Planned future observations will provide additional hyperspectral cubes spanning more wavelength windows that include the emission lines of [O II] $\lambda\lambda$ 3726, 3729, H β , [O III] $\lambda\lambda$ 4959, 5007, [N II] λ 5755, and He I λ 5876. These lines will be measured and modelled to determine temperature, density, and abundances at very fine scales, and combined with an updated proper motion investigation of filaments (Martin et al., in preparation) to improve the accuracy of our reconstruction at fine scales. Our

work contributes to a larger suite of detailed SNR reconstructions being developed that will provide unique constraints for increasingly sophisticated 3D core-collapse simulations (Couch et al. 2015; Wongwathanarat et al. 2017; Burrows, Radice & Vartanyan 2019; Stockinger et al. 2020), that are being evolved to middle-aged SNRs (Orlando et al. 2015, 2016, 2020), attempting to model the complete multimessenger signals of SNe (Andresen et al. 2017; Kuroda et al. 2017; Westernacher-Schneider et al. 2019; Mezzacappa et al. 2020).

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DATA AVAILABILITY

The data underlying this article will be shared on reasonable request to the corresponding author.

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SUPPORTING INFORMATION

Supplementary data are available at MNRAS online.

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APPENDIX A: VELOCITY UNCERTAINTY

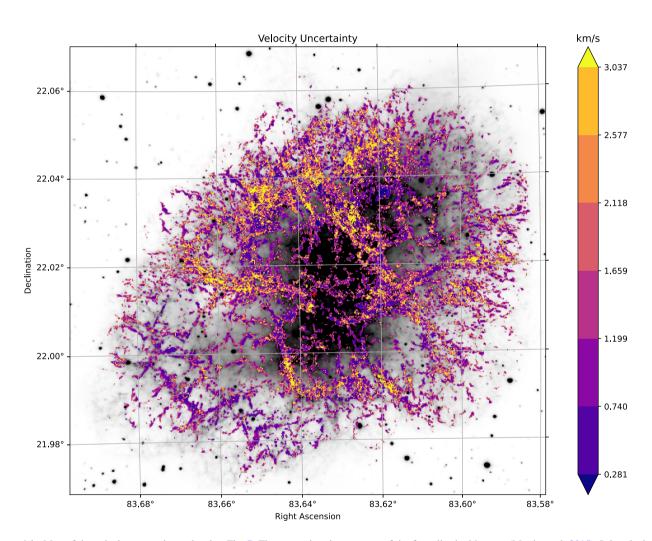


Figure A1. Map of the velocity uncertainty related to Fig. 7. The uncertainty is an output of the fit realized with ORCS (Martin et al. 2015). It is calculated from the covariance matrix returned by the Levenberg–Marquardt minimization process (Levenberg 1944; Marquardt 1963). As all five emission lines for each velocity component share the same velocity parameter, the uncertainty is generally smaller that the uncertainty that would have been obtained by fitting the emission lines independently. As other constraints are implemented in the spectrum model (see Section 3.3) the emission-line velocities and fluxes are the parameters of one spectrum model. As such their uncertainty are only loosely related to the SNR of each emission line (see Martin et al. 2015 for more details).

APPENDIX B: 3D MAPS

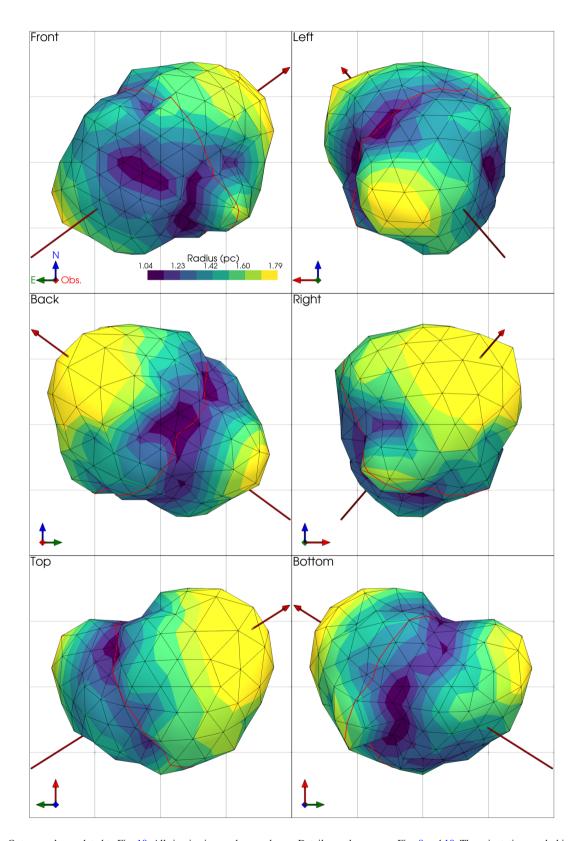


Figure B1. Outer envelope related to Fig. 10. All six viewing angles are shown. Details are the same as Figs 8 and 10. The orientation symbol is colour coded: east is green, north is blue, and the line-of-sight direction is red.

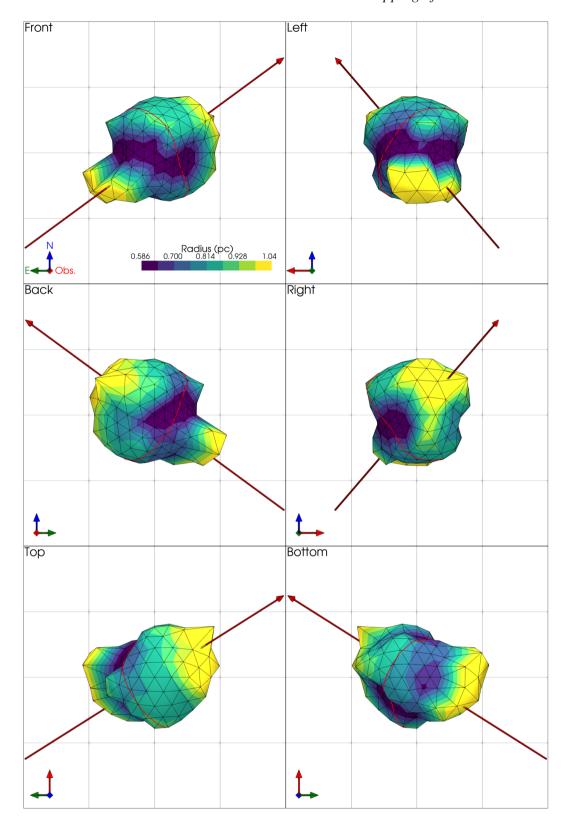


Figure B2. Inner envelope related to Fig. 10. All six viewing angles are shown. Details are the same as Figs 8 and 10. The orientation symbol is colour coded: east is green, north is blue, and the line-of-sight direction is red.

APPENDIX C: ICOSPHERE

1880

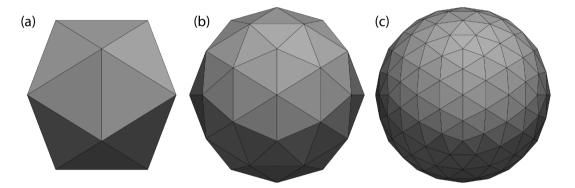


Figure C1. Icosahedron (a, 20 faces), subdivided two times along its edges to make the 80 (b) and 320 faces (c) icospheres. This type of sphere approximation is interesting since its vertices are homogeneously distributed. We used the 320 icosphere to construct the inner and outer envelopes as well as to make a homogeneous grid on the projections of Figs 12 and D1.

APPENDIX D: FILAMENTARY STRUCTURE

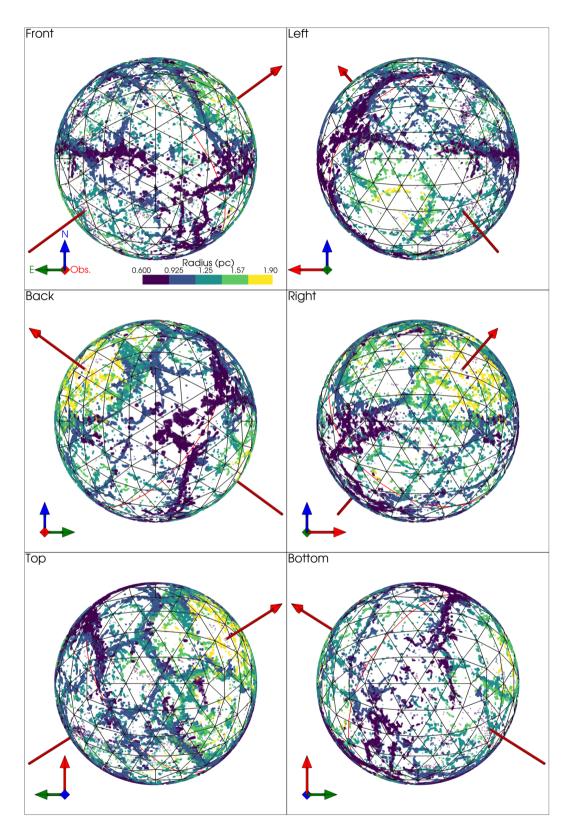


Figure D1. Orthographic projections of all the voxels at the same unit radius to reveal the structuration of the filamentary envelope of the nebula. This is presented as an alternative to Mercator projections shown in Fig. 12 which produce important distortions far from the equator. A grid of triangles with 16.6° ($\simeq \pi/11$) sides helps to measure the size of the structures. The red arrow indicates the direction of the pulsar torus and the red line shows its equator. The orientation symbol is colour coded: east is green, north is blue, and the line-of-sight direction is red.

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