

Discovery and characterization of five new eclipsing AM CVn systems

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ABSTRACT

AM CVn systems are ultra-compact, hydrogen-depleted, and helium-rich, accreting binaries with degenerate or semidegenerate donors. We report the discovery of five new eclipsing AM CVn systems with orbital periods of 61.5, 55.5, 53.3, 37.4, and 35.4 min. These systems were discovered by searching for deep eclipses in the Zwicky Transient Facility (ZTF) light curves of white dwarfs selected using *Gaia* parallaxes. We obtained phase-resolved spectroscopy to confirm that all systems are AM CVn binaries, and we obtained high-speed photometry to confirm the eclipse and characterize the systems. The spectra show double-peaked He lines but also show metals, including K and Zn, elements that have never been detected in AM CVn systems before. By modelling the high-speed photometry, we measured the mass and radius of the donor star, potentially constraining the evolutionary channel that formed these AM CVn systems. We determined that the average mass of the accreting white dwarf is $\approx 0.8 M_{\odot}$, and that the white dwarfs in long-period systems are hotter than predicted by recently updated theoretical models. The donors have a high entropy and are a factor of ≈ 2 more massive compared to zero-entropy donors at the same orbital period. The large donor radius is most consistent with He-star progenitors, although the observed spectral features seem to contradict this. The discovery of five new eclipsing AM CVn systems is consistent with the known observed AM CVn space density and estimated ZTF recovery efficiency.

Key words: binaries: eclipsing – novae, cataclysmic variables – white dwarfs.

1 INTRODUCTION

AM CVn systems are ultra-compact accreting binaries with degenerate or semidegenerate, hydrogen-depleted and helium-rich donors. They are part of the family of cataclysmic variables; a primary white dwarf that is accreting mass from a donor via Roche lobe overflow (Warner 1995). For AM CVn binaries, the donors are degenerate and the binary is very compact with orbital periods ranging from 65 to as short as 5 min (see Solheim 2010 for a review). Thousands of AM CVn systems are expected to be present in our Galaxy, but

their intrinsic faintness limits the known population to ≈ 60 AM CVn systems (see Ramsay et al. 2018 for a recent compilation).

Because of their compactness and short orbital periods, AM CVn stars are an excellent tool to study accretion physics under extreme conditions (e.g. Kotko et al. 2012; Coleman et al. 2018; Cannizzo & Ramsay 2019; Oyang, Jiang & Blaes 2021). Their short orbital periods also means that their angular momentum losses are dominated by gravitational wave radiation. Several hundred AM CVn systems will be detectable by the Laser Interferometer Space Antenna (LISA, Amaro-Seoane et al. 2017) satellite and are one of the most abundant types of persistent LISA sources (Kremer et al. 2017; Breivik et al. 2018; Kupfer et al. 2018). LISA will continuously observe these systems and will show the orbital period evolution of short-period

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AM CVn systems. AM CVn systems are also potential progenitors of rare transient events. Bildsten et al. (2006) discuss that, as a layer of He builds up on the accreting white dwarf, recurring He-shell flashes can occur, which would look like He-Novae. The mass of the He-shell becomes larger and the time between flashes longer as the systems evolve to longer orbital periods. This can result in a very energetic ‘final-flash’, which can be dynamical and eject material from the white dwarf, dubbed a ‘Ia’ transient (Shen et al. 2010). The most important open question regarding AM CVn systems is their formation channel, and how AM CVn systems fit into the overall picture of compact binary evolution (see Section 2.1 and also Nelemans et al. 2001; Toloza et al. 2019).

In this paper, we present the search of Zwicky Transient Facility (ZTF) light curves to find new eclipsing white dwarf binaries and the discovery of five new AM CVn systems and their characterization. In Section 2, we briefly summarize the current understanding of the formation channels and observational properties of AM CVn systems and discuss the currently known eclipsing systems. Section 3 presents the method and search of the ZTF light curves used to find the five new eclipsing AM CVn systems. Section 4 presents all the follow-up observations, high-speed photometry and phase-resolved spectroscopy, and archival data used to characterize the systems. Section 5 presents the methods we used to characterize the systems, and Section 6 presents the results of this analysis. In Section 7, we discuss the implications of the measurements, specifically what the results imply for the formation channels of AM CVn systems. We summarize this paper in Section 8 and end with a short discussion on future work in Section 9.

2 BACKGROUND

2.1 Formation channels

There are three proposed AM CVn formation channels, but their relative importance is uncertain. In the white dwarf channel, a short-period double white dwarf binary is formed after going through two common envelope phases (Ivanova et al. 2013). The resulting binary is a typical CO white dwarf with a low-mass helium white dwarf companion (Paczynski 1967; Tutukov & Fedorova 1989; Deloye et al. 2007). They evolve closer together as a result of gravitational wave radiation and start stable mass transfer at orbital periods of ≈ 2 – 3 m and evolve to longer orbital periods. Simulations by Nelemans et al. (2001) predicted the white dwarf channel to be the dominant formation channel. However, Shen (2015) suggests that all double white dwarfs merge (because of friction with ejected material in a nova eruption), and double white dwarfs do not form AM CVn systems.

The second formation channel, the He-star channel, is similar to the white dwarf channel, but instead of a low-mass white dwarf, the donor progenitor is a non-degenerate He-burning star. These will also evolve to shorter periods but start mass transfer at slightly longer periods of 10 min (Savonije, de Kool & van den Heuvel 1986; Iben & Tutukov 1987; Tutukov & Fedorova 1989; Yungelson 2008; Brooks et al. 2016).

The third formation channel is the evolved-CV channel. In this scenario, the donor must evolve off the main sequence at the same time as the start of mass transfer. The system goes through a phase as a hydrogen-dominated CV and will eventually change into a helium-dominated CV once all the hydrogen has been stripped from the donor (e.g. Podsiadlowski, Han & Rappaport 2003). Models indicate that this channel is rare and does not contribute significantly to the AM CVn population. This is due to the finely tuned starting

parameters and long time-scales required to remove all visible hydrogen from these systems (Nelson et al. 2018). However, there are known helium CVs, which are potential progenitors of the channel (Thorstensen et al. 2002; Breed et al. 2012; Carter et al. 2013b; Green et al. 2020).

2.2 Observational properties

Although AM CVn systems are all accreting DB white dwarfs with a degenerate or semidegenerate donor, their observational characteristics vary significantly. Their appearance (both photometric and spectroscopic) is very different because of differences in the accretion rate, which is strongly correlated with the orbital period. The accretion rate determines the behaviour of the accretion disc (Kato et al. 2001; Nelemans, Yungelson & Portegies Zwart 2004; Ramsay et al. 2012; Kupfer et al. 2013; Coleman et al. 2018) and also sets the accreting white dwarf temperature (e.g. Bildsten et al. 2006).

Very short period ($P \lesssim 10$ m) AM CVn systems have high accretion rates and, depending on the masses, can be ‘direct impact’ accretors. In these systems, there is no accretion disc and the accretion stream directly impacts the white dwarf. These systems emit X-rays, for example, HM Cnc and V407 Vul (Marsh, Nelemans & Steeghs 2004). Systems with periods $\gtrsim 10$ m form accretion discs. System with periods of ≈ 10 – 22 m of the high accretion rate, the systems are in a constant ‘high state’ (Kotko et al. 2012). Intermediate-period systems (≈ 22 – 45 m) with lower accretion rates show dwarf nova outbursts and feature large amounts of flickering in their light curves (see Duffy et al. 2021). As the orbital period increases, the outburst recurrence time increases exponentially (Levitan et al. 2015), and the luminosity of the disc decreases as the orbital period decreases. In long-period systems ($\gtrsim 45$ m), the accretion rate is low, outbursts are very rare (recurrence times of > 100 yr), and the accreting white dwarf dominates the luminosity (Bildsten et al. 2006).

Ramsay et al. (2018) give an overview of the currently known sample of AM CVn systems. This sample has been built up using various methods. Many AM CVn systems (including AM CVn itself) were identified by their blue colour and identification spectra. This method was used most recently by Carter et al. (2013a) who used SDSS colour information. The second main method of finding AM CVn systems is by their outbursts. Breed et al. (2012) and Breed et al. (2014) obtained spectra of Catalina Real-time Transient Survey (CRTS) dwarf novae and found three new AM CVn systems. Levitan et al. (2015) used the Palomar Transient Factory (PTF) to identify cataclysmic variables and identified AM CVn systems with follow-up spectroscopy. van Roestel et al. (2021a) combined the colour selection and outburst selection methods and identified nine new AM CVn systems. Isogai, Kawabata & Maeda (2019) also focused on outbursting CVs but instead used high-cadence photometry to find the period and identify a system as an AM CVn system. Searching for short-period variability was also used to identify a new AM CVn system using Kepler data (Fontaine et al. 2011; Kupfer et al. 2015; Green et al. 2018b). Finally, in parallel with this work, Burdge et al. (2020) searched for compact binaries by searching for short-period variability in ZTF data.

2.3 Eclipsing AM CVn systems

Among the sample of known AM CVn systems, only a few have been confirmed as eclipsing. Eclipsing AM CVn systems where the primary white dwarf is eclipsed by the donor are extremely valuable since they allow the binary parameters to be measured. Hardy

et al. (2017) provide examples of modelling eclipsing accreting cataclysmic variable light curves with various accretion rates.

Three eclipsing AM CVns have been studied in detail so far. The first is PTF1J1919 + 4815, in which just the edge of the disc and bright-spot are eclipsed (Levitan et al. 2014). The second is YZ LMi where the white dwarf is partially eclipsed (Anderson et al. 2005; Copperwheat et al. 2011). Gaia14aae (ASASSN-14cn) is the only published AM CVn in which the white dwarf is confirmed to be fully eclipsed by the donor (Campbell et al. 2015; Green et al. 2018a, 2019a). Besides these well-studied cases, there are also a number of promising candidates. Burdge et al. (2020) presented the discovery of a candidate 17.20 orbital period eclipsing AM CVn system also using ZTF data. In addition, follow-up of ES Cet by Bakowska et al. (2020) indicates that this system is also eclipsing, although it seems that in this case only the disc is eclipsed and not the accreting white dwarf.

Because for YZ LMi and Gaia14aae the white dwarf is eclipsed, the donor mass and radius have been measured to a few per cent accuracy by modelling the light curve. These precise measurements and their comparison with models show an interesting result (Copperwheat et al. 2011; Green et al. 2018a). The donor for YZ LMi is relatively large and is consistent with either the helium star channel or the white dwarf channel. The donor in Gaia14aae is large, which is consistent only with mass–radius models describing the evolved CV channel. This is a surprising result since the evolved CV channel is expected to be the most uncommon channel of the three. These studies demonstrate that eclipsing AM CVn systems allow us to precisely characterize them and better understand their evolutionary history. This motivated us to perform a dedicated search for eclipsing AM CVn systems.

3 TARGET SELECTION

3.1 Zwicky Transient Facility light curves

As part of the ZTF, the Palomar 48-inch (P48) telescope images the sky every night (Bellm et al. 2019a; Graham et al. 2019; Dekany et al. 2020). Several sub-surveys are carried out by ZTF (Bellm et al. 2019b), including an all-sky survey (publicly available), but also higher cadence surveys of smaller areas (e.g. van Roestel et al. 2019; Kupfer et al. 2021). Most surveys use g and r bands, but a small fraction of the observations are done in i band. The exposure times are predominantly 30 s for g and r and 60 s for i exposures. The median limiting magnitude, averaged over the lunar cycle, is $r \approx 20.5$ in all three bands. ZTF images are automatically processed and two main data products are generated. The first are the ‘alerts’, which are based on difference imaging and are mainly designed to identify transients. The second main data product is PSF photometry of persistent sources in the science images (for a full description, see Masci et al. 2019).

3.2 Search method

To find deep eclipsing white dwarfs, we combined the PSF photometry data from the science images with the alert data generated from the difference images. We do this because the PSF photometry is reported only for sources that are detected with a significance of 5 standard deviations in the science image. If the target shows a deep eclipse, no PSF photometry is reported. Alerts are generated only for 5-sigma detection on the difference images, both positive and negative. A non-detection of a source thus generates a negative alert. The negative alerts (like the positive alerts) are vetted by a

‘real-bogus’ system, which is based on deep learning (Duez et al. 2019).

To identify periodic eclipses, we used the Boxed-Least-Square (BLS) algorithm¹ (Kovács, Zucker & Mazeh 2002). We normalized the g , r , and i data and combined them into a single light curve, rejecting any points that were flagged as potentially bad (5–10 per cent, mostly due to clouds). In addition, we removed any points that were more than 5 standard deviations above the median level of light curve in order to reject outbursts. We searched a linear frequency grid and used a frequency step inversely proportional to the baseline and the minimum eclipse duration and used an additional oversampling factor of 10. This typically results in a grid of a few million frequencies to be searched. To identify the best period, we simply used the period with the highest power. In the case of multiple best periods, we used the longest period.

As a post-processing step, we fit the phase-folded light curve with a simple trapezoid plus two sinusoids to model an eclipse, reflection effect, and ellipsoidal modulation. The eclipse width is shared between colour bands, but the depth of the eclipse and amplitude of any sinusoidal component is independently determined for each band. Periods, the period power, the goodness-of-fit of the model, and other statistics were saved for later selection of light curves for visual inspection.

3.3 Application to the ZTF light curves

We analyzed the ZTF light curves DR3 and private data (available on 2019 December 11) of all the sources in the *Gaia* DR2 white dwarf catalogue from Gentile Fusillo et al. (2019) in our search for eclipsing white dwarfs. We processed all light curves with more than 80 epochs in g and r combined (241 775 objects) and searched a period range from 0.02 d (28.8 m) to 5 d on a linear scale in frequency. The lower limit was chosen to reduce the computational time and because Burdge et al. (2020) have already searched for shorter period systems. We visually inspected the folded light curves for all objects in the white dwarf catalogue, which had at least one alert associated with it (6 412 objects). For the rest, we inspected only light curves for which the model fit showed an improvement of $\Delta\chi^2 > 50$ compared to fitting a straight line (27 116 objects). In this work, we present the AM CVn systems found using this method; a full catalogue of eclipsing white dwarf and other interesting discoveries (e.g. van Roestel et al. 2021b) will be presented in future work.

Fig. 1 shows the folded ZTF light curves of the five eclipsing AM CVn systems we discovered in the sample of eclipsing white dwarfs and Table 1 gives their observational properties. ZTFJ1637+49 (also discovered by Keller et al. 2021) is located in a region of the sky that is observed at a higher cadence by ZTF as part of a ZTF partnership survey. For this reason, many more epochs are available compared to the rest of the sky. This allowed us to discover this object first, despite the eclipse being the most shallow and narrow of the five objects, and the fact that no alerts were generated for this object. ZTFJ0220+21 and ZTFJ0407-00 both show negative ‘alerts’ in both g and r bands. A visual inspection of their light curves confirmed their orbital period. ZTFJ0407-00 also showed one outburst, which combined with its period, immediately confirmed its nature as an AM CVn system. We note that ZTFJ0407-00 was also identified as an outbursting cataclysmic variable by ASASSN and *Gaia* as ASASSN-18dg and Gaia20aby.

¹<https://github.com/johnh2o2/cuvarbase>

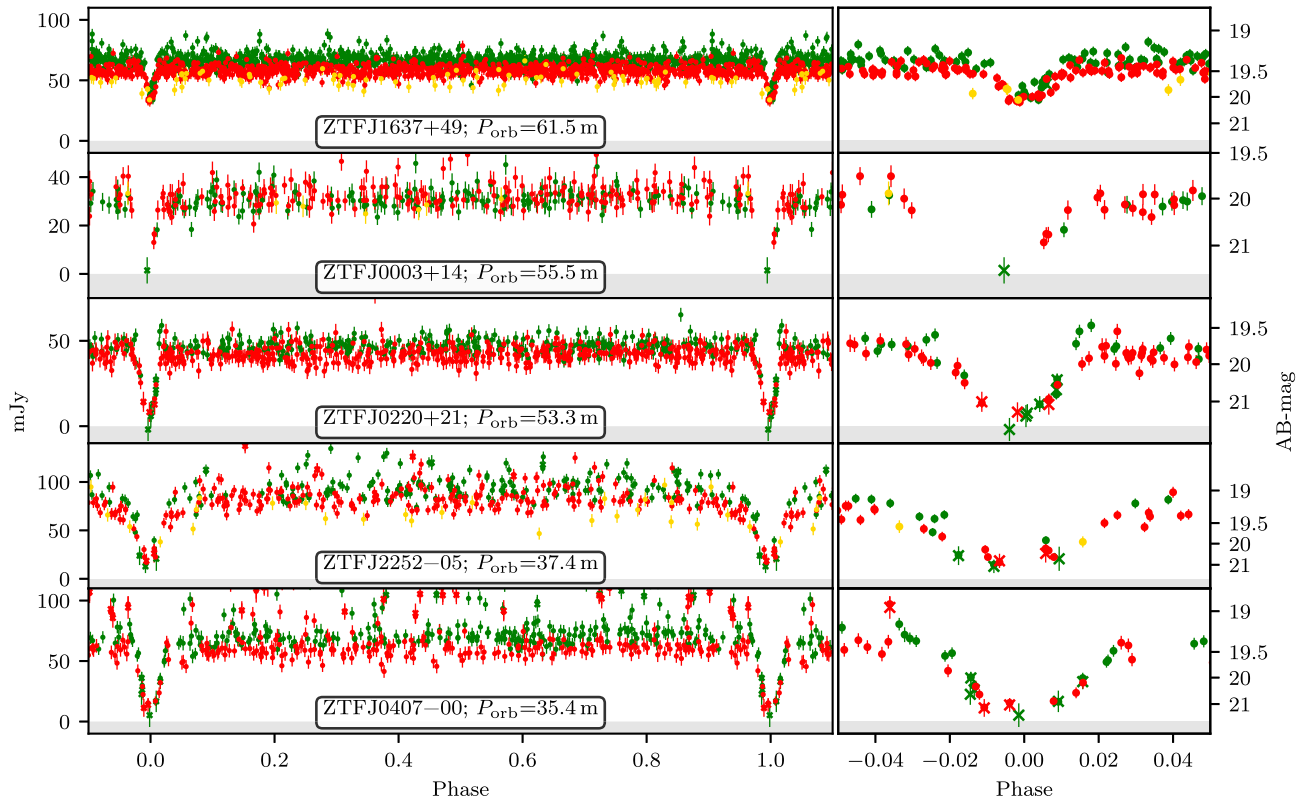


Figure 1. The ZTF light curves of the five new AM CVn stars folded on their orbital periods. ZTF *g*, *r*, and *i* bands are displayed in green, red, and gold. Dots show ZTF PSF photometry and crosses show ZTF alert photometry. The narrow eclipse in each of the light curves was used to discover these objects. The two short-period systems also show irregular variability in their light curves (see Section 6.4 and Fig. 9).

ZTFJ2252-05 was identified later in a general search of persistent sources, which have a *Gaia* parallax (Bailer-Jones et al. 2018) and are located close to the white dwarf track and have negative ZTF alerts. This sample contained a total of 11 766 ZTF sources. ZTFJ2252-05 triggered three negative alerts, and a BLS-period search of the light curve identified a potentially short period, which was confirmed using CRTS and PTF data. ZTFJ2252-05 was not found in the initial search because its *Gaia* parallax was very uncertain and not included in the catalogue by Gentile Fusillo et al. (2019).

ZTFJ0003+14 was identified as a candidate in the initial search but was initially not followed up because of the sparse ZTF light curve and red $BP - RP$ colour. With more epochs available, the eclipse became more prominent and follow-up data confirmed its nature as an AM CVn system.

4 OBSERVATIONS

For each system, we obtained high-speed photometry and phase-resolved spectroscopy. An overview of all follow-up observations can be found in the online materials. In addition, we used multiple surveys to study the long time-scale evolution and spectral energy distribution.

4.1 LRIS spectroscopy

Phase-resolved spectroscopy of all systems was obtained using the Keck I Telescope (HI, USA) and the Low-Resolution Imaging Spectrometer (LRIS; Oke et al. 1995; McCarthy et al. 1998). We used a $1''$ slit, with the R600 grism for the blue arm, and R600 grating

for the red arm. With this setup, spectral resolution is approximately $R \approx 1100$ in the blue arm and $R \approx 1400$ in the red arm. For one spectrum, we used the R300 grating, which has a resolution of $R \approx 800$.

A standard long-slit data reduction procedure was performed with the LPIPE pipeline² (Perley 2019). The pipeline reduced LRIS spectral data to spectra using the standard procedure, including calibration with a standard star. Wavelength calibration was done using lamp spectra obtained at the beginning and end of each sequence. Fine-tuning of the wavelength calibration was done using sky-lines.

In order to identify spectral lines, we interpolated the spectra to a common wavelength grid, averaged them, and normalized the result using a seventh-order polynomial fitted by minimizing the absolute error. The absolute error is less sensitive to emission and absorption lines compared to the squared error commonly used.

4.2 CHIMERA fast cadence photometry

CHIMERA (Harding et al. 2016) is a dual-channel photometer that uses frame-transfer, electron-multiplying CCDs mounted on the Hale 200-inch (5.1 m) Telescope at Palomar Observatory (CA, USA). The pixelscale is 0.28 arcsec/pixel (unbinned). We used the conventional amplifier and used 2×2 binning on most nights (except when the seeing was excellent) to reduce the readout noise and readout time. Each of the images was bias subtracted and divided by twilight flat fields.³

²<http://www.astro.caltech.edu/~dperley/programs/lpipe.html>

³<https://github.com/caltech-chimera/PyChimera>

Table 1. Overview of the five new eclipsing AM CVn stars discovered by their eclipses using ZTF light curves. The parallax is taken from *Gaia* eDR3 Brown et al. (2020). The distance is calculated using a prior based on the white dwarf population (Kupfer et al. 2018). The dust extinction is taken from Green et al. (2019b).

Name	RA	Dec	P_{orb} minutes	ZTF- <i>g</i> AB-mag	ZTF- <i>r</i> AB-mag	<i>G</i> Vega-mag	<i>BP</i> – <i>RP</i> Vega-mag	Parallax mas	Distance pc	$E(g-r)$
ZTFJ1637+49	16 ^h 37 ^m 43 ^s .6	49°17′40″.9	61.5	19.34	19.49	19.40	0.27	4.88 ± 0.27	207 ⁺⁸ ₋₈	<0.01
ZTFJ0003+14	00 ^h 03 ^m 22 ^s .4	14°04′59″.0	55.5	20.19	20.14	20.20	0.35	4.03 ± 0.54	263 ⁺²⁹ ₋₄₀	0.10 ^{+0.02} _{-0.02}
ZTFJ0220+21	02 ^h 20 ^m 08 ^s .6	21°41′55″.8	53.3	19.72	19.82	19.76	0.09	2.94 ± 0.50	350 ⁺³⁹ ₋₅₈	0.14 ^{+0.02} _{-0.02}
ZTFJ2252-05	22 ^h 52 ^m 37 ^s .1	-05°19′17″.4	37.4	19.05	19.16	19.09	0.04	1.95 ± 0.31	536 ⁺⁸² ₋₉₃	0.01 ^{+0.01} _{-0.02}
ZTFJ0407-00	04 ^h 07 ^m 49 ^s .3	-00°07′16″.7	35.4	19.23	19.41	19.42	0.07	1.33 ± 0.37	810 ⁺¹⁹⁰ ₋₂₃₀	0.14 ^{+0.01} _{-0.02}

We used the ULTRACAM pipeline to do aperture photometry (Dhillon et al. 2007). We used an optimal extraction method with a variable aperture of 1.5 times the full width at half-maximum (FWHM) of the seeing (as measured from the reference star). A differential light curve was created by simply dividing the counts of the target by the counts from the reference star. Timestamps of the images were determined using a GPS receiver.

We obtained CHIMERA data for each target in the *g* and *r* or *i* filters during dark or grey time. The seeing for the CHIMERA observations was typically between 0.8 and 1.5 arcsec.

4.3 HiPERCAM fast cadence photometry

HiPERCAM is a high-speed camera for the study of rapid variability (Dhillon et al. 2021) and is able to obtain images in *ugriz* simultaneously. HiPERCAM was mounted on the 10.4-m Gran Telescopio Canarias on La Palma (Spain). With this telescope, HiPERCAM has a 0.081″/pixel scale and a 3.1′ field of view across the diagonal.

We obtained 76 min of data in *ugriz* of ZTFJ1637+49. The observation was timed such that the light curves cover two eclipses. The data were reduced using the dedicated HiPERCAM pipeline,⁴ including debiasing and flat-fielding. Differential light curves were constructed using a single reference star. Timestamps were obtained from a GPS receiver.

4.4 ‘Alopeke fast cadence photometry

‘Alopeke is a low-noise, dual-channel imager mounted on the Differential Speckle Survey Instrument (Scott 2019) of the 8-m Gemini North Telescope on Mauna Kea (Hawaii, USA). In the blue arm, we used the *g* filter and in the red arm we used the *i* filter. The pixelscale of the wide-field mode is 0.07 arcsec/pixel.

Alopeke was used to obtain five light curves of the eclipse of ZTFJ0220+21. Images were bias subtracted and flat-fielded using the standard procedure. We used aperture photometry to extract light curves using the ULTRACAM pipeline. No bright stars were close enough to use differential photometry. Instead, we used a large aperture of 2.5 times the average FWHM and used the raw light curve. No GPS receiver was available for Alopeke, so we used computer timestamps instead.

4.5 Archival photometry

To study the long time-scale photometric variability and the spectral energy distribution, we obtained single epoch or averaged photometry data from multiple other survey telescopes: *Galex* (Bianchi,

Shiao & Thilker 2017), *Gaia* eDR3 (Brown et al. 2020), and *WISE* (Marocco et al. 2020). We also obtained multi-epoch photometry from SDSS (Alam et al. 2015), Pan-STARRS (Chambers et al. 2016), CRTS (Drake et al. 2009), ASAS-SN (Shappee et al. 2014; Kochanek et al. 2017), PTF (Law et al. 2009; Rau et al. 2009), and ATLAS (Tonry et al. 2018; Smith et al. 2020).

5 METHODS

5.1 Timing

To determine the ephemerides of the mid-eclipse times, we use both the ZTF light curve, archival data (SDSS, PS, and CRTS) and the follow-up photometry. We fit the normalized and combined ZTF *g*, *r*, and *i* light curves with the best *lcurve* model (see Section 5.4) as determined from the high-cadence photometry. The only free parameters are the period and mid-eclipse time. As a prior, we use the measured mid-eclipse times from the CHIMERA, HiPERCAM, and Alopeke light curves. In addition, we also add the epochs of any individual in-eclipse points from SDSS, Pan-STARRS, and PTF, and use half their exposure time as the uncertainty. The uncertainties (standard deviations) are determined by using *emcee* (Foreman-Mackey et al. 2013).

5.2 Doppler tomography

To better understand the geometry of the system, we use Doppler tomography (Marsh 2001). Doppler tomography converts a series of 2D spectra obtained at different phases of the orbit into a velocity map (also called a Doppler map). We used the He-I lines at 6678.15, 7065.17, and 7281.35 Å for ZTFJ1637+49, ZTFJ0220+21, and ZTFJ0407-00, because these are not blended with other lines. For ZTFJ0003+14 and ZTFJ2252-05, more blue spectra are available and in this case, we use He- I lines in the blue spectra: 3613.64, 3634.23, 3888.64, 4026.19, and 4921.93 Å. To make the Doppler maps from the LRIS spectra, we used the PYTHON package DOPPLER.⁵ We used a blurring scale of 40 kms⁻¹, and manually set the target reduced χ^2 value to avoid over- or underfitting the map.

5.3 Modelling of the spectral energy distribution

To estimate the white dwarf temperature, we fit the spectral energy distribution of the systems by simply modelling them as a blackbody. The model parameters are the temperature (T_{eff}), the radius of the white dwarf (R_{WD}), the distance (d), and the amount of reddening using the Fitzpatrick (1999) reddening law with the parameter $E_B - V$.

⁴<https://github.com/HiPERCAM/>

⁵<https://github.com/trmrsh/trm-doppler>

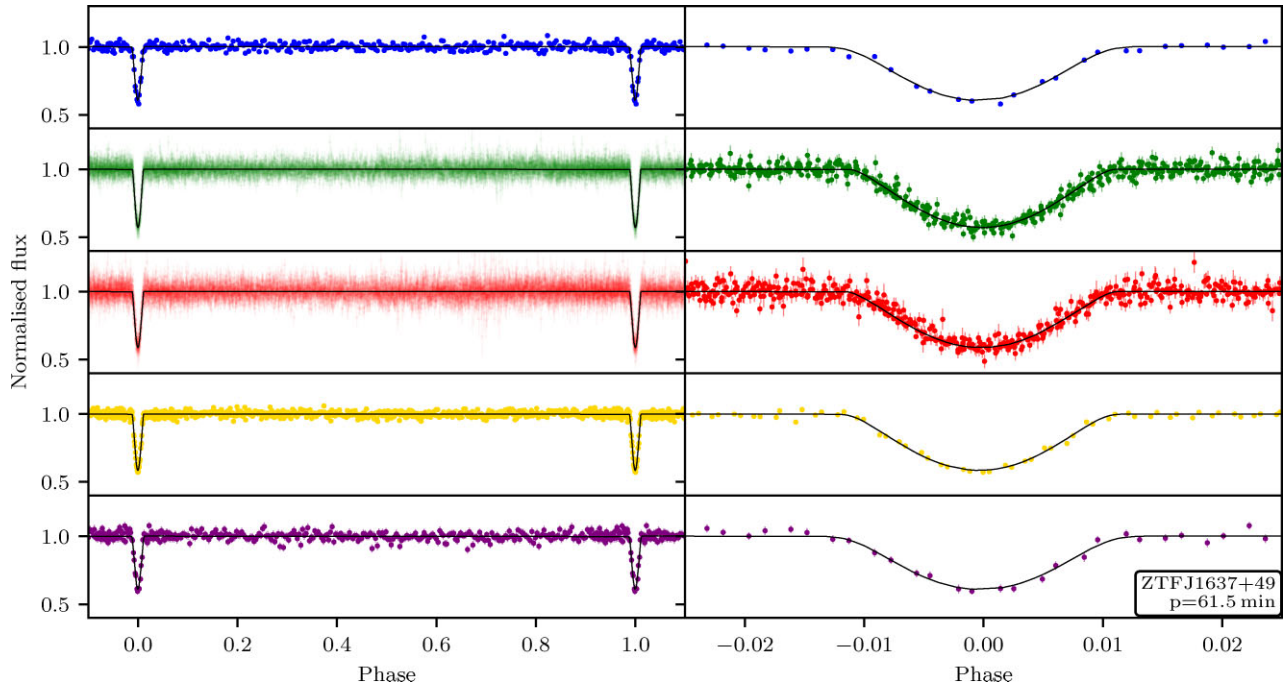


Figure 2. The light curves of ZTFJ1637+49 with the best-fitting models overplotted in the *ugriz* bands (blue, green, red, gold, and purple; from top to bottom). The eclipse depth is identical in each of the five bands, which suggests that there is no contribution from the disc or bright-spot. Therefore, the light-curve model (black line) does not include these components, and the model includes only a white dwarf that is eclipsed by a cold and dark, Roche lobe filling donor.

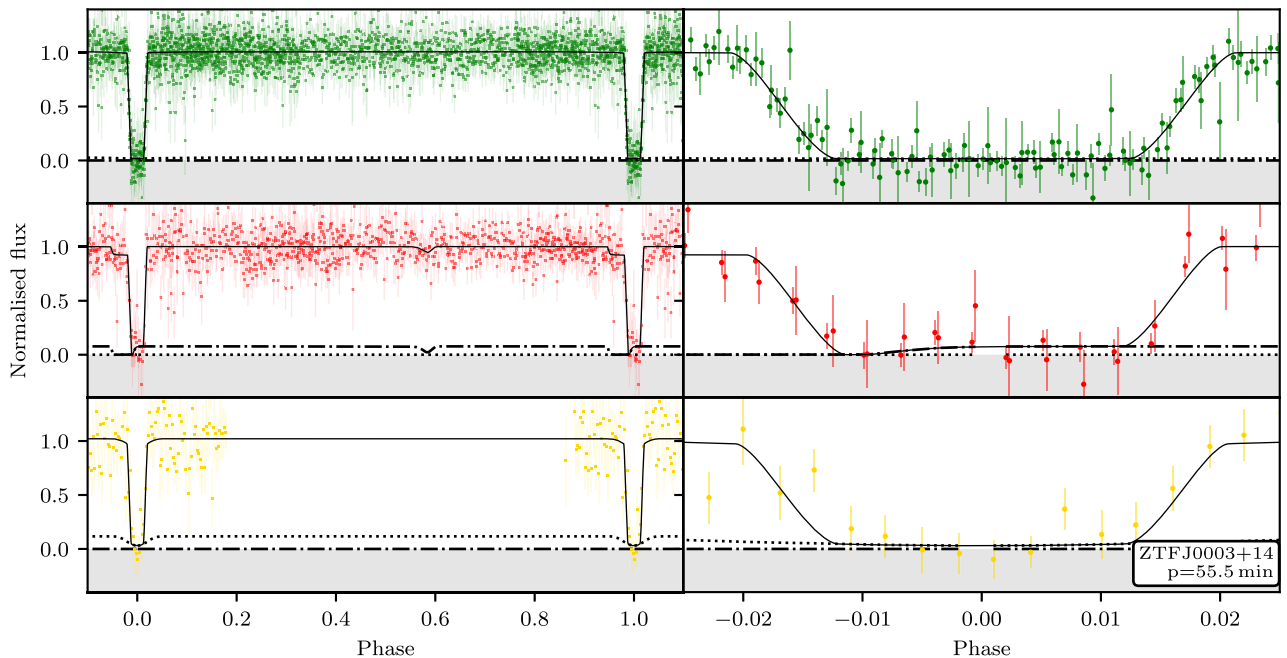


Figure 3. The combined light curves of ZTFJ0003+14 in the *gri* bands, similar to Fig. 2. The full model is shown by the black line, the contribution from the disc is shown by the dotted line, and the contribution by the bright-spot is shown by the dashed-dotted line. The model shows that the white dwarf dominates the luminosity, and disc and/or bright-spot contribute only $\lesssim 10$ per cent to each light curve (see also Table 4).

We constrain the distance by putting a Gaussian prior directly on the parallax using *Gaia* eDR3 values. We also use a Gaussian prior on the radius of the white dwarf using the values obtained using the light-curve modelling. Finally, we constrain the value of E_{B-v} using the Pan-STARRS dustmap (Bayestar19, Green et al. 2019b), with the conversion $E_{B-v} = 0.884E_{g-r}$.

We converted the magnitudes to flux using the zero-points for each filter⁶ (Rodrigo et al. 2012; Rodrigo & Solano 2020). We use the effective wavelength for each filter to calculate the model flux.

⁶<http://svo2.cab.inta-csic.es/theory/fps/>

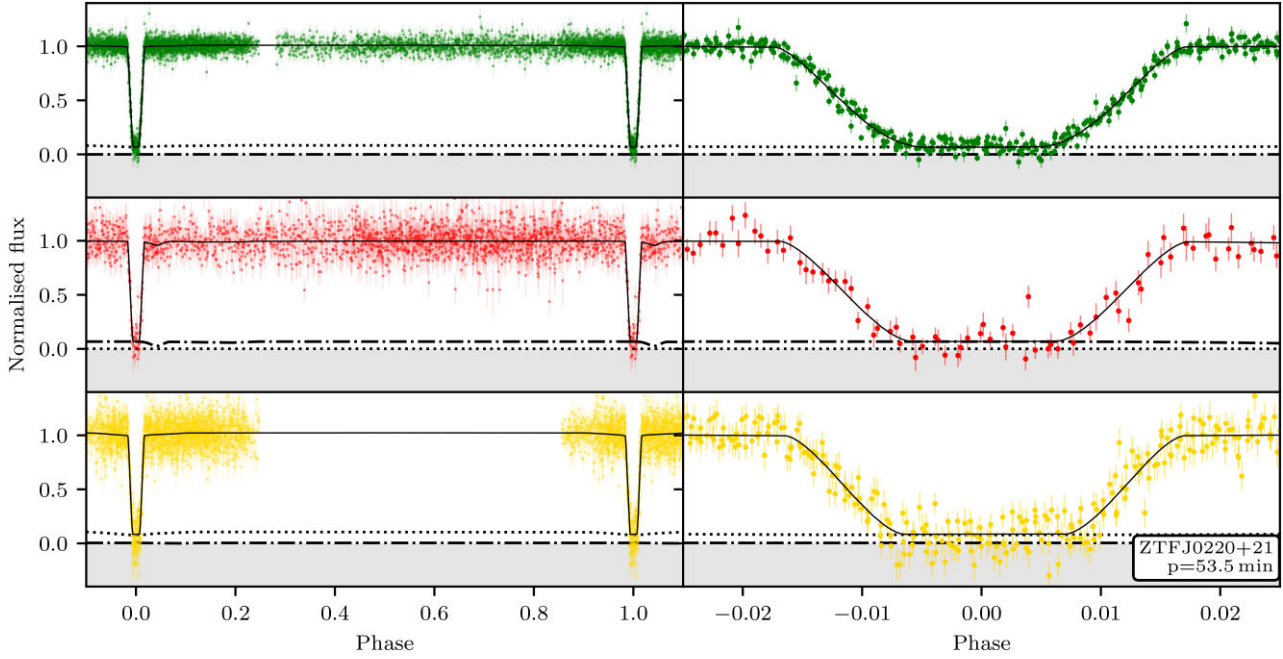


Figure 4. The combined light curves of ZTFJ0220+21 in *gri* bands (top to bottom, see also Fig. 3). Similar to ZTFJ0003+14, the white dwarf dominates the luminosity and disc and/or bright-spot contribute only $\lesssim 10$ per cent.

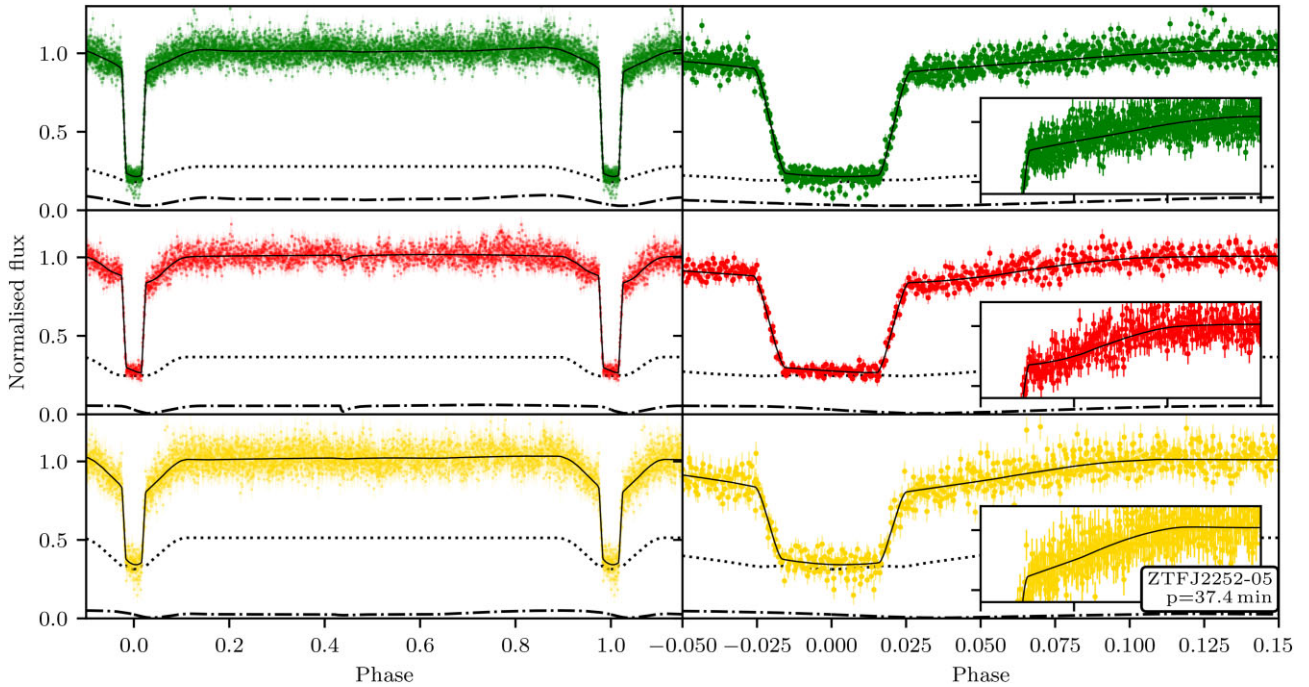


Figure 5. The combined light curves for ZTFJ2252-05 in the *gri* bands (top to bottom). The full model is indicated by the black line, while the contribution from the disc and bright-spot is indicated with a dotted and dashed-dotted line. The light curves have been detrended, but flickering remains visible. The disc contributes significantly more compared to the longer period systems (27–51 per cent), with larger contributions for longer wavelengths. In each of the light curves, a few per cent (3–7 per cent) contribution from the bright-spot is also visible, shown in the inset.

The observed flux is the combined flux from the white dwarf, disc, bright-spot, and the donor. Using the *gri* light curves of the fully eclipsing systems, we can disentangle the contributions from the different components by modelling the light curves in those three bands (see Figs 2–6). For each system, we use the model to determine how much the disc and the bright-spot contribute. We

use this to correct the *gri* magnitudes from PS, SDSS, and ZTF magnitudes.

To find the optimal solution and uncertainties, we use *emcee*. We use a likelihood function assuming Gaussian uncertainties. In order to account for any systematic errors, we include an additional error term in the model, which is optimized together with the other

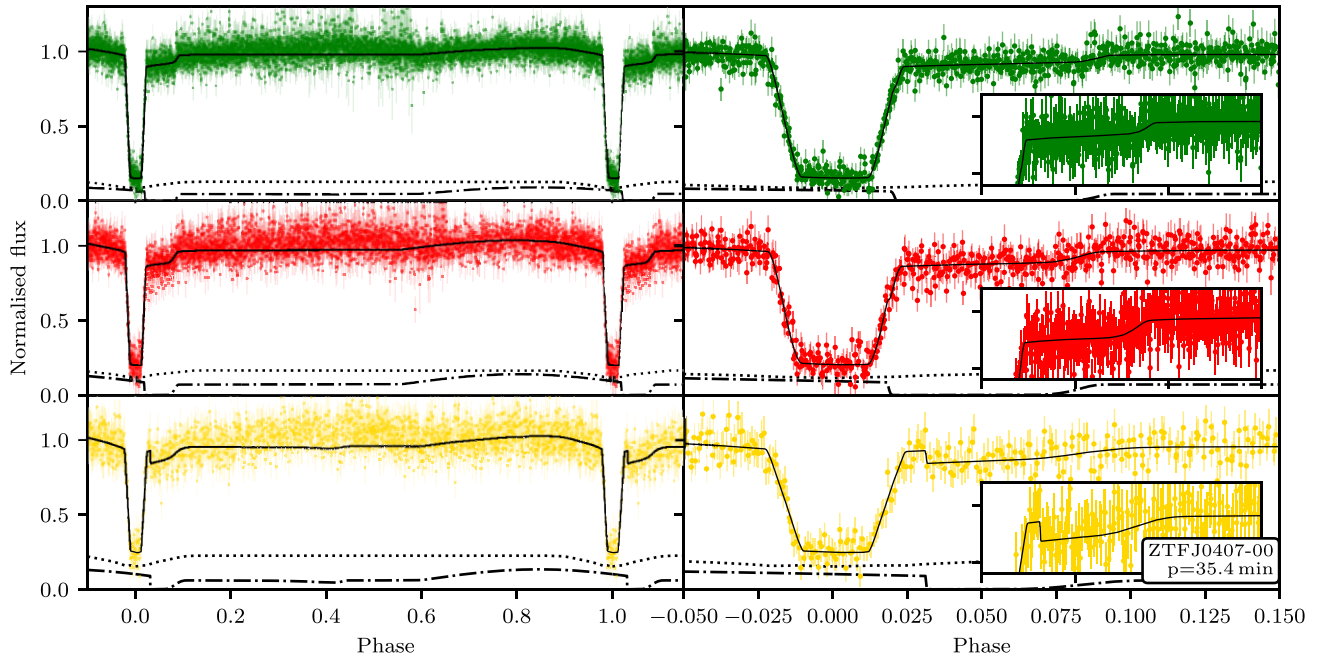


Figure 6. The combined light curves of ZTFJ0407-00 in *gri* bands (top to bottom, similar to Fig. 3). Compared to ZTFJ2252-05, the disc contributes less for this system (13–22 per cent). The overall contribution by the bright-spot is similar as for ZTFJ2252-05 but the eclipse is clearly visible in the *g* and *r* light curves.

parameters. The measurements in other bands are used as upper limits (implemented as one-sided Gaussians). We exclude the two *WISE* bands from the fit as these are likely dominated by the disc and/or donor.

For ZTFJ1637+49 and ZTFJ0003+14, we deviated from this general approach. ZTFJ1637+49 shows only partial eclipses, and we cannot use the eclipse depth and shape to disentangle the contribution to the overall luminosity by the different components. We use the uncorrected magnitudes to fit the white dwarf model and assume that the other components can be neglected, which is justified because this is a very long-period system with a very low accretion rate and cold donor. We exclude the SDSS *r*-band measurement, which was obtained during an eclipse and is 0.5-mag fainter than other *r*-band observations.

For ZTFJ0003+14, the SDSS data were significantly brighter than the PS and *Gaia* data, which suggests that the system was in outburst when SDSS observed it. We, therefore, use the SDSS *ugriz* data as upper limits only.

5.4 Light-curve modelling

We use *Lcurve*⁷ to model the light curves and infer the binary parameters. *Lcurve* uses 3D grids to simulate two stars (spherical or with a Roche geometry). In addition, a disc and bright-spot can be added to the model. In this section, we briefly summarize the model setup. For a detailed description of *Lcurve* given by Copperwheat et al. (2011), and a discussion on the subtleties of modelling eclipsing AM CVn light curves, we refer the reader to Green et al. (2018a).

The basic model is a spherical white dwarf with a dark, Roche lobe filling donor. The free parameters for this model are the inclination (i), mass ratio (q , which sets the radius of the donor, r_2), scaled radius of the accreting white dwarf (r_1), the mid-eclipse time (t_0), and the velocity scale ($[K_1 + K_2]/\sin i$), with $K_{1,2}$ the observable

radial velocity amplitude. We fixed the temperature of the white dwarf to the values obtained from the fit to the spectral energy distribution (SED) (Section 6.3). We set the donor temperature to 2000 K, which in practice means that the donor does not contribute to the model light curve. We fixed the orbital period to the period derived from the ZTF data (see Section 5.1). Limb darkening of the white dwarf is approximated by using the four-parameter Claret law (Claret & Bloemen 2011) with the parameters taken from the DB models by Claret et al. (2020) for the closest temperature value and $\log(g) = 8.5$. In addition, we imposed two restrictions on the white dwarf radius using the approximation of the mass–radius relation of Eggleton from Rappaport, Putney & Verbunt (1989). The first is that it cannot be smaller than a zero-temperature white dwarf. The second is a Gaussian prior on the white dwarf radius relative to the white dwarf M–R relation with an uncertainty of 5 per cent.

The light curves show a range in contributions from the disc and bright-spot, and, therefore, we use different model configurations and free parameters for each of the AM CVn systems. At very long orbital periods, both the disc and bright-spot components do not contribute significantly to the light curve, as is the case for ZTFJ1637+49. This is supported by the fact that the eclipse depths are identical in each of the five HiPERCAM bands. We therefore use just the basic model without a disc or bright-spot to model the light curve. For ZTFJ0003+14 and ZTFJ0220+21, we include both a disc and a bright-spot in the model to account for any small amount of in-eclipse light. We use the same setup as in Green et al. (2018a) and keep most parameters fixed. The only two free parameters of the disc are the temperature (T_{disc}) and the outer radius (r_{disc}). For the bright-spot, we keep most parameters fixed to their default values. The only two free parameters of the bright-spot are the temperature (T_{spot}) and spot length (l_{spot}). We fix the spot position to the outer radius of the disc. For ZTFJ2252-05 and ZTFJ0407-00, we used a model with a disc with two free parameters (T_{disc} , r_{disc}) and used five free parameters for the spot; length, exponent, angle, yaw, temperature, and *cfrac* (again, see Green et al. 2018a for a description of each parameter). We again fixed the bright-spot location to the outer edge of the disc.

⁷<https://github.com/trmrsh/cpp-lcurve>

Table 2. The orbital period and mid-eclipse times as measured from the ZTF and archival photometry.

Name	t_0 (BJD _{TDB})	Period (d)
ZTFJ1637+49	2458370.73498(4)	0.042 707 771(8)
ZTFJ0003+14	2458323.02453(1)	0.038 564 45(8)
ZTFJ0220+21	2458428.74931(8)	0.037 041 443(2)
ZTFJ2252-05	2458469.64845(7)	0.025 968 133 6(9)
ZTFJ0407-00	2458386.99699(2)	0.024 588 123(3)

To find the best parameter values and uncertainties, we use a Markov chain Monte Carlo method as implemented in *emcee*. Before fitting the data, we removed long time-scale trend by fitting a polynomial to the individual light curves. For the two short-period systems, we removed any remaining flickering using Gaussian process regression, using a 3/2 Matern Kernel. Finally, we rescaled the uncertainties in the light curves so that they account for any remaining difference between the data and the model. For each light curve, we use 512 walkers and at least 2000 generations to determine the best-fitting model and the uncertainties on the parameters.

6 RESULTS

6.1 Ephemerii

The mid-eclipse ephemerii are given in Table 2. The combination of archival data that spans a long-baseline and accurate eclipse time

measurements means that the periods can be constrained to $\approx 10^{-8}$ d or better, and the zero-point to a few seconds. We did not detect any significant deviations from the eclipse arrival time, except for system for ZTFJ0407-00. More data are needed to verify these eclipse arrival time variations and determine their nature, which will be the topic of future work.

6.2 Doppler maps

The Doppler maps are shown in Fig. 7. All systems show a clear disc in the Doppler maps. The size of the disc increases slightly as the orbital decreases and the velocities of the components increase. ZTFJ1637+49 and ZTFJ0220+21 (with the best data) show a bright-spot at the top of the figure, and possibly a secondary bright-spot at the lower right of the map, also seen in Gaia14ae (Green et al. 2020). ‘Central spike’ emission is clearly visible for ZTFJ1637+49, which originates from the white dwarf (Kupfer et al. 2016; Green et al. 2020). The other Doppler maps are less clear, but all seem to show brighter parts in the disc that are consistent with bright-spots.

6.3 Spectral energy distribution and white dwarf temperature

The spectral energy distributions are shown in Fig. 8. Also shown are the best-fitting white dwarf models (see Section 5.3) and the white dwarf temperatures as reported in Table 3. In general, the models agree well with the data but do show some inconsistencies at extreme wavelengths. For shortest period systems, a far-ultraviolet (FUV) measurement is available and the model underestimates the

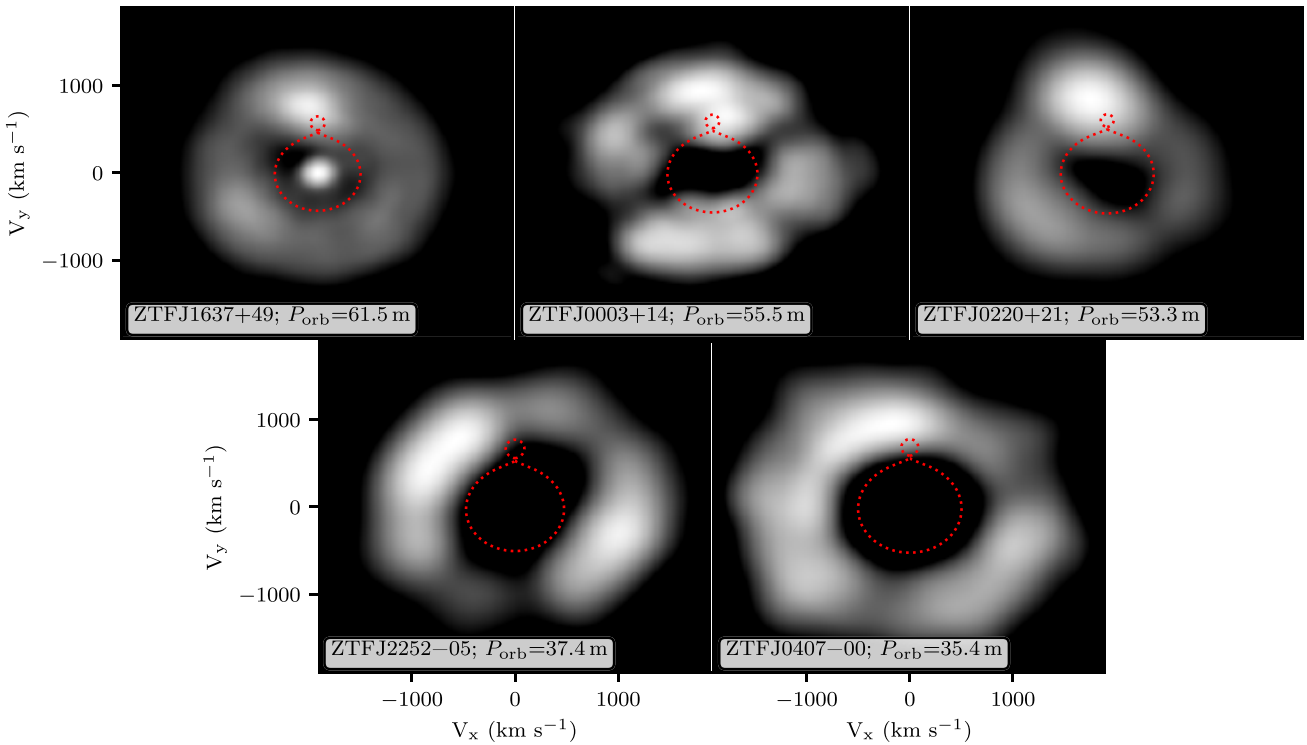


Figure 7. Doppler maps of the five eclipsing AM CVn systems. For ZTFJ1637+49, ZTFJ0220+21, and ZTFJ0407-00, we used spectra from the LRIS red arm, and for ZTFJ0003+14 and ZTFJ2252-05, we used spectra from the LRIS blue arm. Red dashed lines show the Roche lobes of the binary system, with the white dwarf located in the centre of the image and the donor (with the small Roche lobe) on top. In this coordinate system, the accretion flow originates at the top of the donor. ZTFJ1637+49 shows emission from the white dwarf (the ‘central spike’). The primary bright-spots are visible at the top or top left of the figure for all systems. ZTFJ1637+49 and ZTFJ0220+21 show possible secondary spots at the bottom left, and ZTFJ2252-05 shows a possible secondary spot at the bottom right. The structure in the map of ZTFJ0003+14 is caused by the sparse sampling.

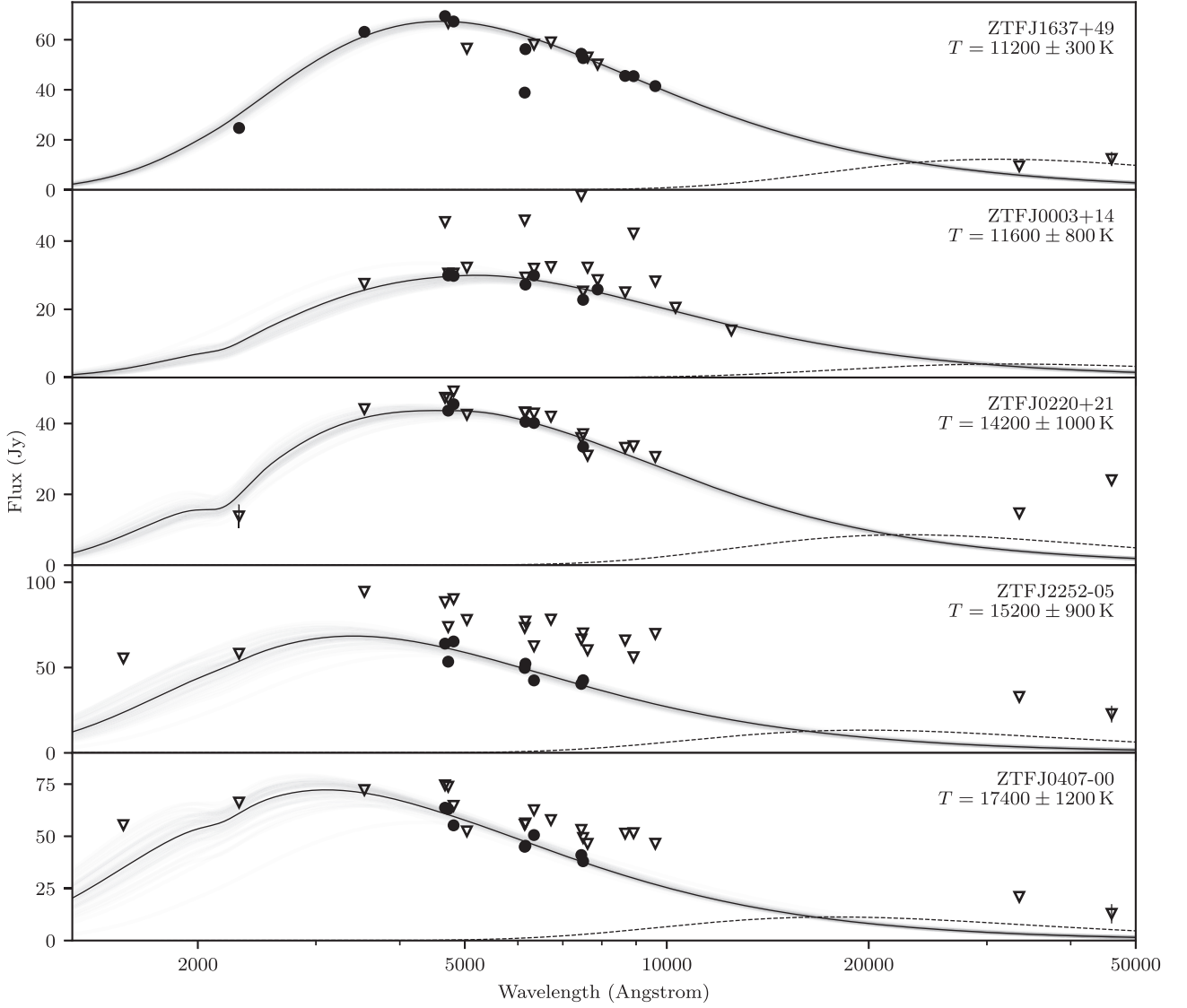


Figure 8. The SED of each system, showing *Galex*, SDSS, PS, median ZTF, UKIDSS, and *WISE* data. Triangles show *observed* flux measurements, which were used as upper limits in the fit. Filled dots show the estimated flux by the white dwarf by removing the contributions from the disc and bright-spot (Table 4). Error bars are omitted if they are smaller than the symbol size. We fitted the data with a blackbody in order to measure the white dwarf temperature (black line). Grey lines show the uncertainty in the fit. The dashed line shows the expected contribution from the donor star if we assume an equilibrium temperature that is set by irradiation from the white dwarf. For ZTFJ1637+49, the correction of the observed flux is assumed to be 0.

Table 3. Binary parameters of all well-characterized eclipsing AM CVn systems. The five ZTF systems are from this work, parameters of Gaia14aae are from Green et al. (2018a), and parameters of YZ LMi are from Copperwheat et al. (2011). In each case, we have used the results based on modelling of the *g*-band light curve, which is the most accurate in all cases.

	P min	q	i deg	T_1 kK	M_1 M_\odot	M_2 M_\odot	R_1 R_\odot	R_2 R_\odot
ZTFJ1637+49	61.5	0.026 ± 0.010	82.7 ± 0.09	11.2 ± 0.3	0.90 ± 0.05	0.023 ± 0.008	0.009 ± 0.001	0.068 ± 0.007
ZTFJ0003+14	55.5	0.0214 ± 0.010	86.5 ± 2.0	11.6 ± 0.8	0.79 ± 0.11	0.017 ± 0.011	0.0106 ± 0.001	0.057 ± 0.012
ZTFJ0220+21	53.5	0.0174 ± 0.005	85.3 ± 2.1	14.2 ± 1.0	0.83 ± 0.07	0.014 ± 0.006	0.010 ± 0.001	0.054 ± 0.007
Gaia14aae	49.7	0.0290 ± 0.0006	86.27 ± 0.10	17.0 ± 1.0	0.872 ± 0.007	0.0253 ± 0.0007	0.00924 ± 0.00009	0.0603 ± 0.0003
ZTFJ2252-05	37.4	0.034 ± 0.006	87.0 ± 1.0	15.2 ± 0.9	0.76 ± 0.05	0.026 ± 0.008	0.010 ± 0.001	0.049 ± 0.004
ZTFJ0407-00	35.4	0.024 ± 0.004	86.5 ± 0.7	17.4 ± 1.2	0.79 ± 0.06	0.019 ± 0.003	0.010 ± 0.001	0.044 ± 0.002
YZ LMi	28.3	0.041 ± 0.002	82.6 ± 0.3	17.0 ± 1.0	0.85 ± 0.04	0.035 ± 0.003	–	0.047 ± 0.001

FUV flux in both cases. This is possibly due to emission from the accretion disc but could also be due to the blackbody assumption.

The flux in the *WISE* bands, which were not used to fit the model, are also underestimated in all cases. To check if this would be consistent with emission from the donor, we calculated the donor equilibrium temperature based on irradiation by the white dwarf. This suggests that the excess in the far-IR for ZTFJ1637+49 could be by the donor (see also Green et al. 2020). For the other objects, the estimated contribution by the donor is insufficient to explain the excess light, and the disc is the more likely source of the IR excess.

6.4 Long time-scale variability

We inspected the ZTF and archival data to study the long time-scale behaviour of the AM CVn systems. As expected, the long-period systems, ZTFJ1637+49, ZTFJ0003+14, and ZTFJ0220+21, do not show any outburst or other long time-scale variability in the ZTF data or the other archival data that span a decade or more. For ZTFJ0003+14, only ZTF data are available that span 3 yr, and no outbursts or trends are visible. We do note that the source is ≈ 0.6 -mag brighter in SDSS compared to ZTF and Pan-STARRS data. ZTFJ0003+14 likely showed an outburst, and SDSS observed it while it was on its way back to quiescence.

Both ZTFJ2252-05 and ZTFJ0407-00 do show variability on longer time-scales, shown in Fig. 9. ZTFJ2252-05 shows low-level variability in the light curve (besides the eclipse) but no clear overall trends. Only two outbursts have been detected, one by CRTS and one by ASAS-SN, both reaching magnitude 16. The light curves are not sampled well enough to make any statement on the duration of the outbursts.

ZTFJ0407-00 also shows variability on longer time-scales. No outbursts have been detected by SDSS, CRTS, Pan-STARRS, or PTF. The ZTF and ASAS-SN data obtained in the last 3 yr show two (possibly three) high-amplitude outbursts that last multiple days. As can be seen in the middle panel of Fig. 9 for ZTFJ0407-00, the quiescence luminosity increased after the last superoutburst by about 0.6 magnitudes and is slowly decreasing. This system shows at least four short-duration (< 1 d) outbursts.

6.5 Binary parameters

The light curves and their best-fitting models are shown in Figs 2–6, and the best-fitting parameters and uncertainties can be found in the online materials. An overview of the binary parameters is given in Table 3, and Table 4 lists the contribution of each component to the overall luminosity. We first discuss the overall results and discuss the result for each object individually at the end of this section.

As expected and can be seen in Table 4, the relative contribution by the disc and bright-spot increases with decreasing orbital periods. In general, for the long-period systems (ZTFJ1637+49, ZTFJ0003+14, and ZTFJ0220+21), the bright-spot is not detected. However, the *r*-band models for ZTFJ0003+14 and ZTFJ0220+21 do include a significant contribution by the bright-spot. Since this feature is not seen in the other bands, we expect that this is due to some asymmetry in the light curve caused by residual flickering, and the additional light is actually from the disc. For the two short-period systems (ZTFJ2252-05 and ZTFJ0407-00), there seems to be a detection of the bright-spot eclipse. However, this is a subtle feature in the light curve. The bright-spot eclipses for ZTFJ0407-00 but only marginally for ZTFJ2252-05. We note that the contribution from the disc is largest for ZTFJ2252-05 despite having a longer orbital period than ZTFJ0407-00. We discuss this further in Section 7.2.

Table 3 shows the binary parameters as derived from the light-curve modelling. The main source of uncertainty is the degeneracy between q and i (Green et al. 2018b). For a light curve with where only the primary eclipse is detected, q and i are fully degenerate. This degeneracy can be lifted with additional features in the light curve by measuring either the bright-spot eclipse or the eclipse shape, which is set by a combination of the limb darkening of the white dwarf and the white dwarf mass–radius relation used.⁸ As we have discussed above, only ZTFJ0407-00 shows a clear detection of the bright-spot eclipse. Therefore, the uncertainty on the mass ratio is high for the other systems, up to ≈ 50 per cent is the worst case (ZTFJ0003+14). Correspondingly, the uncertainties on the inclinations are 0.5–2 degrees. The uncertainties on the other physical parameters are mostly due to this uncertainty in the inclination. We do note that of the five systems, ZTFJ1637+49 has been best constrained on the inclination despite showing only a grazing eclipse. This can be explained by the lack of any disc or bright-spot and the high-quality *g*-band data.

6.5.1 ZTFJ1637+49

The models for ZTFJ1637+49 agree well with the data for each of the colour bands and do not show any systematic deviations. This justifies the use of a model with only the accretor and donor, without any contribution from a disc or bright-spot.

The best-fitting parameters consistently indicate that the inclination is 82.8 ± 1.1 degrees, which is expected for a grazing eclipse. Inspection of the posteriors shows that q and i are strongly correlated (as expected). The mass ratio (q) is 0.025 ± 0.001 . The results are consistent between bands.

The derived binary parameters (masses and radii) are all consistent between bands. The *g*-band results are the most accurate and we use these in the rest of the paper. The mass of the white dwarf is $M_1 = 0.90 \pm 0.05 M_\odot$. The donor has a mass of $M_2 = 0.023 M_\odot$ and radius of $R_2 = 0.068 \pm 0.007 R_\odot$.

6.5.2 ZTFJ0003+14

The fit to the light curves of ZTFJ0003+14 is good and no discrepancies can be seen. The best-fitting models indicate that almost no light is visible when the system is in eclipse. The parameter estimates for the *g* and *i* band are consistent with each other, but the *r*-band parameters differ. This is possibly because the *r*-band model has a 7 per cent contribution from the bright-spot, while the *g* and *i* models attribute any additional light to the disc. This is likely due to some residual systematics in the *r*-band data. Taking this and the data quality into account, we conclude that the *g*-band solution is the most accurate and precise.

As is the case with ZTFJ1637+49, with just a white dwarf eclipse and no additional information, there is a degeneracy between i and q , which are both poorly constrained; $i = 86.5 \pm 2.0$ and $q = 0.0214^{+0.016}_{-0.007}$, which results in relatively poor constraints on the mass and the radius. The mass of the white dwarf is $M_1 = 0.79^{+0.13}_{-0.10} M_\odot$. The donor has a mass of $M_2 = 0.0165^{+0.018}_{-0.006} M_\odot$ and radius of $R_2 = 0.068 \pm 0.007 R_\odot$.

⁸A radial velocity semi-amplitude measurement or surface gravity measurement would also work.

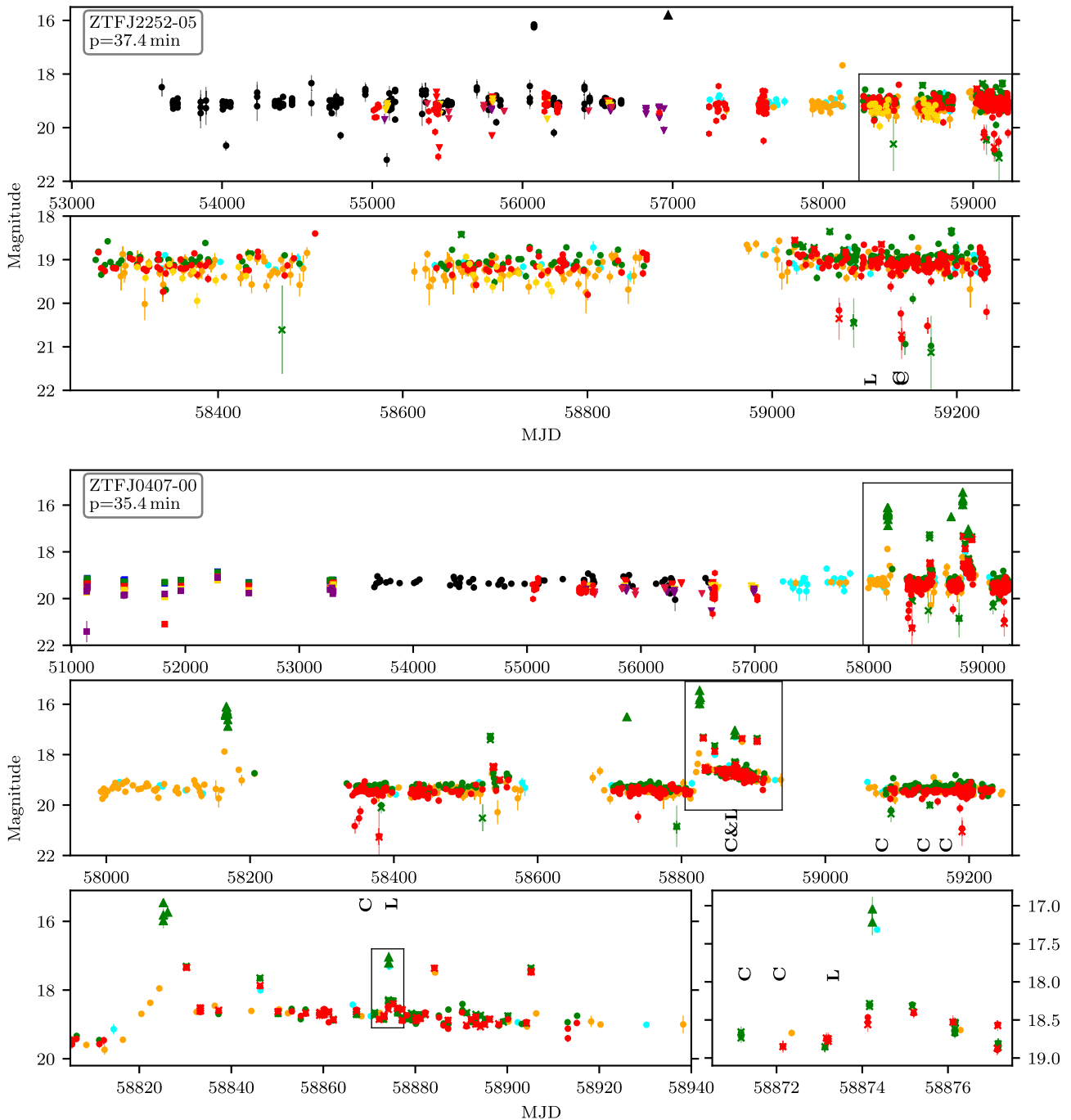


Figure 9. The light curves of the two shortest period systems ZTFJ2252-05 (top) and ZTFJ0407-00 (bottom). The consecutive panels show an increasingly zoomed-in range, indicated by black boxes in the previous panels. The figures show photometry from SDSS (squares), CRTS (dots), PTF (hexagons), ASAS-SN (triangles), and ZTF data (PSF photometry as dots and alerts as crosses). The *ugriz* filters are shown in blue, red, green, yellow, and purple; *V*-band observations are shown in black. ‘C’ and ‘L’ indicate when Chimera and LRIS data were obtained. ZTFJ2252-05: Two outbursts were detected by CRTS and ASAS-SN, 3 yr apart. No other outbursts can be seen in the rest of the data, including well-sampled ATLAS and ZTF data of the last 5 yr. ZTFJ0407-00: No outbursts or long time-scale variability can be identified in the SDSS, CRTS, and PTF data. The ATLAS cyan and orange filter data are shown in cyan and orange dots, with the data binned into 1-d bins. The middle panel shows ZTF and ASAS-SN data from 2017 to 2020, which shows two large-amplitude, multiday long outbursts. The bottom panel shows the most recent data, which shows four short-duration ($\lesssim 1$ d) outbursts that occur very shortly after a superoutburst. These echo outbursts have also been seen in other AM CVn systems (e.g. Green et al. 2020; Duffy et al. 2021; Pichardo Marcano et al. 2021).

6.5.3 ZTFJ0220+21

Models for ZTFJ0220 + 21 agree well with the data and do not show any variability that the models do not account for. We note that in all light curves, the eclipse is not consistent with zero, and

up to 10 percent of the light is emitted by the disc and/or spot. Similar as for ZTFJ0003+14, the *r*-band model does model some contribution by the bright-spot, but the *g* and *i* models do not include any contribution from the bright-spot. Again, this is likely due to systematics in the data.

Table 4. The contribution to the overall luminosity of white dwarf, disc, and bright-spot in the *gri* filter for the best-fitting models. The white dwarf is typically dominant for long-period systems and at shorter wavelengths, while the disc contributes more at short orbital periods and longer wavelengths. Interesting to note is that the disc is more prominent in ZTFJ2252-05 than in ZTFJ0407-00 despite having a slightly longer orbital period. At long periods and with low-signal-to-noise (SNR) data, there can be some degeneracy between the disc and the bright-spot. For the *r*-band model of ZTFJ0003+14 and ZTFJ0220+21, no light from the disc is modelled but instead, the bright-spot contributed 7% of the light. We suspect that this is due to minor systematics in the data and that the 7% contribution of light is actually from the disc.

	WD			Disc			Bright-spot		
	<i>g</i>	<i>r</i>	<i>i</i>	<i>g</i>	<i>r</i>	<i>i</i>	<i>g</i>	<i>r</i>	<i>i</i>
ZTFJ1637+49	100%	100%	100%	–	–	–	–	–	–
ZTFJ0003+14	97%	93%	89%	3%	0%	11%	0%	7%	0%
ZTFJ0220+21	92%	93%	89%	8%	0%	10%	0%	7%	0%
ZTFJ2252-05	65%	58%	46%	27%	36%	51%	7%	5%	3%
ZTFJ0407-00	82%	75%	70%	13%	16%	22%	5%	9%	8%

The parameter estimates between bands deviate significantly. The *g* and *r* bands roughly agree, but the *i*-band solution deviates significantly. It is skewed towards very high-inclination solutions and very low-mass ratios. A comparison between the models shows a different eclipse shape in the *i* band compared to the other two models. The difference is small but does seem to have an effect on the parameter estimates. The difference is possibly a result of the detrending process. Given that the quality of the *g*-data is best, we use this result in the rest of the paper.

As is the case for ZTFJ1637+49 and ZTFJ0003 + 14, the solution for ZTFJ0220+21 is also affected by a degeneracy between *i* and *q*. However, because of the abundance of *g*-band data, the parameters are better constrained compared to ZTFJ0003 + 14 $i = 85.3^{+0.8}_{-0.9}$ and $q = 0.018^{+0.007}_{-0.004}$. The mass of the white dwarf is $M_1 = 0.83^{+0.07}_{-0.08} M_\odot$. The donor has a mass of $M_2 = 0.014^{+0.007}_{-0.005} M_\odot$ and radius of $R_2 = 0.054^{+0.008}_{-0.006} R_\odot$.

6.5.4 ZTFJ2252-05

This shorter period system shows significant variability out of eclipse. While we did detrend the data and combined a number of orbits, some correlated variability remains in the light curve. Besides this, the model is in good agreement with the data. In this system, the disc contribution is clearly visible as the slopes before and after the main eclipse by the white dwarf. There also seems to be some asymmetry present in the eclipse and it seems to be fainter at egress, which is likely the eclipse of the bright-spot. This is, however, at the same level as the residual flickering and might not be significant.

Estimates of the system parameters show roughly consistent between bands. For the sake of consistency, we adopt the *g*-band results in the rest of the paper. Because there is no significant detection of the bright-spot eclipse, there is still a strong degeneracy between *q* and *i*. The inclination and mass ratio are $i = 87.0^{+0.5}_{-1.5}$ and $q = 0.030^{+0.002}_{-0.003}$. The mass of the white dwarf is $M_1 = 0.76^{+0.05}_{-0.04} M_\odot$. The donor has a mass of $M_2 = 0.026^{+0.010}_{-0.002} M_\odot$ and radius of $R_2 = 0.049^{+0.006}_{-0.002} R_\odot$.

6.5.5 ZTFJ0407-00

This system has an orbital period very similar to ZTFJ2252-05 but does not show as much flickering and has a smaller contribution to the luminosity by the disc (Table 4). The contribution by the bright-spot is more significant and can be seen by the broad ‘hump’, which peaks at phase ≈ 0.8 . In addition, there is also a possible contribution by a ‘superhump’ that causes a peak in the light curve at phase 0.2 (also seen in YZ Lmi, see Copperwheat et al. 2011). In this system, the

bright-spot eclipse is clearly visible (at phase 0.02–0.08) as shown by the inset.

The parameter estimates from the *g* and *i* bands both agree, but the *r*-band result indicates a lower inclination and higher mass ratio. There is no obvious difference between light curves. Comparing the models, there is a subtle difference between the duration of the eclipse between bands. This could be the result of the flickering and/or the detrending process. We again adopt the *g*-band solution for the rest of the paper, as it is deemed the most reliable, given the highest SNR and largest amount of data available.

The inclination and mass ratio are $i = 86.5^{+0.8}_{-0.5}$ and $q = 0.024^{+0.003}_{-0.004}$. The mass of the white dwarf is $M_1 = 0.79^{+0.04}_{-0.05} M_\odot$. The donor has a mass of $M_2 = 0.019^{+0.003}_{-0.004} M_\odot$ and radius of $R_2 = 0.044^{+0.002}_{-0.003} R_\odot$.

6.6 The average spectra and spectral lines

Spectra of AM CVn systems are a combination of light from the white dwarf, the disc, the bright-spot, and sometimes a boundary layer on the interface between the disc and the white dwarf (e.g. Kupfer et al. 2015). The donor is cold and not visible. For systems in quiescence, the overall shape of the spectral energy distribution is set by the continuum of the white dwarf. The bright-spot is small but hot and is sometimes seen as excess UV emission.

In quiescence, the disc is optically thin and appears as emission lines. If the system is viewed near edge-on, the lines are double-peaked. In GP Com (Smak 1975; Morales-Rueda et al. 2003; Kupfer et al. 2016) and other systems, a single-peaked emission line is also visible in the centre of many double-peaked He lines, dubbed the ‘central spike’. Radial velocity measurements show that these lines originate from the white dwarf (Marsh 1999; Roelofs et al. 2005; Kupfer et al. 2015) and are likely boundary layer emission from the surface of the white dwarf (e.g. Gehron et al. 2014; Green et al. 2019a).

In some cases, absorption lines of metals are present in the spectra of AM CVn systems (Groot et al. 2001; Anderson et al. 2008; Kupfer et al. 2016). Radial velocity shifts of absorption lines are consistent with that of the white dwarf (Kupfer et al. 2016; Green et al. 2020), which confirms that these lines are formed in the atmosphere of the white dwarf.

The average spectra are shown in Fig. 10, and the spectral lines are listed in Table 5. To identify the lines, we systematically searched the spectra element by element and checked for the presence of spectral lines. First, we confirmed that no hydrogen lines are present.

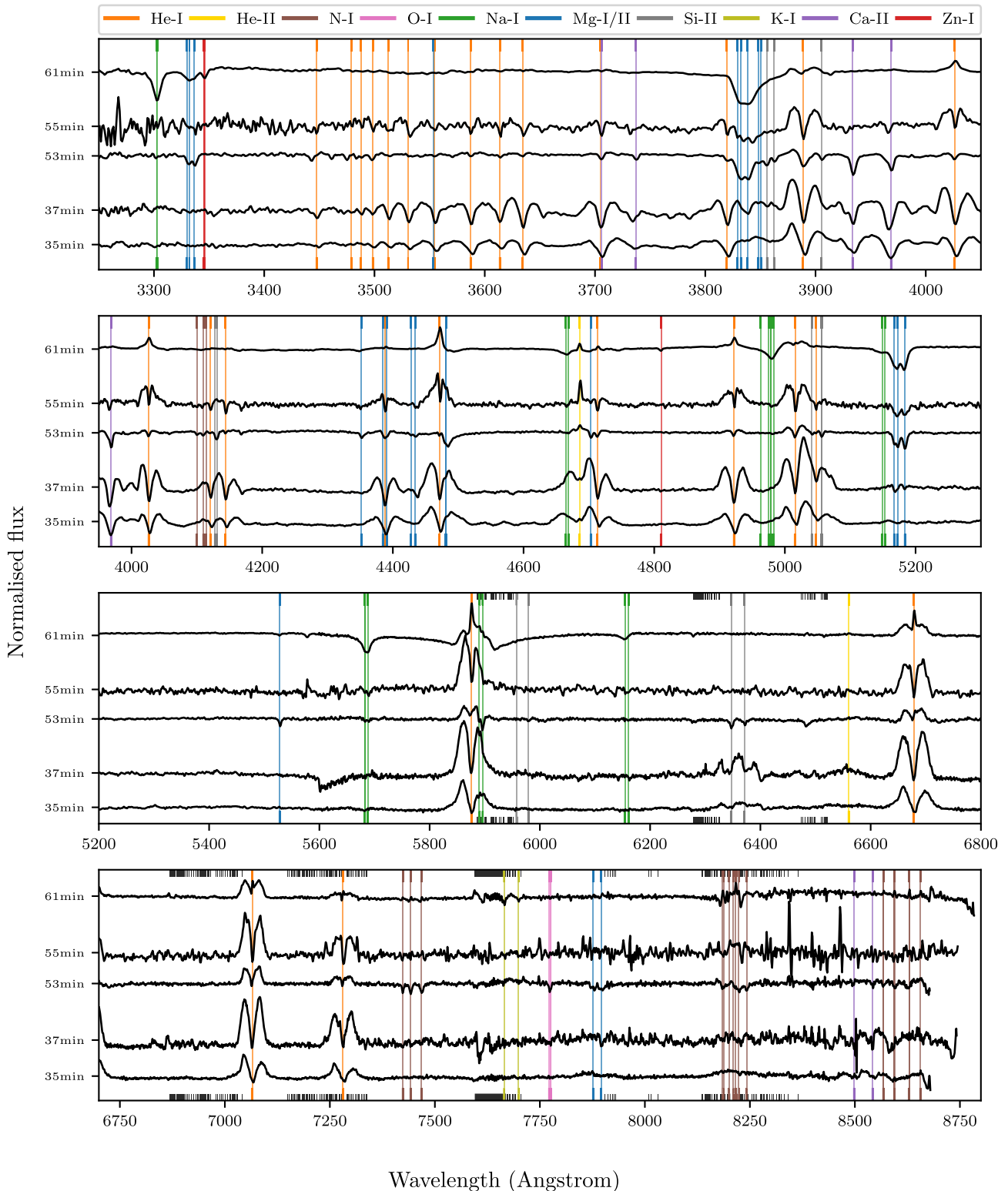


Figure 10. The averaged and normalized LRIS spectra of ZTFJ1637+49, ZTFJ0003+14, ZTFJ0220+21, ZTFJ2252-05, and ZTFJ0407-00 from top to bottom, labelled by their orbital periods. The spectra have only been shifted and have not been re-scaled. The different absorption and emission lines are indicated by coloured vertical lines, and telluric lines are indicated with black ticks at the top and the bottom.

We continued with He-I lines, which are found both in emission (as double peaks) and absorption in all spectra. ZTFJ1637+49 also shows a strong ‘central spike’ component. He-II is also present in all spectra as a small but significant emission line, which is also likely a

‘central spike’. There also seems to be some double-peaked emission from He-II, but other lines close to He-II-4686 Å make this hard to determine with certainty. ZTFJ0003+14 is an exception and shows a strong emission line at He-II-4686 Å.

Table 5. List of elements identified from emission and absorption lines in the averaged LRIS spectra (see Fig. 10). ‘e’ indicates emission lines, ‘de’ indicates double-peaked emission lines, and ‘a’ for absorption lines.

	ZTFJ1637+49	ZTFJ0003+14	ZTFJ0220+21	ZTFJ2252-05	ZTFJ0407-00
He-I	e, de	e	de	de	de
He-II	e	e	e	de	de
N-I	e, a		a	a?	a?
O-I			a		
Na-I	a, e?		a	a	a?
Mg-I	a	a	a	a	a?
Mg-II			a		a?
Si-I			a	de	de
K-I	a				
Ca-II			a	a	a
Zn-I	a				

We continued the search with the CNO elements. N-I lines are in emission in the spectra of ZTFJ1637+49 and absorption for ZTFJ0220+21. The spectrum of ZTFJ0407-00 seems to show a broad emission feature consistent with emission from the N-I multiplet at 8223 Å (for an overview of N lines, see Kupfer et al. 2017). There are also some hints of emission lines by N-I around 8680 Å. There is no clear detection of N-I in the spectra of ZTFJ0003+14 and ZTFJ2252-05, possibly because the SNR of these spectra is lower. Oxygen is clearly detected in ZTFJ0220+21: there is a clear detection of an absorption feature at 7772/4/5 Å. This feature is not detected in the other spectra. We found no carbon lines in any of the spectra, which has implications on the nature of the donor star (see Section 7.3).

Next, we searched for the presence of metal lines in the spectra. Both Na-I and Mg-I/II are detected as absorption lines. Mg-I can be seen in the triplets at 3832 Å and 5172 Å. They are strongest for the long-period system and decrease in strength for the short-period systems. Mg-II lines are weaker but can be seen at 4481 Å and possibly at 4384/90. Na-I lines are especially strong in ZTFJ1637+49 but barely detectable in the other spectra (3302/3, 5682/8, 6154/60, and 5889/95 Å). Ca-II lines (3933/68 Å and also 3706/36 Å) are seen for ZTFJ0003+14, ZTFJ0220 + 21, ZTFJ2252-05, and ZTFJ0407-00, but not for ZTFJ1637+49. Finally, ZTFJ0220+21, ZTFJ2252-05, and ZTFJ0407-00 all show Si-II lines in their spectra: as double-peaked emission lines (6347/71 Å) for the two short-period systems, and as absorption lines for ZTFJ0220+21. There are also lines visible at 3856/62 Å for ZTFJ0220 + 21 and ZTFJ2252-05. No Si-II is visible for ZTFJ1637+49 and ZTFJ0003+14.

There are a few rare elements present. In ZTFJ1637+49, two Zn-I absorption lines can be seen (3345 Å and 4810 Å). In addition, there are two lines present (7665/95 Å) in ZTFJ1637+49, which are consistent with the strongest two K-I lines. We do note that these are located close to telluric absorption lines.

7 DISCUSSION

7.1 Search for eclipsing AM CVn binaries

7.1.1 Recovery efficiency and space density

Gaia has measured a parallax for all seven eclipsing AM CVn systems, and the distance is known with a precision of 5 per cent to 30 per cent. With a sample size of 5 (and two previously known eclipsing AM CVn systems), only an order of magnitude estimate of the local space density is possible. However, there is a two order of

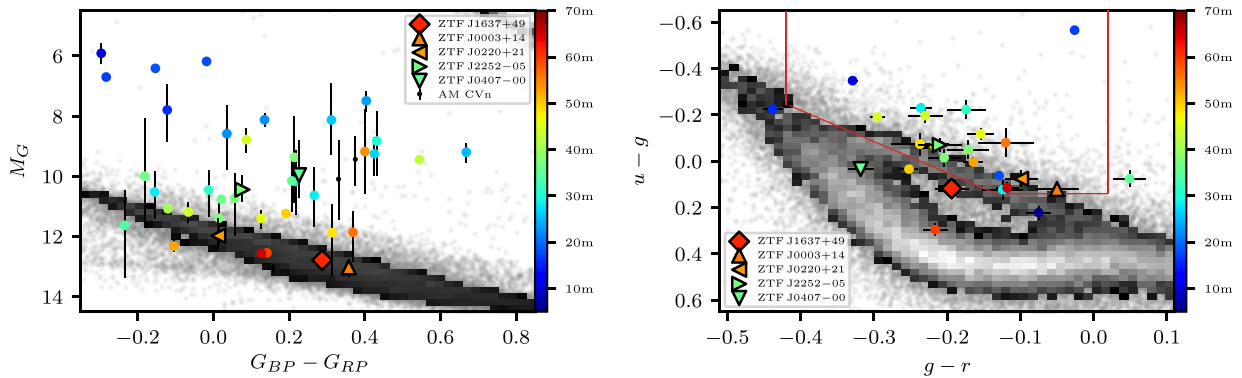
magnitude difference between the predicted AM CVn space density (Nelemans et al. 2001; Kremer et al. 2017) and the measured space density by Carter et al. (2013a), and it is therefore useful to check if the yield is consistent with the measured space density to exclude the possibility of a previously missed population. In addition, an estimate of the recovery efficiency is useful to estimate how many systems ZTF and other surveys are set to discover in the near future.

We have carried out a very thorough search of objects in the white dwarfs catalogue by Gentile Fusillo et al. (2019), and limit the discussion on the completeness of our search to only objects in this catalogue. Of the seven known eclipsing AM CVn systems, only ZTFJ2252-05 is not in this catalogue, and we therefore exclude it in this estimate. Both already known eclipsing AM CVn systems, Gaia14aae and YZ Lmi, are part of this catalogue. We recovered Gaia14aae in our search, but we initially did not recover YZ Lmi because its orbital period is just short of the initial cutoff of 28.8 min (0.02 d). Therefore, we searched all light curves with one or more alerts again but now down to periods of 14.4-min (0.01 d) days and did recover YZ Lmi with the correct period, but no other systems were found.

A total of 241 775 objects in this sample have ZTF light curves with more than 80 epochs (49.6 per cent of the total catalogue). To estimate the recovery efficiency for each object, we assume that if there are five to seven or more in-eclipse points in the light curve, we are able to identify the source as an eclipsing AM CVn system. This can be easily calculated as it is just a function of the total number of epochs in the light curve and the eclipse duty cycle (see Appendix A).

We estimate the eclipse duty cycle for each system and calculate the average probability to recover them from the 241 775 ZTF light curves. The average recovery efficiencies are 33 per cent for ZTFJ1637+49 and 60–75 per cent for the other systems (including Gaia14aae and YZ Lmi). This suggests that there are ≈ 1 –4 eclipsing systems we have not detected, which do have ZTF light curves and another 6–10 outside of the ZTF footprint.

In order to estimate the space density, we use the basic $1/V_{\max}$ method (Schmidt 1968), with distances from Bailer-Jones et al. (2021) (see Table 1). Since the AM CVn systems are very close, we do not correct for expected changes in the space density and assume a uniform distribution. We use the *Gaia* parallax and a magnitude limit of 20.5 to estimate the total volume each of the systems could have been recovered. We correct this estimate by the recovery efficiency we estimated earlier, a correction for the fraction of systems not in the ZTF footprint, and a correction factor of 8 (the average correction factor to account for eclipsing Roche lobe filling binaries with mass ratios between $0.01 < q < 0.05$). This



(a) The *Gaia* observational H-R diagram (eDR3) with as background stars within 200 pc.

(b) The SDSS $u - g$ versus $g - r$, colour-colour diagram of the white dwarf catalog (Gentile Fusillo et al. 2019). The red line shows the colour-selection used by Carter et al. (2013a).

Figure 11. The new eclipsing systems compared to known AM CVn systems in the HR-diagram and colour-colour diagram. The newly discovered eclipsing systems are shown as triangles and a diamond and the known AM CVn systems as dots. The marker colour indicates the orbital period of the system. Note that we corrected the SDSS measurements for ZTFJ1637+49 and ZTFJ0003+14 that were obtained in-eclipse. In Section 7.1.2, we discuss why these systems were not identified as AM CVn systems earlier and the implications for future searches based on colours and parallaxes.

results in an estimated space density of $\rho = 6_{-2}^{+6} \times 10^{-7} \text{ pc}^{-3}$. This is consistent with the measured space density by Carter et al. (2013a), $\rho = 5 \pm 3 \times 10^{-7} \text{ pc}^{-3}$, and again confirms the discrepancy with the population synthesis predictions (e.g. Nelemans et al. 2001). With this search, we exclude the possibility that this discrepancy is due to a large hidden population of faint, low accretion rate AM CVn systems.

7.1.2 Observational properties compared with the known population of AM CVn systems

The currently known sample of AM CVn binaries has been found by various searches based on static colours, outbursts, short periods variability, or by large spectroscopic surveys. These search methods have different inherent biases. Here, we briefly discuss the biases of each method and compare them to the search for AM CVn system using eclipses.

Searches for outbursting AM CVn (e.g. Levitan et al. 2015) will predominantly find systems with periods between 22 and ~ 50 min. A search based on SDSS colours by Carter et al. (2013a) has mostly found AM CVn systems with intermediate periods as well. These systems stand out because their colour is a combination of a DB white dwarf and some contribution by a disc. Shorter period systems (direct impact accretion systems) are easy to find because of their high X-ray luminosity but these are intrinsically rare due to the fast evolution. Large-scale spectroscopic surveys allow for the discovery of systems at all periods (e.g. Anderson et al. 2005). Therefore, most of the long-period ($\gtrsim 50$ min) systems have been discovered using SDSS spectra.

A search for AM CVn systems by their eclipses has very different biases. It is biased towards high inclination systems. Secondly, systems with deep eclipses are easier to detect than shallow eclipses (assuming an efficient pipeline that can handle ‘dropout’). Eclipses are more shallow for short-period systems where the disc or the bright-spot dominates the luminosity. However, short-period systems can show strong superhump periods, which are close to the orbital period. If outbursts and flickering dominate the light curve, the period is more difficult to determine, which is an additional complicating factor. Eclipsing long-period systems are easy to find; the white dwarf dominates the luminosity, which means that the eclipses are deep. In conclusion, using eclipses to find AM CVn systems is biased to

low accretion rate and therefore long orbital periods. The eclipse probability does not decrease significantly with the orbital period since the donor size increases with the orbital period.

To determine why none of these eclipsing systems have been identified earlier as AM CVn systems, we plot the detected eclipsing AM CVn systems and the known sample in an HR diagram and a $u-g-g-r$ colour diagram (Fig. 11).

ZTFJ1637+49 and ZTFJ0220+21 are located on the white dwarf track in the HR diagram and close to the DB track in colour space. Both of these systems are dominated by the DB white dwarf, and light emitted from the disc or bright-spot is almost negligible. Both these systems appear as typical DB white dwarfs. ZTFJ0003+14 is very red and an outlier in both figures. This could be due to reddening ($E_{g-r} = 0.14$). In the HR diagram, it is located slightly above the white dwarf locus, which is expected, given the small contribution from a disc and the low temperature. ZTFJ2252-05 and ZTFJ0407-00 are located above the white dwarf track in the HR diagram, which suggests that the contribution by the disc and the bright-spot was small but not negligible when they were observed by *Gaia*.

In conclusion, finding short-period, non-eclipsing systems like ZTFJ2252-05 and ZTFJ0407-00 is easier because they stand out from the white dwarfs in the HR diagram. In addition, they also show outbursts and flickering. However, systems like ZTFJ1637+49, ZTFJ0003+14, and ZTFJ0220+21 do not stand out in either diagram and also do not show any outburst. If they are not eclipsing, the only solution is to obtain spectra of all white dwarfs and identify them by the He emission lines. Upcoming large spectroscopic surveys like SDSS-V (Kollmeier et al. 2017), 4MOST (de Jong et al. 2012), and WEAVE (Dalton et al. 2012, 2014; Dalton 2016) have programs to observe white dwarfs and will be able to find long-period AM CVn systems that are non-eclipsing.

We note that all five systems are in the SDSS footprint and have $ugriz$ colours, although none of them was found in the search for AM CVn systems using SDSS colours by Carter et al. (2013a) and Carter et al. (2014). ZTFJ1637+49 was observed during the eclipse, which mostly affected the r -band measurement and caused the system to be rejected as a candidate. ZTFJ0003+14 was in outburst when SDSS observed it, and the colours fall outside of the selection criteria (we used the Pan-STARRS g and r measurements in Fig. 11). The primary SDSS measurement of ZTFJ0407-00 also falls outside of the selection. However, it has been observed 14 times by SDSS, and only

two out of these 14 do not pass the selection criteria. ZTFJ0220 + 21 and ZTFJ2252-05 both pass the selection criteria, but no spectra were obtained; the spectroscopic completeness of Carter et al. (2013a) is 70 per cent. While the fact that none of these systems were found by Carter et al. (2013a) initially suggested that they underestimated their recovery efficiency, there is a plausible explanation for why all of these systems were not discovered. We conclude that the space density estimate by Carter et al. (2013a) is not significantly affected by any systematic bias or uncertainty.

7.2 Outbursts and accretion state

The overall trend for AM CVn systems is that the average accretion rate decreases with the orbital period. At orbital periods of 22 min and longer, the disc is generally in a low state with outbursts semiregularly. Levitan et al. (2015) showed that there is an exponential correlation ($\tau \propto P_{\text{orb}}^{7.35}$) between the orbital period and outburst frequency, with a super-outburst frequency of 1 yr at an orbital period of 34 min. The behaviour of the systems we found shows behaviour consistent with this correlation, with a few detected outbursts for the two short-period systems over the last decade and no detected outbursts for the longer period systems.

Because these systems are eclipsing, we can determine the relative luminosity of the disc and because the inclinations are similar also directly compare the spectra. Light-curve modelling shows that the relative contribution by the disc is ≈ 10 – 30 per cent for the short-period systems, just ≈ 5 per cent for the 50-min systems, and seems to be non-existent for the longest period system (see Table 4). A useful aspect of our sample is that there are two pairs of systems with almost identical periods. A direct comparison between the systems in each pair shows interesting differences. As can be seen in both the light curves and the spectra (Fig. 10), the contribution by the disc varies significantly between the members of each pair. This is possibly due to the recent outburst, which would empty the disc and heat the white dwarf, but could also be due to the more compact nature of the donor. Continued monitoring of the systems using high-speed photometry and high SNR light curves to more precisely measure the mass and radius of the donor (Green et al. 2018a) will enable us to resolve these issues.

For ZTFJ0407-00, we observe one outburst in the ZTF data, which showed multiple short ‘echo’ outbursts days to weeks after the main superoutburst, also seen by Green et al. (2020), Duffy et al. (2021), and Pichardo Marcano et al. (2021). Well-sampled light curves of the systems also show a brighter baseline level and up to 20 echo outbursts after a superoutburst. In the case of ZTFJ0407-00, we also observe a change in the eclipse depth; the eclipse is total in the ZTF data (see Fig. 1) but only 60 per cent deep in the Chimera data. These three observations suggest a change in the state of the system, possibly an increased temperature of the white dwarf, a brighter disc, or both.

Because ZTFJ0407-00 is eclipsing, we can potentially measure the changes in the systems more directly using the eclipses. By obtaining high-speed photometry before, during, and after a superoutburst, we can measure changes both in the white dwarf temperature and in the size and brightness of the disc (e.g. Copperwheat et al. 2011).

Besides the usual disc emission line, we note that a small but significant He-II-4686 Å central spike is detected. A high temperature is required to ionize helium, which suggests that there is a hot but small boundary layer in all five systems. This feature is also seen in other long-period systems (e.g. Kupfer et al. 2015) and speculate that this feature is present to some extent in all AM CVn systems, but they can be detected only with high SNR spectra.

7.3 The properties of the donor stars

7.3.1 Chemical composition

The spectra show many different spectral lines, see Fig. 10 and Table 5. Modelling the spectra to determine elemental abundances is challenging and beyond the scope of this paper. We limit this discussion to qualitative estimates only.

Nelemans et al. (2010) showed that abundances can be used to determine the evolutionary channel the donor formed through. First, the presence of any hydrogen unambiguously points to an evolved main-sequence donor (e.g. Breedts et al. 2014; Green et al. 2020). We do not detect any hydrogen in the spectra of any of the systems. Since even a trace amount of hydrogen should be visible in the spectra, we conclude that none of the systems are formed through the ‘evolved’ CV channel.

When the donors have experienced significant helium burning, as is the case for helium star donors, the N abundance decreases to almost undetectable levels. Detailed helium star models for the donor stars in AM CVn systems predict typical surface abundance ratios N/C = 0.001–1 while for white dwarf donor stars N/C ≈ 0.1 if no CNO burning took place, or N/C $\gg 1$ if CNO burning did take place.

We have detected N in both ZTFJ1637+49 and ZTFJ0220+21 and do not detect any C. This is typical for many AM CVn systems and suggests that these systems are formed through the He-WD model.

In ZTFJ0220+21, we also detect oxygen, which suggests an O/N ≈ 1 . The O/N ratio in the WD model is set by the progenitor mass. Models by Nelemans et al. (2010) predict a ratio of O/N of close to 1 for a $1 M_{\odot}$ progenitor mass and an O/N ratio of 0.1 for a $2 M_{\odot}$ initial mass. This suggests that ZTFJ1637+49 evolved from WD donor with a higher initial mass, while ZTFJ0220+21 evolved from a lower initial mass WD donor.

For systems ZTFJ0003+14, ZTFJ2252-05, and ZTFJ0407-00, there is no clear detection of N lines, which makes any inference of the formation channel impossible.

Besides the CNO lines, we also observe a variety of metal absorption lines. The line strengths depend on the element in question and a combination of sedimentation time-scales (Koester 2009), temperature, surface gravity, accretion rate, and abundances of the accreted material.

The expectation is that the abundances of metals are primordial. However, sedimentation and mixing during the donor star lifetime affect the current abundance of metals. We have measured the temperature and surface gravity of the white dwarf, and by modelling the spectra using atmosphere models, we can in principle constrain the abundance of the metals but this is beyond the scope of this paper. This can shed light on both the primordial abundance in these systems as well as constrain the amount of sedimentation and/or mixing that took place during the formation of these systems.

7.3.2 Mass and radius

Fig. 12 shows the mass and radius of the donors in eclipsing AM CVn systems and four AM CVn systems for which the mass ratio has been measured using spectroscopy (Green et al. 2018a). Because the donor is filling its Roche lobe, the density of the donor depends only on the orbital period, indicated by diagonal lines in the figure (Faulkner, Flannery & Warner 1972; Green et al. 2020). Donors lose mass as the orbital period of AM CVn systems increase and evolve from right to left in this diagram. The WD and He-star donors are degenerate, and they increase in size as they lose mass.

The donor models for each formation channel predict a different entropy and therefore a different mass and radius for a given period.

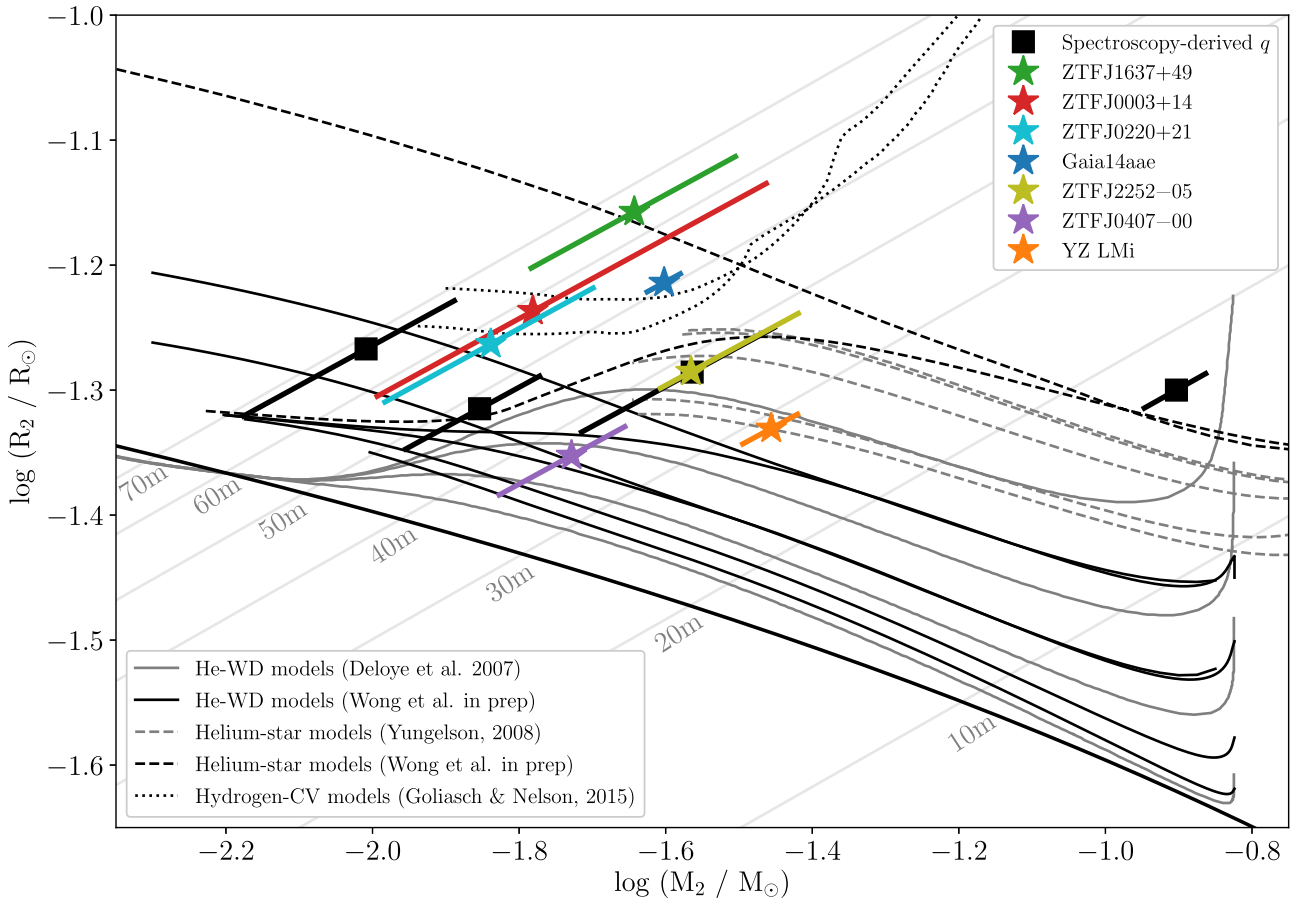


Figure 12. The mass and radius of donor stars in AM CVn systems compared to model predictions, adapted from Green et al. (2018b). Stars indicate measurements of eclipsing systems, the five new systems from this paper, YZ LMi from Copperwheat et al. (2011), and Gaia14aae from Green et al. (2018a). Solid lines show the white dwarf channel models [Deloye et al. 2007 in grey, Wong et al. (in preparation) in black], dashed lines show the H e-star channel models [Yungelson (2008) in grey, Wong and Bildsten (2021) in black], and dotted lines show the evolved CV channel models (Goliasch & Nelson 2015). The white dwarf and helium star tracks include multiple levels of entropy, with the lower entropy models at the bottom. The lowest line shows a zero-entropy donor. Models by Wong and Bildsten (2021) diverge; donors that are allowed to cool shrink at long orbital periods, while donors that are not allowed to cool and lose entropy as they lose mass stay large.

In the figure, we show tracks for evolved CVs (Goliasch & Nelson 2015), the white dwarf track from Deloye et al. (2007), and tracks for the H e-star channel from Yungelson (2008). We also show WD-tracks and H e-star tracks by Wong et al. (in preparation). The tracks by Wong et al. (in preparation) diverge; the models that curve downwards include cooling; the tracks that continue on to the top left do not include cooling.

First of all, the measurements indicate that masses are 1.5–2.5 times more massive than a zero-entropy donor for the same orbital period. This is similar to what has been measured for YZ LMi and Gaia14aae.

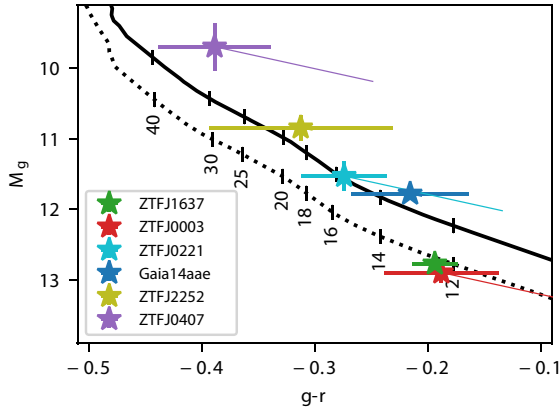
The short-period systems seem to be consistent with either white dwarf models or H e-star models. However, current WD and H e-star models predict that the donors cool and shrink at orbital periods of 30–40 min, which is not consistent with the observations.

The long-period systems seem to be very large, similar to Gaia14aae. As noted by Green et al. (2018a), the measurements are consistent with CV-channel donors, but this channel is excluded by the lack of hydrogen in the spectra (Nelemans et al. 2010). In addition, this channel is also predicted to be the least common, although more recent work by Liu, Jiang & Chen (2021) suggests that this might not be the case.

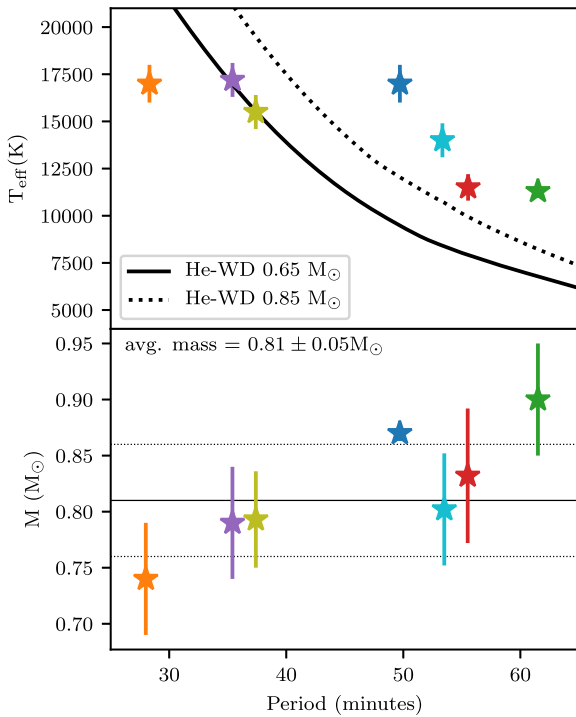
The alternative solution is that AM CVn systems do evolve through the WD and/or H e-star channel but for some reason do not cool and shrink at long orbital periods [indicated by the models by Wong et al. (in preparation)]. To answer this question, the donor properties of the new ZTF systems need to be measured with similar accuracy as for Gaia14aae. In addition, precise characterization of donors of to be discovered short-period eclipsing systems ($\lesssim 25$ min) is needed to constrain the models before adiabatic cooling is predicted to become important. In addition, models need to be updated to make sure that any source of potential heating of the donor is taken into account.

7.4 Properties of the white dwarf

Fig. 13 shows the properties of the white dwarf in eclipsing AM CVn systems. We first compare the absolute magnitude versus the colour of the white dwarf with model values. We calculate these values by using the Pan-STARRS measurement, *Gaia* eDR3 distances, the estimated white dwarf contribution from Table 4, and the reddening towards the system (see Table 1). A general prediction is that the effective temperature of white dwarfs in AM CVn systems is determined by the average accretion rate and therefore correlated with the orbital period (Bildsten et al. 2006). Our measurements



(a) The absolute g -band magnitude versus the $g-r$ colour of the white dwarf in eclipsing AM CVn systems. The measurements have been de-reddened based on the $g-r$ reddening (see Table 1), indicated with lines with the same colour as the markers. Model temperature are indicated below the model in kK.



(b) The temperature and mass of the white dwarf in eclipsing AM CVn systems versus the orbital period. The horizontal lines in the bottom panels show the average mass and the one standard deviation range.

Figure 13. Properties of the accreting white dwarfs in eclipsing AM CVn systems. Models for a $0.65 M_{\odot}$ (dashed line) and $0.85 M_{\odot}$ (solid line) white dwarf and are from Wong and Bildsten (2021). Values for YZ Lmi and Gaia14aae have been taken from Copperwheat et al. (2011) and Green et al. (2018a, 2019b).

generally agree with the model values calculated by Wong et al. (in preparation). Although the error bars are too large to estimate the mass, the general trend is that the long-period systems are massive $\sim 0.85 M_{\odot}$, while the shorter period systems seem more consistent with lower masses $\sim 0.65 M_{\odot}$.

We have measured the temperature from the SEDs and the mass using the eclipses. As we have already seen from the colour of the white dwarf, long-period systems are colder while short-period

systems contain a hotter white dwarf. However, the temperature for the longer period systems seems systematically higher than models predict at those particular periods.

This could be due to a larger than expected donor entropy, which results in a higher mass accretion rate and therefore higher temperature. However, it could also be due to an additional source of energy in the white dwarf that causes the white dwarf to remain hot for a longer time (e.g. Bauer et al. 2020). It is possible that the temperature estimates of the short-period systems are systematically underestimated, possibly by imperfect corrections to the overall luminosity. Alternatively, metals in the white dwarf’s atmosphere can significantly suppress the UV luminosity, which results in an underestimate of the temperature. Since the SED of hot white dwarfs peaks in the UV, short-period systems would be more affected.

By modelling the eclipse light curves and assuming a white dwarf $M-R$ relation, we have also determined the mass of the white dwarfs. These are similar to the white dwarf masses in the other eclipsing AM CVn systems (Gaia14aae and YZ Lmi). The unweighted average and variance of the mass is $0.81 \pm 0.05 M_{\odot}$. This is more massive than the typical isolated white dwarfs (Kepler et al. 2007) and similar to white dwarfs in hydrogen-rich CVs, which have an average mass of $\approx 0.83 M_{\odot}$ (Littlefair et al. 2008; Savoury et al. 2011; Pala & Gänsicke 2017).

However, the explanation for this is different. For hydrogen CVs, angular momentum loss causes systems with low-mass white dwarfs to merge during the early stages of the CV phase (Nelemans et al. 2016; Schreiber, Zorotovic & Wijnen 2016; Zorotovic & Schreiber 2020). In the case of AM CVn systems, accretion in systems with low-mass white dwarf is unstable and causes a merger during the common envelope (e.g. Shen 2015).

Kilic et al. (2016) show that the number of known white dwarfs with $M \gtrsim 0.8 M_{\odot}$ and low-mass white dwarf companions (WD-channel) is sufficient to explain the AM CVn birth rate. However, the low-mass white dwarfs have a low entropy, which would result in cool and small donors (Deloye et al. 2007), inconsistent with our results (Fig. 12).

8 CONCLUSION AND SUMMARY

We searched the ZTF light curves for deep eclipsing white dwarfs and identified five new eclipsing AM CVn systems with periods ranging from 35 to 62 min. Using this sample, we estimated the local space density, which is consistent with previous observational estimates. This is again two orders of magnitude less than model predictions and excludes the possibility that this is due to a hidden population of faint, long-period AM CVn systems.

We obtained phase-resolved spectra and high-cadence light curves to characterize the systems. The high SNR-averaged spectra of the longer period systems revealed many broad metal absorption lines, including potassium and zinc, which have not previously been detected in any other AM CVn systems. Doppler maps show the presence of a ‘central spike’ for the longest period system.

We modelled the high-cadence light curves and the spectral energy distributions and measured the binary parameters (masses, radii, inclination, and white dwarf temperature) for all five systems. First, we showed that the effective accreting white dwarf temperatures of long-period systems are higher than models predict. This suggests a delay in cooling of the white dwarf. Secondly, the average accreting white dwarf mass is $\approx 0.8 M_{\odot}$, more massive than typical single white dwarfs. This suggests that AM CVn systems can be formed only with massive accreting white dwarfs. Thirdly, the donor stars have a high entropy and are a factor of 1.5–2.5 times more massive than a zero-temperature donor at the same orbital period. The high

observed entropy (radius) is consistent with white dwarf or He-star models for the two short-period systems. The long-period systems also have a large entropy (radius), while both WD and He models predict that AM CVn donor should decrease in entropy (radius) as they evolve to periods longer than ≈ 40 min. More accurate donor mass–radius measurements and more complete models are needed to resolve this inconsistency.

9 FUTURE WORK

We will continue to obtain data on the systems presented in this paper to fully utilize their potential. We aim to obtain high SNR, high-cadence light curves in order to measure the donor mass and radius to a precision of ~ 1 per cent (similar to that of Gaia14aae). Continued monitoring of these systems with high-speed cameras will also allow us to measure deviations in the eclipse arrival times.

As estimated in this paper, we expect there to be another handful of eclipsing AM CVn systems brighter than ≈ 20 mag. We will continue to search for new ZTF data for more eclipsing systems. Other survey telescope light curves (ATLAS, *Gaia*, BlackGEM, and Groot 2019) can also be used to find eclipsing AM CVn systems. This does require the ability to detect deep eclipses, either by implementing image differencing or by using forced photometry.

The Vera C. Rubin observatory (Ivezić et al. 2019) is starting observations in the near future. With a single epoch limiting magnitude of $r \approx 24$, it will observe thousands of AM CVn systems. However, spectroscopic verification spectra of this faint population is expensive, and identifying AM CVn systems by measuring the period using eclipses can be done with just the Vera C. Rubin observatory data. This will limit the identification to eclipsing AM CVn systems only, but there should be tens to a hundred of these in the Vera C. Rubin observatory footprint. Such a large sample of eclipsing AM CVn systems will provide a much clearer picture of the donor properties and with that the formation channels of AM CVn systems. We have shown that at least five in-eclipse measurements are needed to identify a period, which implies that a total of hundreds of epochs will be needed (see Appendix A). The Vera C. Rubin observatory cadence will be sparse compared to ZTF and it will take > 5 yr before enough epochs will be collected to enable a systematic search.

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DATA AVAILABILITY

The ZTF data underlying this article are available at <https://irsa.ipac.caltech.edu/Missions/ztf.html>. The other data underlying this article will be shared on reasonable request to the corresponding author.

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SUPPORTING INFORMATION

Supplementary data are available at [MNRAS](https://www.mnras.org/) online.

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APPENDIX A: ZTF DETECTION EFFICIENCY

We determined the detection efficiency for ZTFJ1637+49 as a function of the number of epochs, see Fig. A1. We did this by randomly removing a set fraction of points from the light curve and tested if the BLS algorithm recovered the period. We model the curve with the function:

$$P(k, p) = 1 - \sum_0^k \binom{N}{k} p^k (1-p)^{N-k} \quad (\text{A1})$$

with k the number of *in*-eclipse points and p the effective eclipse duty cycle. For ZTF data of ZTFJ1637+49, the values of the best fit are $k = 5$ and $p = 0.0127$. This shows that the simple approximation is a good description of the actual recovery efficiency, and five *in*-eclipse points are enough to recover the orbital period.

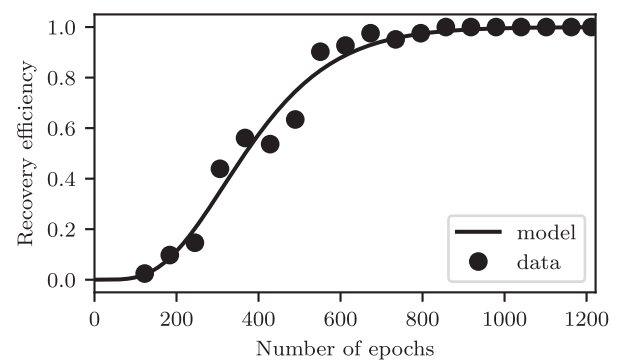


Figure A1. The period recovery efficiency as function of number of epochs. We used the ZTF light curve of ZTFJ1637+49. We randomly removed a fixed fraction of epochs and tested if our search algorithm recovered the known period. We fitted the curve with a simple probabilistic model (equation A1) and is a good approximation of the data. We use the model to rapidly evaluate in what fraction of the light curve an eclipse would be recovered.

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