

# Narrow-band giant pulses from the Crab pulsar

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## ABSTRACT

We used a new spectral-fitting technique to identify a subpopulation of 6 narrow-band giant pulses from the Crab pulsar out of a total of 1578. These giant pulses were detected in 77 min of observations with the 46-m dish at the Algonquin Radio Observatory at 400–800 MHz. The narrow-band giant pulses consist of both main- and inter-pulses, thereby being more likely to be caused by an intrinsic emission mechanism as opposed to a propagation effect. Fast radio bursts (FRBs) have demonstrated similar narrow-band features, while only little has been observed in the giant pulses of pulsars. We report the narrow-band giant pulses with  $\Delta\nu/\nu$  of the order of 0.1, which is close to the value of 0.05 reported for the repeater FRB 20190711A. Hence, the connection between FRBs and giant pulses of pulsars is further established.

**Key words:** pulsars: general – pulsars: individual: B0531 + 21 – fast radio bursts.

## 1 INTRODUCTION

Giant pulses from the Crab pulsar have demonstrated fluences of thousands of Jy ms and burst energies up to  $10^{31}$  erg (Cordes et al. 2004; Hankins, Jones & Eilek 2015; Eilek & Hankins 2016; Hankins, Eilek & Jones 2016; Bera & Chengalur 2019; Bij et al. 2021). They have shown various features in the spectrum, including broad-bandedness (Karuppusamy, Stappers & Lee 2012; Eftekhari et al. 2016) and drifting (Hankins et al. 2003; Hankins & Eilek 2007; Bij et al. 2021), as well as multiple peaks in the temporal profile (Hankins et al. 2003; Bij et al. 2021). Main pulses (MPs) from the Crab at high frequencies (8–10.5 GHz) consist of microbursts, each of which can be resolved into overlapping strongly and randomly polarized nanoshots (Hankins & Eilek 2007). Some speculate that a generic giant pulse from other pulsars such as PSR B1937+21 and PSR B1821–24A could follow a similar pattern (Bilous et al. 2015).

Fast radio bursts (FRBs) are bright radio transients with durations of milliseconds, fluences from a few to hundreds of Jy ms, and origins from galactic to cosmological distances (Lorimer et al. 2007; Thornton et al. 2013; Masui et al. 2015; CHIME/FRB Collaboration 2019a, 2020; Bochenek et al. 2020). Hundreds of FRBs had been reported in the past decade (Petroff et al. 2016; The CHIME/FRB Collaboration 2021). While some FRBs demonstrated repetition (Spitler et al. 2016; CHIME/FRB Collaboration 2019c; Fonseca et al. 2020) and two with periodic activity (Chime/Frb Collaboration 2020; Rajwade et al. 2020), the majority of FRBs appeared non-repeating. The repeating FRBs typically showed narrow-band features and downward frequency drifts across the dynamic spectrum (CHIME/FRB Collaboration 2019b; Hessels et al. 2019; Fonseca et al. 2020), and the non-repeating FRBs usually showed broad-band features in the dynamic spectrum (Macquart et al. 2019; CHIME/FRB Collaboration 2019a). Similar to the Crab, FRBs show a diversity in their temporal and spectral profiles (Petroff et al. 2016; Gourdji et al. 2019; CHIME/FRB Collaboration 2019a, c; Fonseca et al. 2020; Pleunis et al. 2021).

Recently, the repeater FRB 20190711A showed highly band-limited features, for which the spectral width is only  $65 \pm 7$  MHz at a spectral centre of  $1355 \pm 3$  MHz (Kumar et al. 2021). Moreover, PSR J0540–6919 recently showed similar narrow features (Geyer et al. 2021). As giant pulses have burst energies only a few orders of magnitude lower than FRBs, they have been associated with FRBs (Connor, Sievers & Pen 2016; Cordes & Wasserman 2016). The NASA Deep Space Network recently detected a burst from the repeating FRB 20200120E that shows a sub-100-ns structure whose luminosity is  $\sim 500$  times brighter than the Crab pulsar’s nanoshots (Hankins & Eilek 2007; Majid et al. 2021). In addition, the Crab pulsar and a few repeating FRBs share similar power-law indices for their differential distributions of energy. The Crab, FRB 121102, and FRB 180916.J0158 + 65 power-law indices range from 2.1 to 3.1 (Mickaliger et al. 2012), 1.6 to 1.8 (Wang & Zhang 2019), and around 2.3 (Chime/Frb Collaboration 2020), respectively. Lastly, FRBs and giant pulses have similarities in hypothesized emission mechanisms, which we will further discuss in Section 3.3. As such, we are motivated to study the connections between FRBs and giant pulses.

We report a narrow-band giant pulse subpopulation from the Crab pulsar in this paper, which further connects FRBs to pulsars’ giant pulses. We structure the paper as follows: Section 2 discusses the procedure of data pre-processing, illustrates a new technique to correct the dispersion measure (DM) through singular value decomposition (SVD), and proposes a new technique to classify a giant pulse as either broad- or narrow-band based on its spectral properties. Section 3 discusses the subpopulation’s statistics, its properties, and its potential connections to FRBs. Section 4 summarizes the results and explores future research avenues.

## 2 METHODS AND ANALYSIS

### 2.1 Data recording and giant-pulse search

We observed the Crab pulsar with the 46-m dish at the Algonquin Radio Observatory (ARO) on 2018 April 25 in two scans for a total duration of 77 min (49 + 28 min; session 1 + session 2).

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We processed the baseband voltage data using a CHIME acquisition board (Bandura et al. 2016). This digitized the signals, passed them through a polyphase filter, and recorded them in the standard very long baseline interferometry (VLBI) data interface format (VDIF) (Whitney et al. 2009). We channelized the data into 1024 frequency channels from 400 to 800 MHz for two linear polarizations with a time resolution of 2.56  $\mu$ s.

The giant-pulse search algorithm coherently dedispersed the VDIF data with an initial DM value of 56.77 pc cm<sup>-3</sup> (Lyne, Pritchard & Graham Smith 1993).<sup>1</sup> After summing the power over all frequency channels and both polarization components, the algorithm searched for triggers with a minimal signal-to-noise ratio (S/N) of 5 in a 0.328-ms rolling boxcar window. We describe a DM optimization procedure in Section 2.2. We re-searched the data with the optimized DM of 56.7563 pc cm<sup>-3</sup>, which yielded 20 085 triggers with S/N > 5. We saved 12.8 ms of data for each trigger. We determined the triggers' rotational phase with TEMPO2 (Hobbs, Edwards & Manchester 2006) using an ephemeris from Jodrell Bank<sup>1</sup> (Lyne et al. 1993). We identified 1578 triggers with S/N > 9 and the rotational phase being either MP or inter-pulse (IP) as giant pulses for further investigation in this study.

## 2.2 Optimal DM determination

The initial DM systematically underestimated the S/N, thereby reducing some potential pulses' S/N below the detection threshold. It also changed dynamic spectrum structure, limiting the potential for a spectral study. Hence, we corrected the DM. We propose to use SVD, which has been applied to improve the precision of pulsar timing (Lin et al. 2018), to automatically optimize the DM for the giant pulses. SVD decomposes the dynamic spectrum of the giant pulse as the sum of individual modes of dynamic spectra, which can then be analysed as a function of DM.

Specifically, we decomposed the dynamic spectrum of a bright pulse into one eigenvalue and two eigenfunctions:

$$P_{ft} = \sum_n U_{fn} S_n V_{nt}^T, \quad (1)$$

where  $P_{ft}$  is the pulse's dynamic spectrum, and for each mode  $n$ ,  $U_{fn}$  is the eigenfunction in frequency  $f$ ,  $S_n$  is the eigenvalue, and  $V_{nt}^T$  represents the transpose eigenfunction in time. When we changed the pulse's DM, the corresponding primary eigenvalue was also changed. We determined the dynamic spectrum's optimal DM value with the maximal primary eigenvalue.

We applied the procedure to session 2's brightest broad-band pulse. We adjusted the dynamic spectrum by incoherent dedispersion within a range of 56.7550–56.7580 pc cm<sup>-3</sup> and with a step of 0.0001 pc cm<sup>-3</sup>. We then decomposed each dynamic spectrum into the eigenvalue and the two eigenfunctions using SVD. Panel (a) in Fig. 1 shows the primary eigenvalue across a range of DM values. We determined the optimal DM value, 56.7563 pc cm<sup>-3</sup>, by the corresponding maximal primary eigenvalue, and we re-searched the full data using this DM. Panels (b) and (c) in Fig. 1 show the pulse's dynamic spectrum with the initial (56.77 pc cm<sup>-3</sup>) and optimal DM values, respectively. Panels (d) and (e) in Fig. 1 show the pulse's eigenvalue and eigenfunction in time across modes with the initial and optimal DM values, respectively. The eigenfunction in time's primary mode represents the frequency-averaged pulse profile, for which the optimal DM profile has a higher amplitude compared to

the initial DM profile. Furthermore, the optimal DM profile shows the noise level in the third mode, while the initial DM profile does not show the noise level until beyond the fourth mode.

## 2.3 Gain correction

We calibrated the frequency-dependent gains, which are closely related to the observed spectral structure. To do this, we divided each time slice of the dynamic spectrum by the recording session's average gain profile. We determined the profiles by noise-subtracting each session's 1000 brightest pulses, aligning them in time, and then averaging over time in each polarization. Bij et al. (2021) contains more details.

## 2.4 Flux calibration

Flux from the Crab nebula dominated the off-pulse emission. We subtracted the Crab's average off-pulse emission by B0355+54's average off-pulse emission to measure the flux contribution from the Crab nebula. B0355+54 was another pulsar recorded in the same run (Bij et al. 2021). The giant pulse's flux  $S_{GP}$  is then expressed as follows:

$$S_{GP}(f) = S_{\text{nebula}}(f) \times I_{GP}(f)/I_{\text{nebula}}(f), \quad (2)$$

where  $S_{\text{nebula}}(f) \simeq 955 \text{ Jy } (f/1 \text{ GHz})^{-0.27}$  is the Crab nebula's nebular flux spectrum,  $I_{GP}$  is the giant pulse's intensity, and  $I_{\text{nebula}}$  is the nebula's intensity. Bij et al. (2021) contains more details.

## 2.5 Radio-frequency interference (RFI) masking

For each giant pulse, we have 12.8 ms of data. We defined the on-pulse region as  $-0.256$  to  $1.28$  ms, where the peak value of the time series is centred at 0 ms. We chose this range to include precursor-like or strong-scattering features. If the peak value was located near the time-window's boundary, the boundary, instead, was used as a cutoff. We defined the remaining 11.264 ms as the off-pulse region.

We identified and masked the RFI channels through the following schema. First, for each frequency channel, we calculated the mean and standard deviation over the off-pulse time bins, yielding two functions of frequency  $m_{\text{off}}$  and  $\sigma_{\text{off}}$ . We then calculated the gradients of these functions with respect to frequency,  $\nabla m_{\text{off}}$  and  $\nabla \sigma_{\text{off}}$ , and determined the means and standard deviations of  $\nabla m_{\text{off}}$ ,  $\sigma_{\text{off}}$ , and  $\nabla \sigma_{\text{off}}$ . Finally, we masked channels with  $\nabla m_{\text{off}}$ ,  $\sigma_{\text{off}}$ , or  $\nabla \sigma_{\text{off}}$  exceeding  $\pm 1$  standard deviation of their respective frequency means.

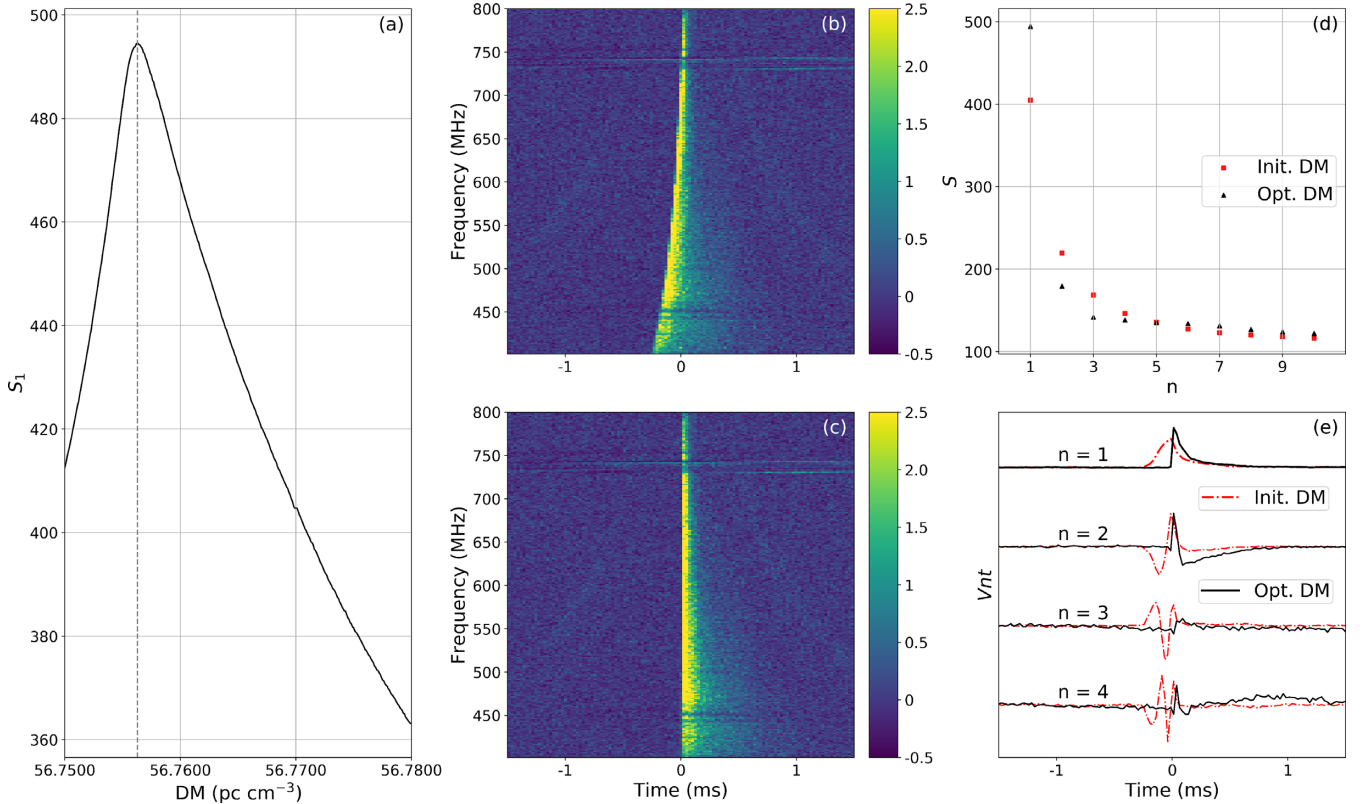
Certain channels demonstrated large negative dips in a frequency sub-band due to noise-subtraction and packet loss from coherent dedispersion. We analysed these pulses separately.

After masking the RFI channels, we averaged the dynamic spectrum over the on-pulse region of 1.536 ms. We rebinned the averaged dynamic spectrum from 1024 to 64 frequency channels to determine the pulse's intensity spectrum. We further masked rebinned channels that consist of more than 40 per cent by RFI channels.

## 2.6 Spectral fitting

Traditionally, a Crab giant pulse's intensity spectrum is fitted with a power law (Karuppusamy, Stappers & van Straten 2010; Karuppusamy et al. 2012; Eftekhari et al. 2016). For broad-band pulses, this is a strong fit (Meyers et al. 2018); however, narrow-band pulses display non-linear structure in amplitude versus frequency in log–log space and thus require a fit with more curvature.

<sup>1</sup><http://www.jb.man.ac.uk/~pulsar/crab.html>



**Figure 1.** DM optimization with the SVD technique. Panel (a) shows the  $S_1$  value as a function of DM. The optimal DM of 56.7563 pc cm<sup>-3</sup>, which is marked with the dashed line, was determined by the corresponding maximal value of  $S_1$ . Panel (b) shows the dynamic spectrum of the brightest broad-band pulse of session 2 with the initial DM of 56.77 pc cm<sup>-3</sup>. Panel (c) shows the dynamic spectrum with the optimal DM of 56.7563 pc cm<sup>-3</sup>. Panel (d) shows the comparison of  $S$  between the SVD decomposition of the dynamic spectrum with the initial (red) and optimal (black) DM values, abbreviated init. and opt., respectively. Panel (e) shows the comparison of  $V_{nt}$  between the SVD decomposition of the dynamic spectrum with the initial (red) and optimal (black) DM values.

Hence, we applied the following fitting function to the 1578 pulses using least-squares optimization:

$$I = \kappa \left( \frac{f}{f_0} \right)^{\alpha + \beta \log \left( \frac{f}{f_0} \right)}, \quad (3)$$

where  $f$  is a frequency value between 400 and 800 MHz,  $I$  is the amplitude (arbitrary units) at a given frequency,  $\alpha$ ,  $\beta$ , and  $\kappa$  are the free parameters to be fit, and  $f_0 = 566$  MHz is the reference frequency, as it is the log-scale centre. To avoid overestimating or underestimating the model in the log-log space, we applied an upper limit of  $10^3$  and a lower limit of  $10^{-1}$  for the amplitude of the spectrum. We estimated the fitted parameters' uncertainty in equation (3) through the standard error propagation. Fig. 2 shows the fitting results, and we will discuss the distribution of parameters in Section 3.1.

We refer to equation (3) as the quadratic fit in accordance with its intensity–frequency structure in log-log space.  $\kappa$  represents the amplitude,  $\alpha$  relates to the bandwidth centre of the pulse relative to  $f_0$ , and  $\beta$  relates to the bandwidth of the pulse. The parameters are coupled and can therefore result in poor fits if the reference frequency is too different from the narrow-band spectral centre. To correct this, we refitted the identified narrow-band pulses, which is described in Section 3.1, with reference frequencies much closer to the spectral centre. We display the resulting properties in Table 1 with error propagation considering covariances. The coupling is not an issue for broad-band pulses.

### 3 DISCUSSION

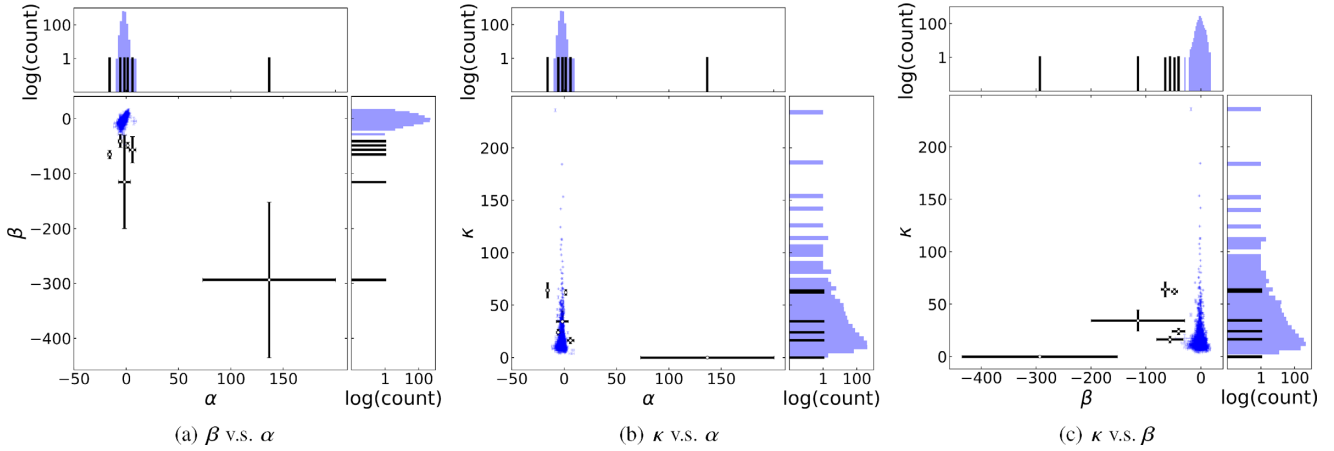
#### 3.1 A population of narrow-band pulses

In total, we identified six narrow-band giant pulses with three MPs and three IPs, which represent a 0.4 per cent population in the 1578-pulse sample. Fig. 2 shows the distributions of the fitting parameters for the broad-band (in blue) and narrow-band (in black) pulse populations. Therefore, the clustering of the broad-band pulses, with narrow-band outliers in panels (a) and (c), distinguishes the two populations.

Due to the high spectral curvature, narrow-band pulses show  $\beta \leq -30$  in the  $\beta$  value histograms in panels (a) and (c) of Fig. 2. We further validated this threshold by inspecting the quadratic fit with  $\alpha$  and  $\kappa$  fixed at their population medians and noting that narrow-band features are strongly visible around  $\beta \leq -30$ . This indicates the method could be used to identify narrow-band pulses in a data set. Furthermore, since the narrow-band and broad-band points overlap in panels (a) and (b),  $\alpha$  is not a strong discriminator of narrow- versus broad-bandedness. We note that the largest  $\alpha$  in panels (a) and (b) of Fig. 2 corresponds to pulse C in Fig. 3. In general, a large  $\alpha$  indicates a significant difference between the spectral centre and the reference frequency.

We present a gallery of the flux-calibrated narrow-band pulses in Fig. 3 in descending brightness from panel A to F. We show the on-pulse-averaged spectral profile overlaid with the quadratic fitting in the right-hand panel and the time series in the top panel. We display the properties of the narrow-band pulses in Table 1.





**Figure 2.** The distributions of the fitting parameters  $\alpha$ ,  $\beta$ , and  $\kappa$ . In each of the middle panels, the points with blue error bars represent broad-band pulses (1572 of them), while the points with black error bars represent narrow-band pulses (six of them). The error bars represent the 68 per cent confidence interval of the fitted result. Furthermore, for each of the following sub-plots, the middle panel shows the scatter plot of the  $(x, y)$  data, the top panel is the histogram of the  $x$ -data, and the right-hand panel is the histogram of the  $y$ -data. Panel (a):  $\beta$  versus  $\alpha$ . A clear separation of the narrow- and broad-band populations suggests  $\beta$  is a discriminating parameter between them. Panel (b):  $\kappa$  versus  $\alpha$ . A lack of separation of the populations in the middle and top panels suggests  $\alpha$  is not a discriminating parameter. Panel (c):  $\kappa$  versus  $\beta$ . The separation of the populations suggests  $\beta$  is a discriminating parameter, and the separation of narrow-band pulses in the right-hand panels suggests they occur at a wide range of brightnesses. As discussed in Section 2.6,  $\kappa$  is coupled to  $\alpha$ ; therefore, the narrow-band  $\kappa$  values are not fully accurate in panels (b) and (c), but the fact that narrow-band pulses are observed at a wide range of brightnesses remains even after refitting.

**Table 1.** Properties of six narrow-band pulses. The label of the pulse corresponds to Fig. 3. The S/N is integrated over the whole 400 MHz bandwidth. MP and IP refer to the main- and inter-pulse, respectively.  $S_{\max}$  refers to the peak flux density and  $F$  to the fluence. The  $\nu$  and  $\Delta\nu$  represent the measured spectral centre and bandwidth at full width at half-maximum (FWHM), respectively. The statistical uncertainties represent the 68 per cent confidence interval of the measurements.

| Pulse             | A        | B        | C        | D        | E        | F        |
|-------------------|----------|----------|----------|----------|----------|----------|
| S/N               | 57       | 32       | 16       | 13       | 11       | 9        |
| Type              | MP       | IP       | MP       | IP       | MP       | IP       |
| $S_{\max}$ (Jy)   | 1995(38) | 1198(56) | 669(29)  | 593(22)  | 419(48)  | 335(23)  |
| $F$ (Jy ms)       | 285(1)   | 146(1)   | 52(1)    | 69(1)    | 50(1)    | 71(1)    |
| $\nu$ (MHz)       | 500.9(3) | 575.3(4) | 713(1)   | 563(1)   | 602(2)   | 528(2)   |
| $\Delta\nu$ (MHz) | 100.8(5) | 122.8(7) | 71(3)    | 90(2)    | 68(3)    | 133(4)   |
| $\Delta\nu/\nu$   | 0.201(1) | 0.213(1) | 0.100(4) | 0.160(4) | 0.112(5) | 0.251(8) |

We measured the peak flux and fluence using the data with a 25.6  $\mu$ s time resolution and a 1.5625 MHz frequency resolution. The spectral centre  $\nu$  refers to the frequency channel with the model's peak value, while the spectral bandwidth  $\Delta\nu$  refers to the FWHM. This table shows that narrow-bandedness is independent of pulse-brightness, as there are narrow-band pulses observed at a range of S/N, peak flux densities, and fluences. Furthermore,  $\Delta\nu/\nu$  is independent of brightness, but further data would be helpful to understand its distribution.

### 3.2 The microstructure in the brightest narrow-band pulse

Farah et al. (2018) reported FRB 170827 with fine spectral modulations on a frequency scale of 1.5 MHz and striations on the scale of 100–200 KHz. It also displayed spiky emission features that can exceed 1 kJy in brightness in the frequency sub-band of 841–843 MHz. Motivated by this result, we further studied Pulse A's observably hyper-narrow-band intensity around 496–512 MHz.

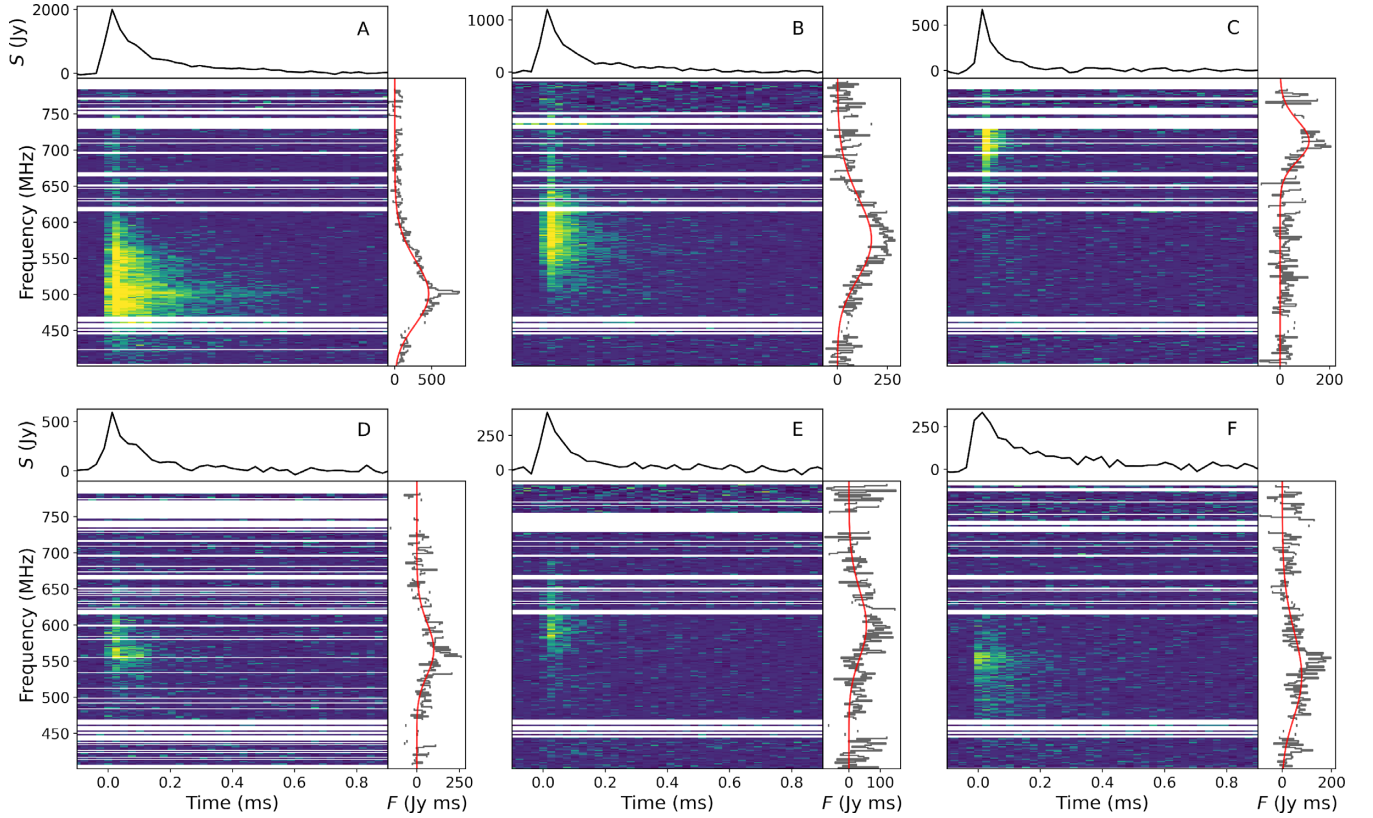
Pulse A showed a few bright and unresolved spots in the dynamic spectrum when we viewed it with the highest resolution in time (2.56  $\mu$ s) and frequency (0.390 625 MHz). These spots are referred to as the microstructure. The bright microstructures are around 496–512 MHz and 0–30  $\mu$ s in the dynamic spectrum.

Interstellar scintillation (ISS) is unlikely to cause the feature. The angular broadening of the Crab in VLBI yields a scattering angle of  $\theta \sim 1.5$  mas at 600 MHz for ISS (Rudnitskii et al. 2016). Assuming thin-screen scattering with a scattering screen roughly halfway to the pulsar (Vandenberg 1976), the decorrelation bandwidth is 30 KHz. This is much smaller than the 390 KHz frequency resolution, so the scintillation is unlikely to cause the microstructure.

Through the following statistical analysis, we argue that the bright microstructures show no significance greater than  $3\sigma$ . We first standardized the off-pulse region to obtain the mean and standard deviation as equal to 0 and 1, respectively. We divided the dynamic spectrum, which was pre-processed in Section 2.5, by the standard deviation of the off-pulse for each frequency channel. This is the so-called on/off ratio.

We then compared the signal baseline between the on- and off-pulse regions to compare the on-pulse bright microstructure to the noise. We found that the on-pulse region's signal baseline is 15 times higher than the off-pulse region's baseline. To estimate the significance of the on-pulse bright microstructures, we multiplied the off-pulse region by a factor of 15 (the so-called amplified off-pulse region) and used it as the noise-fluctuation for the on-pulse region. We then generated the cumulative distribution function (CDF) of the amplified region. We applied this process to each of the six narrow-band giant pulses.

Lastly, we determined the significance of the on-pulse bright microstructures with the amplified off-pulse region as the baseline. Considering the look-elsewhere effect for six narrow-band giant pulses, the  $z$ -score of 3 gives the  $p$ -value of 0.000 225. This corresponds to the on/off ratio of 94 for the amplified off-pulse region CDF. We found that the on/off ratio of the bright microstructures has a range from 35 to 47, which is below the  $3\sigma$  significance.



**Figure 3.** The dynamic spectrum, time series, and spectral profile of the six narrow-band giant pulses. Each central panel shows the frequency–time dynamic spectrum with a frequency resolution of 1.5625 MHz and a timing resolution of 25.6  $\mu$ s, where the RFI channels are masked out. The upper panel show the time series of the flux ( $S$ ) in units of Jy, which is the frequency-averaged profile. The side panel show the spectral profile of the fluence ( $F$ ) in units of Jy ms and the fitting model via the grey and red lines, respectively.

### 3.3 Possible physical scenarios of narrow-band emission

A number of models predict narrow-band emission in radio transients. Cordes et al. (2017) shows that caustics produced by plasma lensing can strongly magnify ( $\lesssim 10^2$ ) FRB signals on short time-scales, which look like narrow-band spectral peaks (0.1–1 GHz). These images can also interfere, creating even narrower ( $\sim 1$ –100 MHz) frequency structures. If plasma lensing were the cause of narrow-band spectral structure, adjacent pulses in time should also demonstrate it, but we only observed 6 narrow-band pulses in a sample of 1578 at sporadic times, so this hypothesis is less likely. However, Bij et al. (2021) argues that narrow-band features could arise from the interference of nanoshots that are nearly equally spaced, and these nanoshots could be echoes produced by plasma lensing in the pulsar wind. Therefore, plasma lensing could, in principle, cause the narrow-band features, though the predicted bandwidth of the narrow-band emission is still unknown.

Metzger, Margalit & Sironi (2019) argues that FRB emission can be modelled as synchrotron maser emission from decelerating relativistic blast waves. This model explains FRBs’ observed downward drifting (CHIME/FRB Collaboration 2019b; Hessels et al. 2019; Fonseca et al. 2020) as arising from the blast-wave’s deceleration coupled with induced Compton scattering at low frequencies and maser emission fall-off at high frequencies. For millisecond bursts, they predict a  $\Delta\nu/\nu$  value near 1, which is above what we observe. However, they argue that this could be due to a simplistic treatment of low-frequency suppression of the spectral energy distribution due to Compton scattering and that a more accurate treatment of the suppres-

sion would lead to a sharper spectral peak. Thus, this model should not be ruled out as a potential explanation for narrow-band pulses.

Lastly, some models rely on the Lorentz factor of the particles that generate the radio waves. Lyutikov (2021) proposes a model in which radio waves are emitted by the Compton scattering of Alfvén waves interacting with a particle beam generated through reconnection events. They deduce a particle produces a set of emission bands with spectral separation  $4\gamma_0^2 k_w c$ , where  $\gamma_0$  is the particle beam’s Lorentz factor and  $k_w$  relates to the environmental turbulence properties. Lu, Kumar & Zhang (2020) considers a model in which Alfvén waves carry released energy near the polar regions of the neutron star. When arriving at the charge starvation radius  $R$ , the waves generate an electric field that accelerates clumps of particles formed from two-stream instability. They argue the spectrum of radio waves from coherent curvature emission by the clumps can only be slightly broadened [ $\Delta\nu/\nu \simeq (\gamma\ell_\perp/R)^2 \sim 0.1$ ] due to the Doppler effect, and the spectrum can display variations over a narrow band from delays in the radiation arrival time. Here,  $\gamma$  is the particle’s Lorentz factor and  $\ell_\perp$  is the particle clump’s transverse size.

### 3.4 Spectral similarities between pulsars and FRB 20190711A

Macquart et al. (2020) reported FRB 20190711A with a bandwidth of  $\sim 150$  MHz at the  $L$  band, and later Kumar et al. (2021) reported a repeating and narrow-band pulse from the same source with a spectral centre of  $1355 \pm 3$  MHz and a spectral bandwidth of  $65 \pm 7$  MHz, which corresponds to a  $\Delta\nu/\nu$  value of  $0.048 \pm 0.005$ .

Recently, Geyer et al. (2021) observed ‘flux knots’ in the giant pulses of PSR J0540–6919, which are single, bright, band-limited features that are symmetric in frequency response. They observed 24 flux knots in their three recording epochs totalling 5.7 h, with 18 showing FWHM less than 236 MHz when fitted with a Gaussian profile. The mean FWHM of the 24 knots is 198 MHz and the mean FWHM of the 18 narrowest knots is 146 MHz. The narrowest band-limited pulse has FWHM  $68.3 \pm 4.7$  MHz with a spectral centre of  $1472 \pm 2$  MHz, which corresponds to a  $\Delta\nu/\nu$  value of roughly  $0.046 \pm 0.003$  using the same definition as before. They determine the flux knots are unlikely to be caused by scintillation or lensing at the shock boundary.

The  $\Delta\nu/\nu$  values stated above are roughly a factor of 2 smaller than six narrow-band pulses that are listed in Table 1. This could potentially be explained by a point made in Kumar et al. (2021), that there could be emission below their detection threshold, leading to a smaller measured spectral bandwidth than was physically generated. This could be due to the far distance of FRB 20190711A ( $z = 0.522$ ) (Macquart et al. 2020; Kumar et al. 2021). Therefore, the  $\Delta\nu/\nu$  values determined here are likely closer to that of FRB 20190711A than is immediately apparent. Moreover, this argument, the  $\Delta\nu/\nu$  value measured for the narrowest pulse of PSR J0540–6919 is likely due to intrinsic factors given its galactic origin. As the narrow-band pulses observed by Geyer et al. (2021) occupy a wider distribution of  $\Delta\nu/\nu$  above a threshold of 0.05, it is comparable to the pulses observed here and to FRB 20190711A.

In any case, the fact that FRB 20190711A and two pulsars show both broad- and narrow-band features further connects FRBs and giant pulses from pulsars.

## 4 CONCLUSIONS

This paper reports a new narrow-band giant pulse subpopulation from the Crab pulsar identified between 400 and 800 MHz via a new fitting method. The approximate occurrence rate of these pulses is less than five in every thousand giant pulses. We observed the pulses with fluxes of several hundreds to thousands of Jy and consisting of both MPs and IPs. Due to shared phenomenology, this discovery further connects giant pulses to FRBs.

Gourdji et al. (2019) and Kumar et al. (2021) argued that conducting sub-band burst search strategies can enhance further research in this area. We encourage re-searching the existing giant-pulse data sets with sub-band searching (Mickaliger et al. 2012; Eftekhari et al. 2016; Meyers et al. 2018; van Leeuwen et al. 2020). Searching sub-bands would increase the chance that lower S/N narrow-band pulses with smaller  $\Delta\nu/\nu$  would be found, especially in broad-band studies and studies of objects without a previously known DM (Gourdji et al. 2019). Modifications in the definition of S/N could also be made to incorporate narrow-bandedness (Gourdji et al. 2019).

Furthermore, while we found that the microstructure in the narrow-band giant pulses does not exceed  $3\sigma$  statistical significance, others have investigated the time and frequency microstructure in FRBs (Farah et al. 2018; Macquart et al. 2019; Nimmo et al. 2021). We encourage searching for this in giant pulses as exceptionally narrow-band features could reach the brightnesses observed in FRBs. For this reason, we encourage observing giant pulses at high time and frequency resolution (Kramer, Johnston & van Straten 2002; Crossley et al. 2010; Eftekhari et al. 2016; van Leeuwen et al. 2020; Bij et al. 2021) for studying the microstructure.

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## DATA AVAILABILITY

The data analysed in this study will be shared on reasonable request to the corresponding author.

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