

# Significant luminosity differences of two twin Type Ia supernovae

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## ABSTRACT

The Type Ia supernovae (SNe Ia) 2011by, hosted in NGC 3972, and 2011fe, hosted in M101, are optical ‘twins,’ having almost identical optical light-curve shapes, colours, and near-maximum-brightness spectra. However, SN 2011fe had significantly more ultraviolet (UV;  $1600 < \lambda < 2500 \text{ \AA}$ ) flux than SN 2011by before and at peak luminosity. Several theoretical models predict that SNe Ia with higher progenitor metallicity should (1) have additional UV opacity and thus lower UV flux; (2) have an essentially unchanged optical spectral-energy distribution; (3) have a similar optical light-curve shape; and (4) because of the excess neutrons, produce more stable Fe-group elements at the expense of radioactive  $^{56}\text{Ni}$  and thus have a lower peak luminosity. Following these predictions, Foley and Kirshner suggested that the difference in UV flux between SNe 2011by and 2011fe was the result of their progenitors having significantly different metallicities. They also measured a large, but insignificant, difference between the peak absolute magnitudes of the SNe ( $\Delta M_{V, \text{peak}} = 0.60 \pm 0.36 \text{ mag}$ ), with SN 2011fe being more luminous. We present a new Cepheid-based distance to NGC 3972, substantially improving the precision of the distance measurement for SN 2011by. With these new data, we determine that the SNe have significantly different peak luminosities ( $\Delta M_{V, \text{peak}} = 0.335 \pm 0.069 \text{ mag}$ ). Consequently, SN 2011fe produced 38 per cent more  $^{56}\text{Ni}$  than SN 2011by, consistent with predictions for progenitor metallicity differences for these SNe, although alternative models may also explain this difference. We discuss how progenitor metallicity differences can contribute to the intrinsic scatter for light-curve-shape-corrected SN luminosities, the use of ‘twin’ SNe for measuring distances, and implications for using SNe Ia for constraining cosmological parameters.

**Key words:** supernovae: general – supernovae: individual: SN 2011by, SN 2011fe – galaxies: individual: M101, NGC 3972.

## 1 INTRODUCTION

Type Ia supernovae (SNe Ia) are excellent standardizable candles that can be measured to cosmological distances. Observations of SNe Ia have been crucial in discovering cosmic acceleration (Riess et al. 1998; Perlmutter et al. 1999), as well as making the most precise measurements of the Hubble constant,  $H_0$  (e.g. Riess et al.

2018), and the equation-of-state parameter for dark energy,  $w$  (e.g. Jones et al. 2018, 2019; Scolnic et al. 2018; Abbott et al. 2019).

SNe Ia are *not* ‘standard candles’ (just as Cepheid variables are not standard candles, strictly speaking), having a factor of  $\sim 10$  difference in luminosity from one extreme to the other. However, after correcting for light-curve shape (e.g. Phillips 1993) and colour (e.g. Riess, Press & Kirshner 1996; Tripp 1998), SNe Ia have a small scatter in their measured distances (typically  $\sim 8$  percent; e.g. Hicken et al. 2009; Stritzinger et al. 2011). A corollary to this empirical measurement is that two SNe Ia with exactly the same light-curve shapes, colours, and spectra should have luminosities

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that differ by at most the intrinsic luminosity scatter that belies additional, unaccounted physical diversity.

One possible driver for the non-zero intrinsic scatter is progenitor stars with differing metallicity. In this case, the number of neutrons increases (alternatively,  $Y_e$  decreases) with increasing metallicity. When the star explodes, the additional neutrons result in more stable Fe-group elements at the expense of radioactive  $^{56}\text{Ni}$ , which powers the SN light curve and directly affects its peak luminosity (Timmes, Brown & Truran 2003; Bravo et al. 2010). However, since roughly the same amounts of Fe-group elements are generated, the overall optical opacity is roughly the same, and the light-curve shape and colour are unaffected (Mazzali & Podsiadlowski 2006). Consequently, differing progenitor metallicity could cause the residual luminosity scatter observed among SNe Ia.

In addition to causing larger statistical distance uncertainties, changing progenitor metallicity with redshift could systematically bias the measurement of cosmological parameters (Podsiadlowski et al. 2006). Specifically, if the average progenitor metallicity decreases with increasing redshift, one might expect a drift in the mean peak luminosity of SNe Ia with redshift. Determining if such an effect exists, its magnitude, and its relationship with metallicity is critical for precisely and accurately measuring cosmological parameters with SNe Ia.

While changing progenitor metallicity has a minimal effect on the optical light curves, colours, and spectra of SNe Ia, the ultraviolet (UV) is significantly affected (e.g. Höflich, Wheeler & Thielemann 1998; Lentz et al. 2000; Sauer et al. 2008; Walker et al. 2012). In most models, increasing the progenitor metallicity increases the line blanketing within the outer layers of the ejecta. While these layers quickly become optically thin at longer wavelengths, they remain optically thick to UV photons through peak brightness. As a result, higher metallicity progenitors result in SNe Ia with depressed UV flux relative to the optical flux.

Differences in the UV continuum for low- and high-redshift SNe Ia have been detected in different surveys (Foley et al. 2012a; Maguire et al. 2012; Milne et al. 2015). While these detections are consistent with changing progenitor metallicity with redshift, there could be other effects related to changing populations that do not bias cosmological measurements.

The current sample of low-redshift SNe Ia with high-quality UV spectroscopy is relatively small (Kirshner et al. 1993; Foley et al. 2012b, 2014, 2016; Foley 2013; Foley & Kirshner 2013; Mazzali et al. 2014; Pan et al. 2015). A much larger sample of UV spectra from *Swift* has recently been published (Pan et al. 2018), but the spectra are of lower quality than what is typically obtained with the *Hubble Space Telescope* (*HST*). None the less, the sample of SNe Ia with UV spectra has been critical for understanding the connection between progenitor metallicity, UV properties, and optical luminosity.

In particular, the best indication of different progenitor metallicity for two SNe Ia comes from our studies of SNe 2011by and 2011fe (Foley & Kirshner 2013; Graham et al. 2015; hereafter **FK13** and **G15**, respectively; although see also Milne et al. 2013, Mazzali et al. 2014, and Foley et al. 2016), two ‘twin’ SNe Ia (e.g. Fakhouri et al. 2015) with nearly identical optical light curves, colours, and spectra, but dramatically different UV colours and spectra. Because of their similar optical properties, the differences in UV behaviour can be constrained to progenitor metallicity (**FK13**), with the SN 2011by and SN 2011fe progenitors being above and below solar metallicity, respectively. While the SNe have different late-time ( $t > 100$  d) optical decline rates, their nebular spectra are nearly identical (**G15**).

Having established that SNe 2011by and 2011fe likely had substantially different progenitor metallicity, they provide an excellent opportunity to directly determine the effect of metallicity on SN luminosity and distance estimates. Originally, **FK13** determined that their peak *V*-band absolute magnitudes differed by  $\sim 0.6$  mag, significantly larger than the intrinsic scatter of SNe Ia. However, this difference directly depends on the distances assumed for these nearby SNe. In particular, while there was a measured Cepheid distance to M101, the host galaxy for SN 2011fe (Shappee & Stanek 2011), there previously was only a Tully–Fisher distance to NGC 3972 (Tully et al. 2009), the host galaxy of SN 2011by. The latter had a relatively large uncertainty (0.36 mag), and systematic differences between the Cepheid and Tully–Fisher scale could have been the main cause for the apparently large differences in SN luminosity.

To reduce this source of uncertainty, we obtained a series of *HST* images to find Cepheid variable stars in NGC 3972 and measure both a precise absolute distance to NGC 3972 and a relative distance between M101 and NGC 3972, removing uncertainties common to both measurements. From this analysis, we find that the distance to NGC 3972 is similar to the Tully–Fisher measurement (although with a shift of 0.26 mag), and SNe 2011by and 2011fe do indeed have significantly different luminosities.

We will use our observations to examine the expectation that progenitor metallicity will affect the  $^{56}\text{Ni}$  mass of an SN Ia (Timmes et al. 2003; Bravo et al. 2010). We recognize that these inferences are limited at this time by how well these models span the parameter space of SN physics. Future models may find other mechanisms to explain the observed differences which may warrant revisiting our inferences.

Our *HST* observations are presented in Section 2. We detail our Cepheid distance estimates, direct luminosity comparisons of the SNe, and direct SN distance estimates in Section 3. We discuss the implications of this result and conclude in Section 4.

## 2 OBSERVATIONS

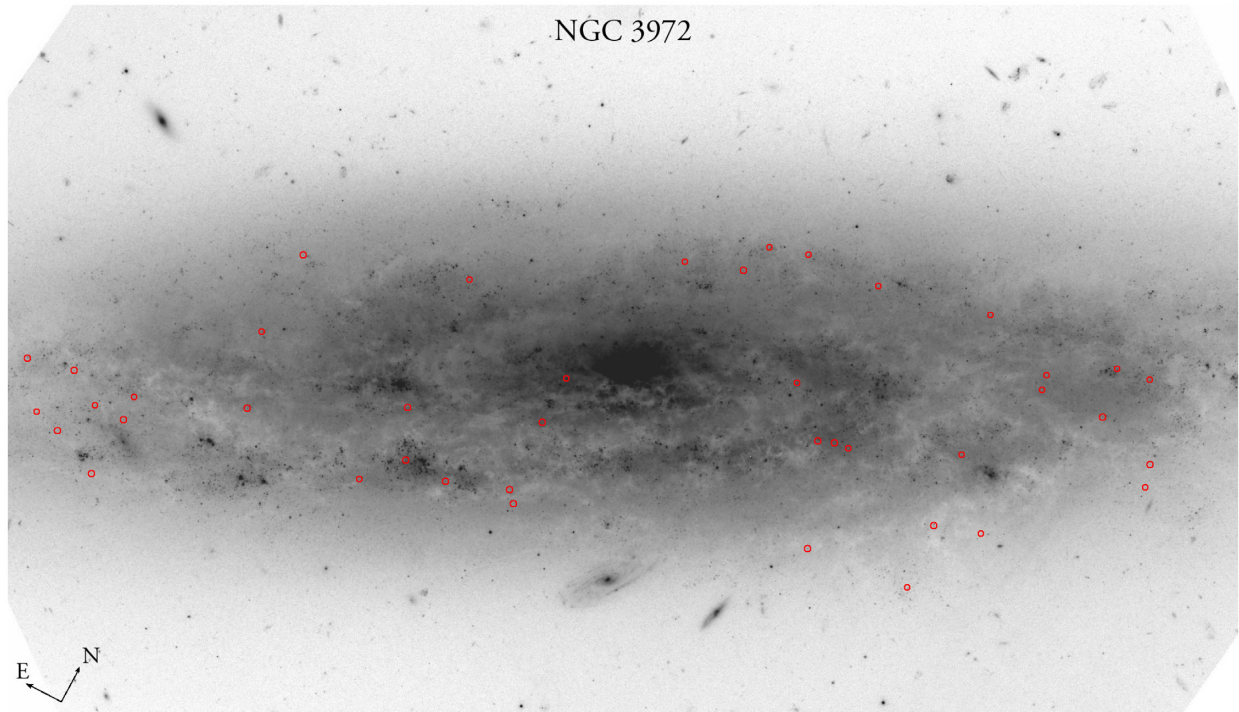
### 2.1 Cepheids in NGC 3972

To obtain a precise Cepheid distance to NGC 3972, we observed the galaxy using the *HST* Wide-Field Camera 3 (WFC3) UVIS and infrared (IR) channels (Programme GO–13647; PI Foley). Details of the UVIS and IR observations and data reduction are presented by Hoffmann et al. (2016) and Riess et al. (2016), respectively. Here we briefly review them.

Observations with WFC3/UVIS and the F350LP ‘white light’ filter were used to discover Cepheids and measure their periods. The data were obtained over 12 separate epochs, with the specific timing chosen to minimize the integral of the power over the frequency interval corresponding to the observation window. For six epochs, we also obtained observations with WFC3/IR and the F160W (roughly *H*) filter. For the other six epochs, half had an observation with WFC3/UVIS and the F555W (roughly *V*) filter and the other half had an observation with WFC3/UVIS and the F814W (‘wide *I*’) filter. The filtered observations are used primarily to aid in selection and to constrain dust reddening.

The first and last epochs were obtained on 2015 April 19 and July 08 UT, respectively, corresponding to an 80-d baseline. Data were retrieved from the Mikulski Archive for Space Telescopes and reduced as described by Hoffmann et al. (2016) and Riess et al. (2016). An *HST*/WFC3 image of NGC 3972 is shown in Fig. 1.

Photometry was performed with DAOPHOT/ALLSTAR (Stetson 1987) and ALLFRAME (Stetson 1994) using point spread functions



**Figure 1.** 90 arcsec  $\times$  160 arcsec *HST*/WFC3 F350LP image of NGC 3972. The image is generated from the stack of all F350LP data and the intensity scale is logarithmic. To aid orientation, a compass rose is shown, with each arrow corresponding to 5 arcsec. The positions of Cepheid variables used to determine the distance to NGC 3972 are marked with red circles.

created with TINYTIM (Krist, Hook & Stoehr 2011) as described by Macri et al. (2006), Riess et al. (2009, 2011), and Hoffmann et al. (2016).

## 2.2 *HST* spectra of SN 2011by

Optical spectra of SN 2011by were obtained with *HST*/STIS (Programme GO–12298; PI: Ellis). STIS produces excellent absolute and relative spectrophotometry, and therefore the relative luminosity as a function of wavelength for similar-phase spectra can be used to determine the relative reddening of two twin SNe.

SN 2011by was observed with STIS on five epochs, although only two use an UV setting. The two UV/optical spectra were presented by Maguire et al. (2012, but only the optical portion), FK13, and G15. The remaining spectra are first presented here. The data were reduced using the standard *HST* Space Telescope Science Data Analysis System (STSDAS) routines to bias-subtract, flat-field, extract, wavelength-calibrate, and flux-calibrate each SN spectrum. Similar reductions were performed for the SN 2011fe spectra used in this study (Foley et al. 2012b, 2014, 2016; Foley & Kirshner 2013; Foley 2013; Pan et al. 2015). A log of all observations is presented in Table 1. The SN 2011by spectra are shown in Fig. 2.

## 3 ANALYSIS

### 3.1 Selecting Cepheids in NGC 3972

First, the F350LP light curves of all sources were examined to determine the subset that are variable. We visually inspected the light curves and rejected obviously spurious photometry and photometry with unusually large uncertainties. The Welch–Stetson

**Table 1.** *HST*/STIS spectral observations of SN 2011by.

Phase <sup>a</sup>	UT date	Exposure (s) <sup>b</sup>
−9.1	2011 April 30.522	8300 + 2263 <sup>c</sup>
−4.7	2011 May 5.139	0 + 2263
−0.4	2011 May 9.343	5316 + 2263 <sup>d</sup>
3.0	2011 May 13.749	0 + 2263
8.8	2011 May 18.203	0 + 2263

*Notes.* <sup>a</sup>Days since *B* maximum, 2014 February 2.0 UT (JD 2,456,690.5).

<sup>b</sup>First and second numbers correspond to the time for the G230L and G430L gratings, respectively.

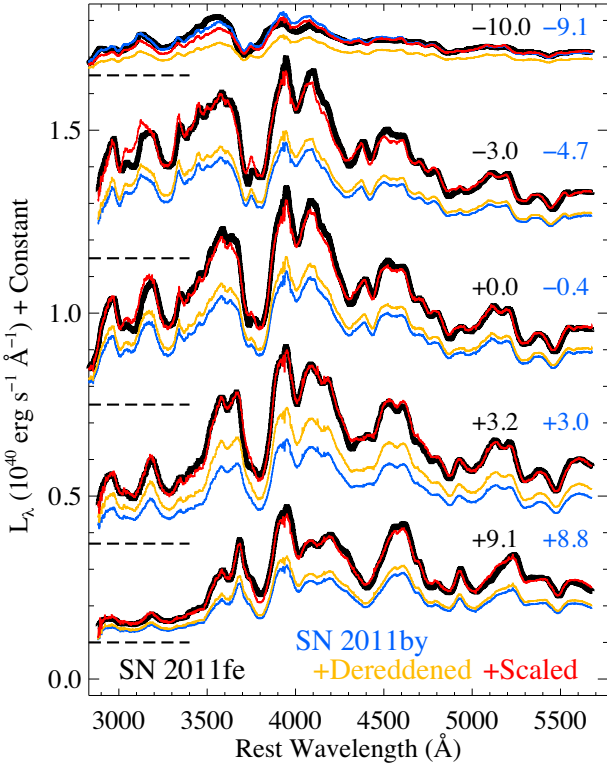
<sup>c</sup>Originally published by G15.

<sup>d</sup>G430L data originally published by Maguire et al. (2012); and G230L data originally published by FK13.

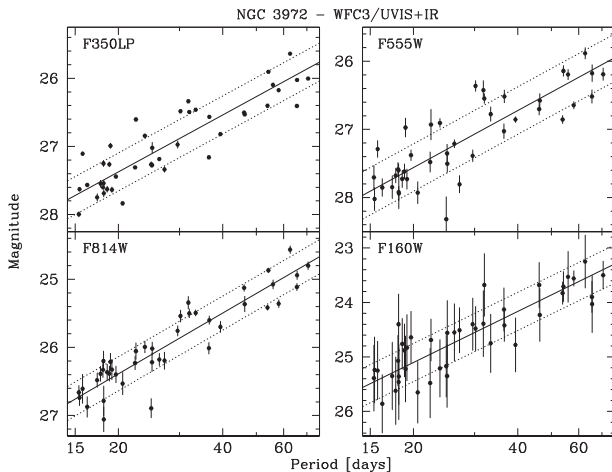
variability index (Stetson 1996) was used to determine which objects are variable.

We matched the light curves of all sources with template Cepheid light curves (Yoachim et al. 2009) of periods between 10 and 100 d. All data (regardless of band) were used for the fitting. From the best-fitting period, the model predicts a corresponding amplitude. Comparing the predicted amplitude to the F350LP light curve, we measured the  $\chi^2$  statistic. More than 90 per cent of the objects selected as variable were poorly matched by the Cepheid template light curves. For the remaining subset, we further refined the best-fitting parameters. Finally, we used additional criteria to remove objects that are inconsistent with isolated low-to-moderate-reddening Cepheids.

In total, we selected 71 Cepheids. We present a finding chart of NGC 3972 with the Cepheids marked in Fig. 1. Details of the selection process can be found in Hoffmann et al. (2016).



**Figure 2.** *HST*/STIS spectra of SNe 2011by (blue curves) and 2011fe (black curves) for five matched phases with each phase labelled next to the spectra. The spectra have been scaled by their geometric dilution factor so that they are in  $L_\lambda$  units. The spectra have been shifted vertically by arbitrary amounts indicated by the dashed lines. Also plotted are the SN 2011by spectra after being dereddened (gold curves) and scaled (red curves) to match the corresponding SN 2011fe spectra using the best-fitting values for both  $E(B - V)$  and the scale factor, as discussed in the text. For all but the first epoch, the similarity in spectral shape and features is striking.



**Figure 3.** Period–luminosity relations (Leavitt laws) for the Cepheid variables in NGC 3972 in the *HST*/WFC3 F350LP (upper left), F555W (upper right), F814W (lower left), and F160W (lower right) filters.

### 3.2 Cepheid distance for NGC 3972

As was done by Riess et al. (2016), we use the period–luminosity relation (Fig. 3), correcting for metallicity, and a combination of

NGC 4258, the Milky Way, and the Large Magellanic Cloud (LMC) as an anchor to determine the distance of NGC 3972. We refer the reader to Riess et al. (2016) for details of this calculation.

For all measured Cepheids, we determine the Wesenheit magnitude (Madore 1982), which corrects for extinction and the finite temperature width of the instability strip. We compute a period–luminosity relation and remove significant outliers as well as Cepheids with periods below the completeness limit (see Riess et al. 2016). Fig. 3 displays the final period–luminosity relation for NGC 3972, consisting of 42 Cepheids. The Cepheid data imply a distance modulus of  $31.594 \pm 0.071$  mag.

Additionally, we can directly compare the Cepheid data for NGC 3972 and M101 to determine their relative distances without the uncertainties of the absolute distance scale. The relative distance is particularly important for comparing SNe 2011by and 2011fe. Directly comparing the Cepheid data for both galaxies and accounting for covariances in the measurements, we determine that NGC 3972 has a distance modulus that is  $2.459 \pm 0.062$  mag greater than that of M101.<sup>1</sup>

### 3.3 Luminosity differences for SNe 2011by and 2011fe

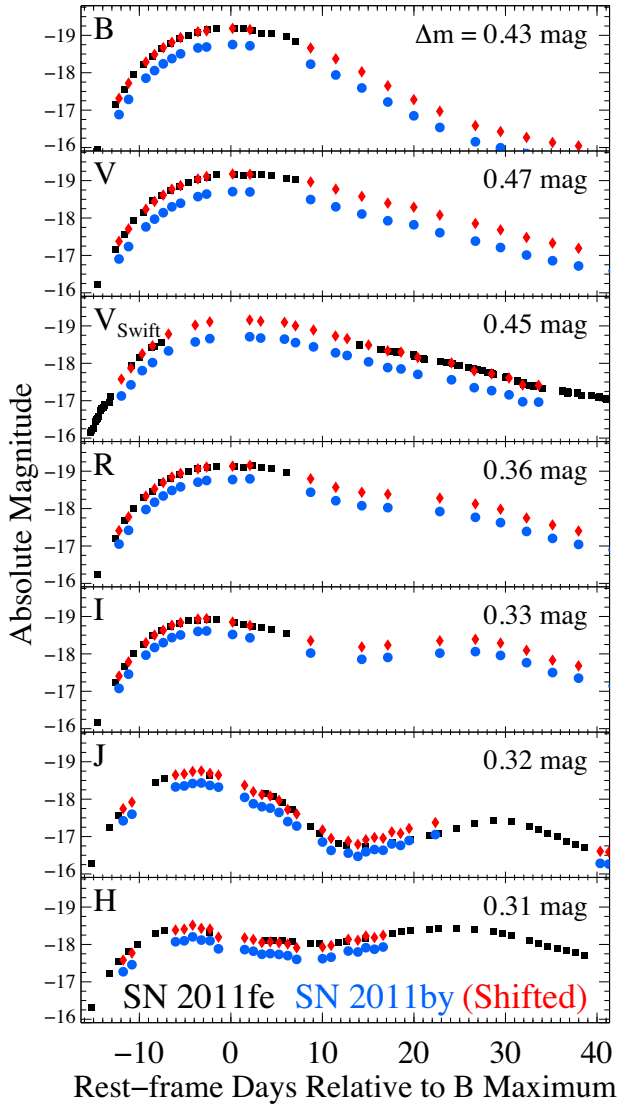
With the absolute and relative distances to M101 and NGC 3972, we can directly compare the observations of SNe 2011by and 2011fe on an absolute scale. However, to do this, one must correct for any host-galaxy extinction. While previous studies have suggested that both SNe are consistent with having zero reddening, SN 2011by is slightly redder than SN 2011fe. In order to account for the possibility of a different reddening for each SN and a coherent, grey offset in their absolute magnitudes, we simultaneously fit for both.

Conveniently, SNe 2011by and 2011fe were both observed by *Swift* (Brown et al. 2012; Milne et al. 2013) and the Lick Observatory 0.76 m Katzman Automatic Imaging Telescope (KAIT; Silverman, Ganeshalingam & Filippenko 2013; Zhang et al. 2016), making  $S$ -corrections (Stritzinger et al. 2002) unnecessary (and thus removing one potential systematic uncertainty). Unfortunately, near peak brightness, SN 2011fe was too bright to have accurate flux measurements in the *Swift*  $UBV$  bands. As a result, there is a small phase range of only a few days, far from peak, where both SNe have *Swift*  $B$  photometry; it is therefore difficult to determine a precise offset in this band and these data are not used in our analysis. Because of potential intrinsic UV differences among the two SNe, we also do not use the  $U$  band (and bluer bands) *Swift* data to measure the reddening. However, both SNe have sufficient overlap in *Swift*  $V$  to determine a magnitude offset in that band.

Additionally, Matheson et al. (2012) observed SN 2011fe in  $JH$  and Friedman et al. (2015) observed SN 2011by in  $JHK_s$ . While each SN was observed with different telescopes, instruments, and slightly different filters, we were able to determine the necessary  $S$ -corrections using the SN 2011fe near-IR (NIR) spectral sequence (Hsiao et al. 2013) and the available filter functions<sup>2</sup> (Cohen, Wheaton & Megeath 2003). This process is similar to what was done by Weyant et al. (2018) for comparing SNe Ia in these two systems.

<sup>1</sup>We use the Riess et al. (2016) determination of the Cepheid distance for M101 ( $\mu = 29.14$  mag) rather than that of Shappee & Stanek (2011,  $\mu = 29.04$  mag). Primarily, this is so that both galaxies have consistent methodology. However, we note that the measurements are consistent (to within 0.01 mag) when the same LMC or NGC 4258 zero-points are used.

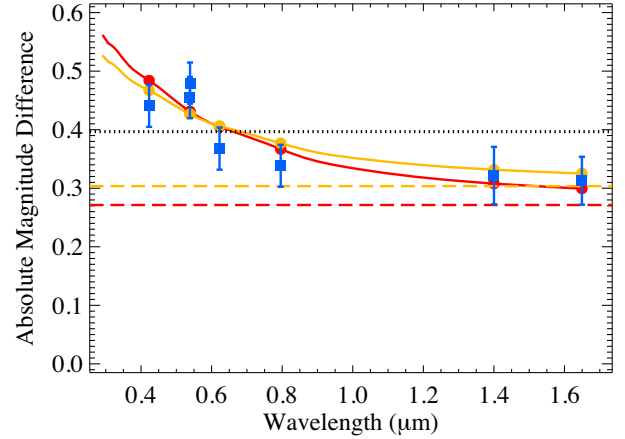
<sup>2</sup><https://www.noao.edu/kpno/manuals/whirc/filters.html>



**Figure 4.** Optical and NIR light curves of SNe 2011by (blue circles) and 2011fe (black squares) in KAIT *BVRI*, *Swift V*, and *JH* bands. The red diamonds represent the SN 2011by light curve shifted by a single magnitude for each band, noted in each subpanel, to match the luminosity of SN 2011fe.

Using their peak-brightness spectra, we measured a  $K$ -correction for each SN. The relative  $K$ -correction was  $<0.012$  mag for all bands.

Correcting for Milky Way extinction (Schlafly & Finkbeiner 2011),  $K$ -corrections,  $S$ -corrections (for *JH*), and their distances, we produce absolute magnitude light curves in *BVRJH*, which we present in Fig. 4. We note that the absolute magnitude light curves are not corrected for any potential host-galaxy extinction. To determine the relative magnitude offset in each band, we use a b-spline function to interpolate each light curve to match the phases for the other light curve. We then fit for an offset between the two light curves. These offsets, as a function of effective filter wavelength (as determined from the peak-brightness SN 2011fe spectrum), are presented in Fig. 5. In all bands, SN 2011fe is 0.31 to 0.48 mag more luminous than SN 2011by, with bluer bands having a larger offset. As a cross-check, Dhawan, Jha & Leibundgut (2018) found a difference in the peak absolute *J* magnitude of 0.30 mag,



**Figure 5.** Absolute magnitude difference between SNe 2011by and 2011fe as a function of wavelength. The blue squares show the KAIT *BVRI*, *Swift V*, and *JH* bands. The effective wavelength for each point is determined by convolving the filter transmission functions with the peak-brightness spectrum. The blue curve represents the difference in their peak-brightness *HST/STIS* spectra. The black dotted line illustrates the best-fitting constant offset to all data. The red and gold solid lines represent the best-fitting reddening and offset model (using a Fitzpatrick 1999 reddening law with  $R_V = 3.1$ ) when only fitting the photometry and varying the reddening, and using spectral matches to determine the reddening and the photometry to determine the offset, respectively. The red and gold dashed lines display the corresponding constant offsets. Our best-estimate reddening is  $E(B - V) = 0.039 \pm 0.006$  mag and best-estimate constant offset is  $0.304 \pm 0.062$  mag, which corresponds to the gold dashed line.

comparable to our full light-curve *J*-band offset of 0.32 mag, using the same data. The average offset in all bands is  $0.397 \pm 0.014$  mag, but a single offset for all bands does not fit the data well, having  $\chi^2/\text{d.o.f.} = 19.7/6$ .

Notably, the offset between SNe 2011by and 2011fe in a given band is similar at all epochs probed by the photometry. The one exception is for the *J* band for phases between  $\sim 10$  and  $\sim 25$  d after peak brightness. This indicates that the intrinsic colour evolution for the SNe is similar and that the offsets in a given band are primarily caused by slow-changing attributes such as a luminosity offset and dust extinction.

Assuming that the change in absolute magnitude offset with wavelength is caused by differential dust reddening, we simultaneously fit for a constant offset and dust reddening. Using either a Cardelli, Clayton & Mathis (1989) or Fitzpatrick (1999) reddening law, and fixing  $R_V$  to be 3.1, we find consistent reddening values (differing by 0.001 mag with  $\chi^2/\text{d.o.f.} = 5.2/4$  and  $5.0/4$ , respectively) with  $E(B - V) \approx 0.047$  mag. If we allow  $R_V$  to float, then we find best-fitting values for  $E(B - V)$  of  $\sim 0.038$  mag (the choices differ by 0.004 mag with  $\chi^2/\text{d.o.f.} = 5.3/5$  and  $5.1/5$ , respectively) with  $R_V \approx 4.2$ . Regardless of the choice of reddening law, there remains a constant, grey offset of  $\sim 0.27$  mag (the choices differ by 0.01 mag). For our final analysis, we use the Fitzpatrick (1999) reddening law.

To further constrain the reddening, we examine the spectrophotometry of SNe 2011by and 2011fe. Optical spectra of both SNe were obtained with *HST/STIS*. SN 2011fe was observed on ten separate epochs covering phases of  $-13$  to  $+40$  d (Maguire et al. 2012; Foley 2013; Foley & Kirshner 2013; Mazzali et al. 2014).

We match each SN 2011by spectrum to an SN 2011fe spectrum with a similar phase (to within  $\sim 1$  d). Specifically, the  $-9.1$ ,  $-4.7$ ,  $-0.4$ ,  $3.0$ , and  $8.8$ -d SN 2011by spectra are matched to  $-10.0$ ,

–3.0, 0.0, 3.2, and 9.1-d SN 2011fe spectra, respectively. With a small phase difference between spectra, spectral feature differences should be minimal, especially for such similar SNe. After correcting for Milky Way reddening and their distances, each SN 2011by spectrum is dereddened (to account for potential host-galaxy reddening) and scaled to match its corresponding Milky-Way-dereddened SN 2011fe spectrum. Since the phases are not perfectly matched, we do not expect the flux scaling, which corresponds to an achromatic offset, to be correct; however, the colour evolution between these epochs should generally be small, allowing for an accurate measurement of the reddening. This method is graphically outlined in Fig. 2.

Using a Fitzpatrick (1999) reddening law with  $R_V = 3.1$ , we find that the reddening of SN 2011by (relative to SN 2011fe) ranges from  $E(B - V) = -0.11$  mag (i.e. SN 2011fe is redder) to 0.06 mag, with 3/5 of the epochs having  $E(B - V) = 0.023$  to 0.027 mag. Only the first epoch has ‘negative reddening,’ which we consider to be the result of a combination of a quickly changing spectral-energy distribution (SED) at these early times and a phase difference of 0.9 d. Ignoring the first epoch, the remaining epochs have an average reddening of  $E(B - V) = 0.039 \pm 0.006$  mag, which we consider to be our best estimate of the host-galaxy reddening of SN 2011by relative to that of SN 2011fe. Fixing the reddening to this value, the best-fitting coherent absolute magnitude offset is  $0.303 \pm 0.006$  mag. We note that the uncertainty on this number neglects the distance uncertainty and reddening uncertainty (as the reddening was fixed).

Assuming no host-galaxy dust reddening for SN 2011fe and  $E(B - V) = 0.039 \pm 0.006$  mag for SN 2011by, the peak  $V$ -band absolute magnitude for each SN is  $-19.18 \pm 0.05$  and  $-18.85 \pm 0.07$  mag, respectively. The majority of the uncertainties in these values is related to the distances, as determined from the Cepheid measurements. Since the distance estimates are obtained through the same method, several sources of uncertainty do not apply to a relative distance measurement. Taking our best estimates for different terms, we can determine the relative peak  $V$ -band absolute magnitude and uncertainty,

$$\Delta M_V = \Delta m - \Delta E(B - V)R_V - \Delta \mu, \quad (1)$$

$$\sigma_{\Delta M_V} = \left( \sigma_{\Delta m}^2 + (3.1\sigma_{E(B-V)})^2 + \sigma_{\Delta \mu}^2 \right)^{1/2}, \quad (2)$$

with parameters and uncertainties

$$(\Delta m, \Delta E(B - V), R_V, \Delta \mu) = (2.93, 0.044, 3.1, 2.449), \quad (3)$$

$$(\sigma_{\Delta m}, \sigma_{E(B-V)}, \sigma_{\Delta \mu}) = (0.007, 0.006, 0.062), \quad (4)$$

where  $\Delta E(B - V)$  is the total difference in reddening, including the Milky Way contribution. We therefore find

$$\Delta M_V = 0.335 \pm 0.063 \text{ mag}, \quad (5)$$

with SN 2011fe being more luminous. Simultaneously fitting the reddening and an achromatic offset, we find  $\Delta M_V = 0.342 \pm 0.065$  mag. The difference is consistent with, but smaller than, that found by FK13:  $0.60 \pm 0.36$  mag. It is also consistent with the Riess et al. (2016) difference (0.286 mag), which only used optical light-curve data. If one also makes a 0.06 mag host-mass correction (e.g. Kelly et al. 2010; Lampeitl et al. 2010; Sullivan et al. 2010; see Section 4), there is no difference between our measurement and that of Riess et al. (2016). With the updated relative distances, we find that SNe 2011by and 2011fe had peak  $V$ -band absolute magnitudes which were significantly different, with a significance of  $4.9\sigma$ . Furthermore, we find a coherent, reddening-

**Table 2.** Supernova and host-galaxy properties.

Parameter	SN 2011by	SN 2011fe
Galaxy	NGC 3972	M101
$\mu$ (mag)	31.594 (0.071)	29.135 (0.047)
$V_{\text{peak}}$ (mag)	12.91 (0.01) <sup>F</sup>	9.98 (0.02) <sup>P</sup>
$\Delta m_{15}(B)$ (mag)	1.14 (0.03) <sup>S</sup>	1.10 (0.04) <sup>P</sup>
$E(B - V)_{\text{MW}}$ (mag)	0.013	0.008
$E(B - V)_{\text{host}}$ (mag)	0.039 (0.006)	0
$M_{V, \text{peak}}$ (mag)	-18.85 (0.07)	-19.18 (0.05)
Peak bolometric luminosity ( $10^{42}$ erg s <sup>-1</sup> )	9.3 (0.7)	12.9 (0.7)
<sup>56</sup> Ni mass ( $M_{\odot}$ )	0.43 (0.09)	0.59 (0.12)
$M_{V, \text{peak}}$ offset (mag)	0.33 (0.07)	0
<sup>56</sup> Ni mass ratio (related to 11by)	1	1.38 (0.09)
P99 $M_{V, \text{peak}}$ offset (mag)	0.028 (0.022)	0
SALT $\mu$ (mag)	31.96 (0.04)	29.16 (0.06)
SALT $M_B$ offset (mag)	0.16 (0.08)	0
Cepheid-SN $\mu$ Offset (mag)	-0.14 (0.08)	+0.15 (0.08)

Notes. F = FK13; P = Pereira et al. (2013); and S = Silverman et al. (2013).

free (Wesenheit) offset of  $0.314 \pm 0.062$  mag, corresponding to a significance of  $5.1\sigma$ .

We present summary information before both SNe in Table 2 and an updated absolute  $V$ -band light curves in Fig. 6 to illustrate these differences. This figure uses an expanded set of light-curve data from a variety of sources (see G15, and references therein) to show the full evolution of SNe 2011by and 2011fe for  $\sim 1$  yr after explosion.

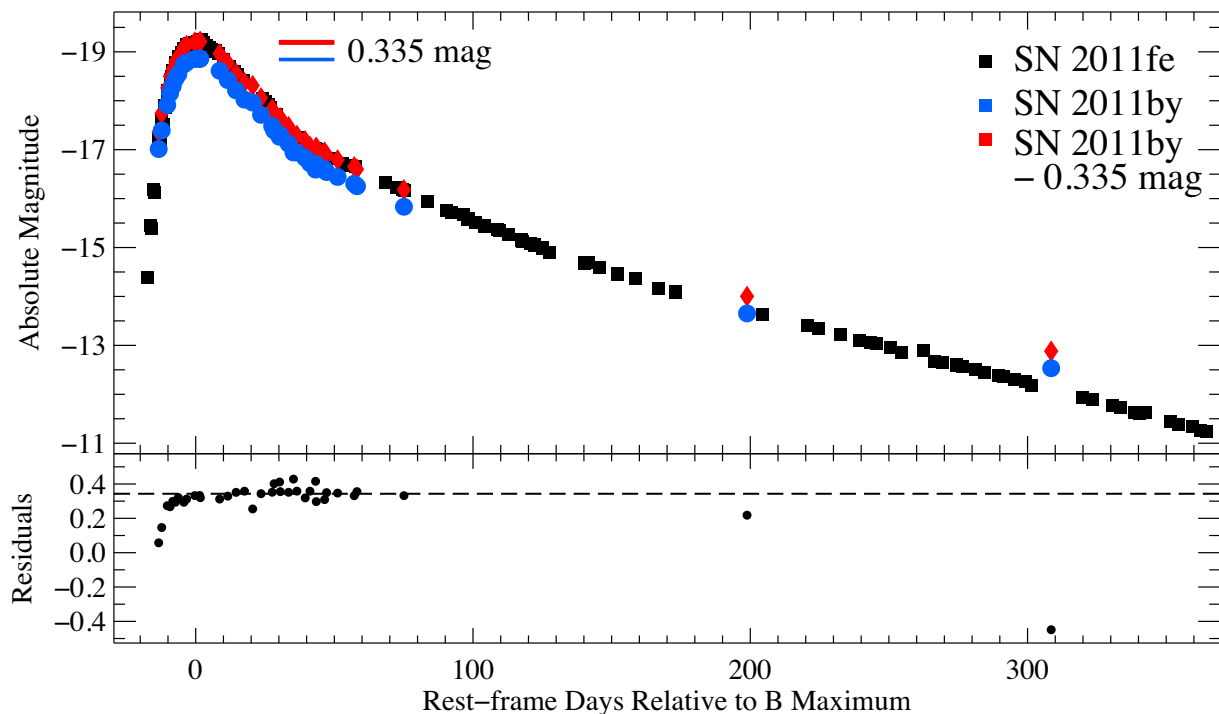
The grey magnitude offset corresponds to a difference in peak bolometric luminosity. SNe 2011by and 2011fe have practically indistinguishable maximum-light (as well as essentially all other epochs) optical spectra (FK13, G15), light-curve shapes (FK13), and colour curves (G15). Therefore, their bolometric corrections must be similar. While their UV spectra are different, this will have a minor effect on the bolometric luminosity (at most a few per cent); it is also in the direction of SN 2011fe having a higher bolometric luminosity than of SN 2011by, which would make their luminosities even more discrepant. While it is possible that their mid-IR and far-IR emission is significantly different, this is unlikely given all other evidence, and should have a small overall effect on the bolometric luminosity.

To determine the peak bolometric luminosity, we use the peak spectra for the two SNe (FK13), which cover the rest-frame wavelengths  $\sim 1600\text{--}10\,200$  Å for both SNe. We then extend the spectra to the NIR by extrapolating an 18 000 K blackbody whose flux is matched to the optical data. Since we mostly care about the relative luminosities, the exact NIR SED is not especially important. Integrating the spectra and using the distance measurements for each SN, we find peak bolometric luminosities of  $(9.3 \pm 0.7) \times 10^{42}$  and  $(12.9 \pm 0.7) \times 10^{42}$  erg s<sup>-1</sup> for SNe 2011by and 2011fe, respectively.

To determine the <sup>56</sup>Ni mass, we use the common formula,

$$M_{^{56}\text{Ni}} = \frac{L_{\text{bol, max}}}{\alpha \dot{S}(t_{\text{r, bol}})}, \quad (6)$$

where  $\alpha$  is a unitless parameter of order unity that describes the diffusion of radiation through the ejecta,  $\dot{S}$  is the instantaneous rate of energy injection from radioactive decay, and  $t_{\text{r, bol}}$  is the bolometric rise time (see e.g. Arnett 1982; Jeffery 1999). For this analysis, we use  $\alpha = 1 \pm 0.2$ , which is a common choice (e.g. Stritzinger et al. 2006). Others have chosen a slightly higher value for  $\alpha$  ( $\alpha = 1.2 \pm 0.2$ ; Scalzo et al. 2010; Pereira et al. 2013);



**Figure 6.** Top: absolute  $V$ -band light curves of SNe 2011by (blue circles) and 2011fe (black squares) as presented by G15, but adjusted to account for the new distances to each SN and the measured host-galaxy extinction for SN 2011by. The SN 2011fe light curve is a combination of data from Richmond & Smith (2012), G15, and Zhang et al. (2016). The SN 2011by data are from Silverman et al. (2013) and G15. Also plotted is the SN 2011by light curve shifted by 0.335 mag, corresponding to the difference in peak brightness between the two SNe. Bottom: difference between the absolute  $V$ -band light curves for SN 2011by and SN 2011fe, where the SN 2011fe light curve was interpolated to match the epochs of the SN 2011by observations. The dashed line is at 0.335 mag.

however, the exact choice does not affect our main result, which examines the ratio of  $^{56}\text{Ni}$  masses.

For this analysis, we use a bolometric rise time of  $t_{r, \text{bol}} = 16.58 \pm 0.14$  d for SN 2011fe (Pereira et al. 2013), and assume that SN 2011by has the same rise time. This assumption is reasonable given the similar light-curve shapes and colour curves for the two SNe. We note that there is some evidence of SN 2011by having a slightly slower  $V$ -band rise (Fig. 6); however, G15 found that the SN 2011fe rise time was  $0.6 \pm 0.4$  d longer than that of SN 2011by (opposite of what one might immediately assume from the differences in the  $V$  band). Changing the rise time by a day in either direction only affects the SN 2011by  $^{56}\text{Ni}$  mass by  $0.02 M_{\odot}$ . Using equation (6), we find  $^{56}\text{Ni}$  masses of  $0.43 \pm 0.09$  and  $0.59 \pm 0.12 M_{\odot}$  for SNe 2011by and 2011fe, respectively, where the largest component of the uncertainty is from  $\alpha$ .

For the above calculation, we propagated the uncertainty from several different sources (rise time,  $\alpha$ , etc.) that are likely the same for both SNe. In the scenario where these values are the same for both SNe, but the exact value is uncertain, we can measure the ratio of the  $^{56}\text{Ni}$  masses with an uncertainty which does not include the uncertainties of these different values. Doing this, we find a  $^{56}\text{Ni}$  ratio of  $M_{11\text{fe}}(^{56}\text{Ni})/M_{11\text{by}}(^{56}\text{Ni}) = 1.38 \pm 0.09$ . This value is similar to that found by FK13 (1.7), but slightly lower, which is unsurprising given the similar, but slightly different luminosities for the two analyses. With the assumptions listed above, the two SNe have significantly different  $^{56}\text{Ni}$  masses, with  $4.2\sigma$  significance.

### 3.4 Light-curve distance estimates

In the previous section, we determined that SNe 2011by and 2011fe had significantly different luminosities and  $^{56}\text{Ni}$  masses.

However, these SNe do not fall outside the range of all SNe Ia. For measuring distances with SNe Ia, differences in light-curve shape and colour make SNe with different intrinsic luminosities have similar *corrected luminosities*. SNe 2011by and 2011fe have very similar observational properties, and thus it would be unlikely for these twin SNe to have the significantly different corrected luminosities.

None the less, we go through this exercise below. Importantly, we must consider the intrinsic scatter for a given distance-fitting algorithm to determine the significance of any difference. The intrinsic scatter indicates how much diversity in distances there is after correcting for photometric parameters and can be the result of additional physical conditions such as metallicity. If SNe 2011by and 2011fe are different by less than the intrinsic scatter, they would not represent outliers for measuring cosmological parameters. However, whatever causes the differences in their peak luminosity would likely contribute to the overall intrinsic scatter measured for large samples of objects.

The simplest approach to determine the expected difference in  $M_{V, \text{peak}}$  is to use the decline-rate parameter,  $\Delta m_{15}(B)$ . Phillips et al. (1999) determined empirical equations for this relation that are independent of colour. For the  $V$  band, they find

$$\Delta M_{V, \text{peak}} = 0.672(\Delta m_{15}(B) - 1.1) + 0.633(\Delta m_{15}(B) - 1.1)^2, \quad (7)$$

where the difference is explicitly relative to an SN with  $\Delta m_{15}(B) = 1.1$  mag. Since SN 2011fe conveniently has exactly this value, the equation can be used to determine the expected difference between SNe 2011by and 2011fe, yielding  $0.028 \pm 0.022$  mag, with SN 2011fe expected to be slightly (insignificantly) more luminous. As

expected, based on the light-curve shape alone, the two SNe are expected to have nearly identical peak luminosities.

One can now test how different the relative distances derived from the light-curve shape and apparent brightness of SNe 2011by and 2011fe are from those directly measured from Cepheids. The difference between these two methods reduces to a difference in peak absolute magnitudes, as determined by both methods. This difference is  $0.44 \pm 0.07$  mag, having a  $6.1\sigma$  significance level.

We also used the Spectral Adaptive Light curve Template 2 (SALT2) algorithm (Guy et al. 2007) to determine the distances and peak absolute magnitudes of the two SNe. SALT2 simultaneously fits multiple light curves, which should include subtle differences in colour and light-curve shape in any distance estimate. However, SALT2 is limited to measuring distances from optical light curves.

The difference between SALT2-estimated *B*-band absolute magnitudes is  $0.16 \pm 0.08$  mag, consistent with that found with the Phillips et al. (1999) method, and consistent with zero offset in absolute magnitude. Since the SALT2 method corrects for colour differences, which could be caused by reddening, this difference could be caused simply by the SALT2 treatment of extinction. To test this possibility, we determine the difference in  $A_B$  estimated from a direct comparison of the SN light curves,

$$\begin{aligned} A_B &= R_B \times E(B - V) = 4.1 \times (0.039 \pm 0.006) \text{ mag} \\ &= 0.160 \pm 0.025 \text{ mag}, \end{aligned} \quad (8)$$

which is identical to the difference in  $M_B$  measured by SALT2. Therefore, SALT2 is measuring the slight colour difference between the two SNe, but is incapable of measuring the grey offset between them. In other words, SALT2 expects SNe 2011by and 2011fe to have the same intrinsic luminosities. As a result, the difference in Hubble residuals (HRs) for the two SNe is approximately the difference between the reddening-uncorrected  $\Delta M_V$  and the SALT2 difference:  $\Delta HR = 0.33$  mag. This is similar to what was seen by Riess et al. (2016), finding  $\Delta HR = 0.29$  mag using SALT2.

Riess et al. (2016) found that SNe 2011by and 2011fe have HRs of  $-0.14$  and  $0.15$  mag, respectively, making neither an outlier relative to the scatter. On the other hand, it is perhaps a coincidence that SN 2011by is faint relative to the mean of the sample and SN 2011fe is bright relative to the mean of the sample. If either SN 2011by (SN 2011fe) were replaced with a true copy of SN 2011fe (SN 2011by), the mean absolute magnitude of the 19 Cepheid-SN calibrators would shift by  $-0.016$  mag ( $+0.019$  mag). This shifts the value of  $H_0$  by 0.72 per cent to 0.86 per cent, changing the best-estimate Riess et al. (2016) value of  $H_0$  of  $73.24 \text{ km s}^{-1} \text{ Mpc}^{-1}$  to  $72.71$  and  $73.87 \text{ km s}^{-1} \text{ Mpc}^{-1}$ , respectively. This would be a small change to the value of  $H_0$ ; however, the relatively small size of the Cepheid-SN calibrator sample, where individual objects can influence the measured value of  $H_0$ , will clearly be a limiting factor in the very near future.

#### 4 DISCUSSION AND CONCLUSIONS

We find that SNe 2011by and 2011fe, despite having nearly identical optical spectral sequences (G15) and light-curve shapes/colours (FK13, G15), have different peak luminosities. This result is similar to that of FK13 — but with our new Cepheid distance to NGC 3972, this result is highly statistically significant. The observations suggest that SN 2011fe generated 38 per cent more  $^{56}\text{Ni}$  than SN 2011by. Furthermore, the differences in luminosity are significantly larger than the intrinsic luminosity scatter for SNe Ia.

The one substantial luminosity-independent observational difference between SNe 2011by and 2011fe is their near-peak UV flux

difference (FK13, G15). SN 2011fe had relatively more UV flux and a higher peak bolometric luminosity than SN 2011by, both of which were predictions for an SN with relatively low progenitor metallicity (Timmes et al. 2003; Mazzali & Podsiadlowski 2006). Although there could be alternative explanations, our current observations are consistent with the explanation that the progenitors of SNe 2011by and 2011fe had supersolar and subsolar metallicities, respectively (FK13; Mazzali et al. 2014, G15).

Recent work by Pan et al. (2019) finds a correlation between host-galaxy metallicity and the UV continuum of SNe Ia after controlling for light-curve shape and colour. Specifically, SNe Ia located in high-metallicity host galaxies tend to have lower UV flux ( $\lambda < 2700 \text{ \AA}$ ) than those from low-metallicity host galaxies. This is similar to the trend seen between SNe 2011by and 2011fe if present-day host-galaxy metallicity is a reasonable proxy for progenitor metallicity.

If SNe Ia were perfectly described by their optical light-curve shape and colour, then SNe 2011by and 2011fe should have the same peak luminosity. The difference in luminosities indicates that additional unaccounted physics must increase the scatter of SN Ia measurements beyond errors in analysis. This comparison indicates that progenitor metallicity is likely a large component of the ‘intrinsic scatter.’ However, current distance estimators do not consider SNe 2011by and 2011fe significantly different (in part because of their internal model uncertainties and in part because of the intrinsic scatter), and thus neither would necessarily be excluded from a cosmological analysis. Their inclusion as SN-Cepheid calibrators has a minimal impact on the value of  $H_0$ , but will be limiting in the near future if the size of the calibrator sample is not increased significantly.

Recent cosmological analyses have found a significant offset in the average HR between SNe Ia in low- and high-mass galaxies (Kelly et al. 2010; Lampeitl et al. 2010; Sullivan et al. 2010). Although the exact functional form of any relation is not known (e.g. Childress et al. 2013), a correction is often applied as a step function in host-galaxy stellar masses with the step at  $10^{10} M_\odot$ . While this effect has not been significant in all analyses (e.g. Scolnic et al. 2018; Brout et al. 2019), a typical value for the difference is  $\sim 0.06$  mag, with SNe Ia in low-mass galaxies being fainter. Our results are broadly consistent with this trend, where NGC 3972 and M101 have stellar masses below and above  $10^{10} M_\odot$ , respectively. It is therefore possible that the mass step is driven primarily by metallicity differences in the progenitor systems which correlate with the host galaxy’s total stellar mass at the time of explosion.

A recent analysis of ‘twin’ SNe Ia suggested a low intrinsic dispersion of only 0.08 mag (Fakhouri et al. 2015). SNe 2011by and 2011fe are, by all accounts, better twins than those presented by Fakhouri et al. (2015), yet they have a peak absolute magnitude difference that is  $\sim 4$  times larger than the scatter for their sample. While choosing SNe Ia with similar spectral properties should not typically increase scatter, the incredibly well observed and precisely measured SNe 2011by and 2011fe provide a cautionary tale for using this method for improving distance estimates.

Future analyses must evaluate how this result will affect their conclusions. Obviously, there is additional information in the UV SED, and observing the rest-frame UV could potentially improve SN Ia distance estimates. However, if the average progenitor metallicity is changing with redshift (e.g. Childress, Wolf & Zahid 2014), there may be a systematic bias to SN Ia distances with redshift. As there is some indication of changing UV properties with redshift (Foley et al. 2012a; Maguire et al. 2012; Milne et al. 2015), a thorough analysis of this effect should be performed. In particular, additional UV spectra of low-redshift SNe Ia will be



critical for understanding how progenitor metallicity affects SN Ia distance estimates.

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