

RESEARCH PAPER

# A model for gas transport in pear fruit at multiple scales

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## Abstract

**A two-dimensional multiscale gas exchange model was developed to evaluate the effect of ambient conditions, fruit size, and maturity on intracellular O<sub>2</sub> and CO<sub>2</sub> concentrations in pear fruit via computational analysis. The model consists of interconnected submodels that describe the gas exchange at the macroscopic scale of the fruit and the microscopic scale of the cells. The multiscale model resulted in a comprehensive description of gas exchange at different scales. The macroscale model was used to describe the gas exchange of the fruit under controlled atmosphere conditions while corresponding intracellular concentrations of microstructure tissue were computed from the microscale. Ripening of the fruit increased the risk of physiological disorders, since increased respiration resulted in anoxia in the fruit centre even under typical storage conditions.**

**Key words:** anoxia, controlled atmosphere storage, gas transport, multiscale modelling, pear.

## Introduction

Exchange of O<sub>2</sub> and CO<sub>2</sub> of plants with their environment is essential for metabolic processes such as photosynthesis and respiration. Gas exchange is caused by differences in gas concentrations between the applied external atmosphere and the internal atmosphere of plant organs. In bulky organs, such as fruits and roots, these gradients exist due to O<sub>2</sub> consumption and CO<sub>2</sub> production during respiration and fermentation (Kader, 1988; Geigenberger *et al.*, 2000; Ho *et al.*, 2008). In developing seeds, the combination of respiration and photosynthesis may cause large gradients in gas concentrations (Rolletschek *et al.*, 2003; Borisjuk and Rolletschek, 2009). In leaves, gradients have been observed due to CO<sub>2</sub> assimilation (Morison *et al.*, 2005; Warren, 2008). In some fruits, such as pears, which are typically stored under controlled atmosphere (CA) condition, anoxia may occur, eventually leading to fermentation, which causes a chain of events ultimately leading to cell death, tissue damage, and commercial loss (Franck *et al.*, 2007). For a better understanding of plant metabolism it is important to quantify the metabolic gas exchange and the effect of the external conditions on the intracellular metabolic gas concentration.

Mathematical modelling is a powerful tool to study the mechanisms of gas transport in plant material. Different

approaches to gas transport modelling in plant tissue have been reported, from the macroscale (Mannapperuma *et al.*, 1991; Lammertyn *et al.*, 2003; Ho *et al.*, 2008) to the microscale level (Denison, 1992; Aalto and Juurola, 2002; Ho *et al.*, 2009). In macroscale models, plant material is considered as a continuum, which consists of different interconnected tissues characterized by apparent macroscopic properties of the biological materials (Lammertyn *et al.*, 2003; Ho *et al.*, 2008). Apparent gas transport properties of plant tissue have been determined by measuring gas exchange through small tissue samples (Lammertyn *et al.*, 2001; Schotsmans *et al.*, 2003, Ho *et al.*, 2006a, b). However, plant tissue has a cellular structure. The microscale topology in which individual cells and intercellular space can be distinguished determines to a large extent gas transport in the tissue (Parkhurst and Mott, 1990; Aalto and Juurola, 2002; Mendoza *et al.*, 2007; Verboven *et al.*, 2008). Plant tissue, therefore, cannot be considered as a real continuum material. Inside plant organs such as the fruits, gas is believed to be transported through intercellular spaces (Mendoza *et al.*, 2007; Verboven *et al.*, 2008). O<sub>2</sub> subsequently permeates through the cellular membrane to the cytoplasm and eventually diffuses in the cytoplasm into the

mitochondria where the respiration takes place. The CO<sub>2</sub> produced essentially follows the reverse path.

A microscale gas transport model has been developed to describe gas transport at the cellular level through the intercellular space and cells (Ho *et al.*, 2009). Although such a model provided detailed predictions of the local microscale gas concentrations, a microscale model that covers microscale gas exchange in the entire fruit is currently not feasible because of the excessive computer resources required to solve such a model on the entire microscale topology.

The multiscale modelling paradigm provides an alternative approach to combine the relative simplicity of continuum-type models defined at the macroscale level with the level of detail models incorporating the microscale features. A multiscale gas transport model is basically a hierarchy of models which describe the gas transport phenomena at different spatial scales (see Fig. 1). These models are coupled via computational analysis, in which the model results relevant to a particular spatial scale are linked to simulations at a different spatial scale. Multiscale modelling has been introduced successfully in material science and geoscience (Regenauer-Lieb and Yuen, 2003; Raghavan and Ghosh, 2004; de Pablo and Curtin, 2007) and is also being recognized as a useful tool for biological applications (Seymour, 2001; Wood *et al.*, 2002; Mebatsion *et al.*, 2008). In this contribution, a multiscale model will be introduced and validated to perform a computational analysis of gas exchange in plant materials at different scales. Pear fruit was chosen as a model system. Since ripening fruit is more susceptible to storage disorder (Veltman *et al.*, 1999; Lammertyn *et al.* 2000; Franck *et al.*, 2003), the model will be applied to evaluate the effect of environmental con-

ditions, fruit size, and maturity on cellular respiration and the risk of local fermentative conditions.

## Materials and methods

### Materials

Pears (*Pyrus communis* ‘Conference’) were harvested on 20 August 2007, at the pre-climacteric stage at the Fruitteeltcentrum (Rillaar, Belgium), cooled, and stored according to commercial protocols for a period of 21 d at -1 °C followed by CA storage (2.5 kPa O<sub>2</sub>, 0.7 kPa CO<sub>2</sub> at -1 °C) until they were used for the experiments. These fruit were considered as the control treatment and will be further designated as ‘control fruit’; some fruit were stored for another 7 d at 20 °C in ambient air as a ripening treatment and will be designated as ‘ripe fruit’.

### Continuum model of gas exchange in intact fruit

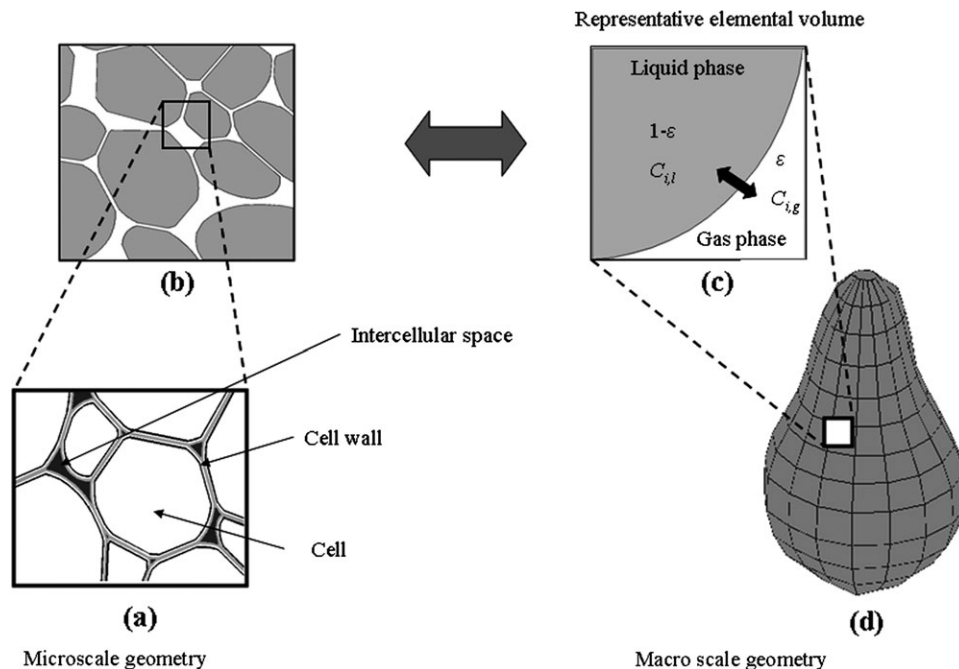
At the macroscopic spatial scale, the fruit tissue was considered as a continuum of material. A permeation–diffusion–reaction model (Ho *et al.*, 2008) was applied to study gas exchange due to respiration of intact fruit with the environment:

$$\alpha_i \frac{\partial C_i}{\partial t} + \nabla \cdot (\mathbf{u} C_i) = \nabla \cdot D_i \nabla C_i + R_i \quad (1)$$

$$C_i = C_{i,\infty} \quad (2)$$

where  $\alpha_i$  is the gas capacity of component  $i$  in the tissue and  $C_i$  (mol m<sup>-3</sup>) is the concentration of gas  $i$  (O<sub>2</sub>, CO<sub>2</sub>, N<sub>2</sub>). In the equations,  $D_i$  (m<sup>2</sup> s<sup>-1</sup>) is the apparent diffusion coefficient,  $\mathbf{u}$  (m s<sup>-1</sup>) the apparent velocity vector,  $R_i$  (mol m<sup>-3</sup> s<sup>-1</sup>) the production term of the gas component  $i$  related to O<sub>2</sub> consumption or CO<sub>2</sub> production, and  $t$  (s) the time. The index  $\infty$  refers to the gas concentration of the ambient atmosphere.

Gas partial pressure gradients were considered to be the driving force for diffusive gas transport. Differences in diffusion rates of



**Fig. 1.** Multiscale hierarchy of pear geometry. (a) Detailed microstructure of tissue; (b) and (c) tissue and its representative elemental volume; (d) pear geometry.  $C_{i,g}$  and  $C_{i,l}$  are concentration of gas  $i$  in the gas and liquid phase while  $\epsilon$  is the porosity of tissue.

the different gases led to total pressure gradients that caused convective exchange as described by Darcy's law.

$$\mathbf{u} = -\frac{K}{\mu} \nabla P = -\frac{K \cdot R \cdot T}{\mu} \nabla (\sum C_i) \quad (3)$$

with  $K$  ( $\text{m}^2$ ) the permeation coefficient,  $P$  (Pa) the pressure, and  $\mu$  (Pa.s) the viscosity of the gas. The relationship between the gas concentration and pressure was assumed to follow the ideal gas law ( $P = CRT$ ).

The extended Michaelis–Menten kinetics have been applied as a semi-empirical model to describe the respiration characteristic of intact and tissue fruit (Peppelenbos *et al.*, 1996; Hertog *et al.*, 1998; Lammertyn *et al.*, 2001b; Ho *et al.*, 2008). A non-competitive inhibition model was used to describe  $\text{O}_2$  consumption as formulated by Equation 4:

$$R_{\text{O}_2} = -\frac{V_{\text{m},\text{O}_2} \cdot C_{\text{O}_2}}{(K_{\text{m},\text{O}_2} + C_{\text{O}_2}) \cdot \left(1 + \frac{C_{\text{CO}_2}}{K_{\text{m},\text{CO}_2}}\right)} \quad (4)$$

with  $V_{\text{m},\text{O}_2}$  ( $\text{mol m}^{-3} \text{s}^{-1}$ ) the maximum oxygen consumption rate,  $C_{\text{O}_2}$  ( $\text{mol m}^{-3}$ ) the  $\text{O}_2$  gas concentration,  $C_{\text{CO}_2}$  ( $\text{mol m}^{-3}$ ) the  $\text{CO}_2$  gas concentration,  $K_{\text{m},\text{O}_2}$  ( $\text{mol m}^{-3}$ ) the Michaelis–Menten constant for  $\text{O}_2$  consumption,  $K_{\text{m},\text{CO}_2}$  ( $\text{mol m}^{-3}$ ) the Michaelis–Menten constant for non-competitive  $\text{CO}_2$  inhibition, and  $R_{\text{O}_2}$  ( $\text{mol m}^{-3} \text{s}^{-1}$ ) the  $\text{O}_2$  consumption rate of the sample. The equation for the production rate of  $\text{CO}_2$  consists of an oxidative respiration part and a fermentative part.

$$R_{\text{CO}_2} = -r_{\text{q,ox}} \cdot R_{\text{O}_2} + \frac{V_{\text{m},\text{f},\text{CO}_2}}{\left(1 + \frac{C_{\text{O}_2}}{K_{\text{m},\text{f},\text{O}_2}}\right)} \quad (5)$$

with  $V_{\text{m},\text{f},\text{CO}_2}$  ( $\text{mol m}^{-3} \text{s}^{-1}$ ) the maximum fermentative  $\text{CO}_2$  production rate,  $K_{\text{m},\text{f},\text{O}_2}$  ( $\text{mol m}^{-3}$ ) the Michaelis–Menten constant of  $\text{O}_2$  inhibition on fermentative  $\text{CO}_2$  production,  $r_{\text{q,ox}}$  the respiration quotient at high  $\text{O}_2$  partial pressure, and  $R_{\text{CO}_2}$  ( $\text{mol m}^{-3} \text{s}^{-1}$ ) the  $\text{CO}_2$  production rate of the sample. The effect of temperature on the respiration rate was described by Arrhenius' law (Hertog *et al.*, 1998).

The macroscale geometrical model was based on reconstructed photographic images of intact pear. The pear geometry was considered to be axi-symmetric and the model was solved with gas concentration variations in the radial direction ( $r$ ) and vertical axis ( $z$ ). To study the effect of fruit size on gas exchange, geometrical models were constructed with radii of 2.6, 3, 3.2, 3.7, and 4.2 cm by scaling the original geometrical model. The model was solved using the finite element method (Comsol 3.3, Comsol AB, Stockholm, Sweden).

**Gas transport parameters:** The gas exchange properties of the fruit tissue were measured in the measurement set-up using fluorescent optical probes. The system consisted of two chambers (measurement chamber and flushing chamber) separated by the disc-shaped tissue sample. Due to different applied gas concentrations between the two chambers, gas diffusions took place. The  $\text{O}_2$  and  $\text{CO}_2$  concentrations were measured in the measurement chamber with fluorescent optical probes (Foxy-Resp and FCO2-R; Ocean Optics). The gas diffusion properties were then estimated from the gas concentration profiles as described by Ho *et al.* (2006a). The  $\text{N}_2$  diffusivity was determined indirectly from the total pressure and the  $\text{O}_2$  partial gas pressure of the binary  $\text{O}_2$ – $\text{N}_2$  gas mixture (Ho *et al.*, 2006b).

Permeation properties of pear epidermis and cortex tissue were determined by measuring the total pressure difference between two chambers separated by a tissue sample (Ho *et al.*, 2006b). Both chambers were flushed with humidified  $\text{N}_2$  gas at  $10.0 \text{ l h}^{-1}$ . The pressure was adjusted so as to obtain a 6 kPa pressure difference between the measurement and flushing chamber. The inlet and outlet valves of one chamber were closed, and the decrease in pressure of this chamber was monitored for at least 4 h. The

permeability was then estimated from this pressure drop using the procedure described by Ho *et al.* (2006b). More details can be found in Ho *et al.* (2006a, b).

**Respiration kinetic parameters:** A non-competitive inhibition model was used to describe respiration kinetics of fruit tissue. Respiration kinetic parameters were reported by Ho *et al.* (2008). The respiratory activity of pear depends on its maturity (Veltman *et al.*, 1999). Since the respiration rate was assumed to be determined by one rate-limiting enzymatic reaction (Chevillotte, 1973), the Michaelis–Menten constant  $K_{\text{m},\text{c}}$ , which is a ratio of rate constants, would be expected to be relatively independent of temperature (Hertog *et al.*, 1998). The  $K_{\text{m}}$  value for  $\text{O}_2$  and  $\text{CO}_2$  was therefore assumed to be constant and was taken from Ho *et al.* (2008) (see Table 2). On the other hand, the maximal  $\text{O}_2$  consumption rate  $V_{\text{m},\text{O}_2}$  and maximal  $\text{CO}_2$  fermentative production rate  $V_{\text{m},\text{f},\text{CO}_2}$  are a function of the initially available enzyme concentration (Hertog *et al.*, 1998). These parameters were, therefore, considered to vary from batch to batch, depending on fruit maturity and season. To determine the  $V_{\text{m},\text{O}_2}$  and  $V_{\text{m},\text{f},\text{CO}_2}$  values of tissue, a respiration experiment was carried out in which a pear was put into a closed jar in ambient air at  $-1^\circ\text{C}$ .

Each 1.7 l jar containing two pear fruits resulted in  $\sim 224 \text{ g pear l}^{-1}$ . Two different air conditions were applied at 20 kPa  $\text{O}_2$ , 0 kPa  $\text{CO}_2$ , and 0 kPa  $\text{O}_2$ , 0 kPa  $\text{CO}_2$  by gas mixtures. The gas mixtures were made from pure gases using an in-house built mixing panel equipped with mass flow controllers (Brooks Instrument, The Netherlands). The composition of the mixtures was measured by using a gas analyser (Checkmate II, PBI Dansensor, Denmark) and the resultant accuracy of the concentration in the mixture was better than 0.2 kPa from the reading of the gas analyser. The gas analyser has an accuracy of  $\pm 0.1\%$  absolute for the  $\text{O}_2$  reading and  $\pm 0.5\%$  absolute for the  $\text{CO}_2$  reading, and was calibrated against calibrated mixtures (Air products N.V., USA). For each of conditions, three jars were connected in series and flushed with conditioned air for at least 1 d. Then the jars were closed and the  $\text{O}_2$  and  $\text{CO}_2$  gas partial pressure changes with time were measured by the gas analyser. The gas percentages were converted to partial pressures by multiplying them by the measured total pressure (DPI 142, GE Druck, Germany).  $V_{\text{m},\text{O}_2}$  and  $V_{\text{m},\text{f},\text{CO}_2}$  were estimated by fitting the macroscale model to the experimental data using a non-linear least squares estimation program written in Matlab (The Mathworks, Inc., Natick, USA). To determine the changes of  $V_{\text{m},\text{O}_2}$  and  $V_{\text{m},\text{f},\text{CO}_2}$  due to ripening, the pears were kept for a period of 7 d at  $20^\circ\text{C}$  in normal air preceding the respiration measurement at  $-1^\circ\text{C}$ . Then, the  $V_{\text{m},\text{O}_2}$  and  $V_{\text{m},\text{f},\text{CO}_2}$  of tissue were estimated based on the respiration measurement data.

#### Microscale model

The microscale model was applied to describe respiratory gas diffusion in the intercellular space (pore), the cell wall network, and through the cell membrane into the cytoplasm (Ho *et al.*, 2009). For the intracellular liquid phase, gas diffusion in the liquid was coupled to cellular respiration kinetics.

**$\text{O}_2$  transport model:** Microscale diffusion was assumed to dominate transport through each of the compartments and was described by Fick's second law, with the characteristic diffusion coefficient  $D_{\text{O}_2}$  (Eq (6)). Respiration was incorporated into the model as a source term  $R_{\text{O}_2}$ .

$$\frac{\partial C_{\text{O}_2}}{\partial t} = \nabla \cdot D_{\text{O}_2} \nabla C_{\text{O}_2} + R_{\text{O}_2} \quad (6)$$

where  $C_{\text{O}_2}$  ( $\text{mol m}^{-3}$ ) is the  $\text{O}_2$  concentration in a certain phase and  $D_{\text{O}_2}$  ( $\text{m}^2 \text{s}^{-1}$ ) is the  $\text{O}_2$  diffusivity. The relationship between the  $\text{O}_2$  concentration in the gas phase  $C_{\text{O}_2,\text{g}}$  and that in the liquid phase  $C_{\text{O}_2,\text{l}}$  is given by Henry's law:



$$C_{O_2,l} = R \cdot T \cdot H_{O_2} \cdot C_{O_2,g} \quad (7)$$

with  $R$  ( $8.314 \text{ J mol}^{-1} \text{ K}^{-1}$ ) the universal gas constant,  $T$  (K) the temperature, and  $H_{O_2}$  ( $\text{mol m}^{-3} \text{ kPa}$ ) Henry's constant for  $O_2$ . In the intracellular liquid phase, Michaelis–Menten kinetics were used as a phenomenological model to describe the  $O_2$  consumption rate of cell protoplasts (Lammertyn *et al.*, 2001b):

$$R_{O_2} = \frac{V_{m,O_2} \cdot C_{O_2}}{K_{m,O_2} + C_{O_2}} \quad (8)$$

with  $V_{m,O_2}$  ( $\text{mol m}^{-3} \text{ s}^{-1}$ ) the maximum oxygen consumption rate in the liquid phase and  $K_{m,O_2}$  ( $\text{mol m}^{-3}$ ) the Michaelis–Menten constant for  $O_2$  consumption. The cell membrane is essentially a phospholipid bilayer. Passive gas transfer across the cell membrane occurs according to Fick's first law as a consequence of a concentration difference over the membrane. The flux  $J_{O_2}$  ( $\text{mol m}^{-2} \text{ s}^{-1}$ ) through the membrane was equal to

$$J_{O_2} = -h_{O_2,\text{mem}} \Delta C_{O_2} = -h_{O_2,\text{mem}} (C_{O_2} - C_{O_2}^*) \quad (9)$$

where  $h_{O_2,\text{mem}}$  ( $\text{m s}^{-1}$ ) is the  $O_2$  permeability of the cell membrane and  $C_{O_2}^*$  ( $\text{mol m}^{-3}$ ) is the equilibrium  $O_2$  concentration in the liquid phase of the outer membrane.

*CO<sub>2</sub> transport model:* For pores and cell walls, the following equation was used:

$$\frac{\partial C_{CO_2}}{\partial t} = \nabla \cdot D_{CO_2} \nabla C_{CO_2} \quad (10)$$

where  $C_{CO_2}$  ( $\text{mol m}^{-3}$ ) is the  $CO_2$  concentration in a certain phase and  $D_{CO_2}$  ( $\text{m}^2 \text{ s}^{-1}$ ) is the  $CO_2$  diffusivity. The model of  $CO_2$  transport in the liquid phase was

$$\frac{\partial C_{CO_2}}{\partial t} = \nabla \cdot D_{CO_2} \nabla C_{CO_2} + R_{CO_2} - k_1 C_{CO_2} + k_2 \frac{[H]^+ C_{HCO_3^-}}{K} \quad (11)$$

$$\frac{\partial C_{HCO_3^-}}{\partial t} = \nabla \cdot D_{HCO_3^-} \nabla C_{HCO_3^-} + k_1 C_{CO_2} - k_2 \frac{[H]^+ C_{HCO_3^-}}{K} \quad (12)$$

with  $C_{HCO_3^-}$  ( $\text{mol m}^{-3}$ ),  $D_{HCO_3^-}$  ( $\text{m}^2 \text{ s}^{-1}$ ) the cytoplasmic concentration and diffusivity of  $HCO_3^-$ , respectively,  $R_{CO_2}$  ( $\text{mol m}^{-3} \text{ s}^{-1}$ ) the cytoplasmic  $CO_2$  production rate, and  $k_1$  ( $\text{s}^{-1}$ ) and  $k_2$  ( $\text{s}^{-1}$ ) the  $CO_2$  hydration rate constant and  $H_2CO_3$  dehydration rate constant, respectively.  $[H]^+$  ( $\text{mol L}^{-1}$ ) and  $K$  ( $\text{mol L}^{-1}$ ) are the concentration of protons  $H^+$  and the acid dissociation constant for  $H_2CO_3$ . A more detailed explanation can be found in Ho *et al.* (2009). The latter two terms of Equations 11 and 12 represent the forward and backward conversion rate of  $CO_2$  to  $HCO_3^-$ , respectively. The equation for the production rate of  $CO_2$  in the cytoplasm accounts for both oxidative and fermentative respiration.

$$R_{CO_2} = -r_{q,\text{ox}} \cdot R_{O_2} + \frac{V_{m,f,CO_2}}{\left(1 + \frac{C_{O_2}}{K_{m,f,O_2}}\right)} \quad (13)$$

The first term on the right hand side indicates the oxidative  $CO_2$  production rate due to consumption of  $O_2$ ; the second term represents anoxic conditions in the cell where the oxidative respiration process is inhibited and replaced by a fermentation pathway.

Similar to  $O_2$  transport, the flux  $J_{CO_2}$  ( $\text{mol m}^{-2} \text{ s}^{-1}$ ) through the membrane was written as

$$J_{CO_2} = -h_{CO_2,\text{mem}} \Delta C_{CO_2} = -h_{CO_2,\text{mem}} (C_{CO_2} - C_{CO_2}^*) \quad (14)$$

with  $V_{m,f,CO_2}$  ( $\text{mol m}^{-3} \text{ s}^{-1}$ ) the maximum fermentative  $CO_2$  production rate of the intracellular cellular liquid phase,  $K_{m,f,O_2}$  ( $\text{mol m}^{-3}$ ) the Michaelis–Menten constant of  $O_2$  inhibition on fermentative  $CO_2$  production, and  $r_{q,\text{ox}}$  the respiration quotient at

high  $O_2$  partial pressure (the ratio between  $CO_2$  production and  $O_2$  consumption). The relationship between the equilibrium  $CO_2$  concentration in the gas and liquid phase was again assumed to be described by Henry's law:

$$C_{CO_2,l} = R \cdot T \cdot H_{CO_2} \cdot C_{CO_2,g} \quad (15)$$

with  $H_{CO_2}$  ( $\text{mol m}^{-3} \text{ kPa}^{-1}$ ) Henry's constant for  $CO_2$ .

Parameters of the microscale were reported by Ho *et al.* (2009) (see Supplementary Table S1 available at *JXB* online). The  $V_{m,O_2}$  of tissue was converted to the value for cytoplasm by dividing it by the porosity of the tissue.

Tissue geometries were constructed from light microscopic images of cortex parenchyma tissue of pear and generated using the ellipse tessellation algorithm (Mebatsion *et al.*, 2006). The tissue model was then imported into a finite element simulation code (Comsol 3.3, Comsol AB, Stockholm, Sweden) via a Matlab interface (see more details in Mebatsion *et al.*, 2006) where a finite element mesh was generated on the pear geometry. Equations of gas exchange were discretized over the meshed geometry and solved using the finite element method in Comsol.

### Multiscale model and localization

In this computational analysis for multiscale simulation, the macroscale gas transport model was first applied to predict the respiratory gas distribution in the fruit. Simulations were carried out for pears under well-defined environmental conditions. In total, 35 conditions, ranging from 0.1 kPa to 3.5 kPa  $O_2$  in combination with 0.7 kPa  $CO_2$  at  $-1^\circ \text{C}$  were applied. The critical region was defined as the position where the  $O_2$  and  $CO_2$  concentrations in the pear were minimal and maximal, respectively, as predicted by the macroscale model. This region was considered to be likely to switch to a fermentative metabolism due to anoxia or high  $CO_2$  partial pressure. The microscale model was solved to compute the corresponding intracellular concentration. Hence, the gas concentration of the critical region of the macroscale model was applied at the boundary of the computational domain in the microscale simulation. The model was solved by means of the finite element method in Comsol Multiphysics vs. 3.3 (Comsol AB, Stockholm).

## Results

### Macroscale model, gas exchange properties, and respiration kinetics parameters

The measured gas transport properties are shown in Table 1. A high variability was observed. The gas diffusivity values of the epidermis and subepidermis were small. The higher diffusivity in the axial direction compared with that in the radial direction is probably due to the fact that vascular bundles are not filled with sap during storage of the fruit and thus can be considered as hollow tubes facilitating gas transport (Verboven *et al.*, 2008). It is likely, therefore, that the vascular bundles along the axis of the pear indeed facilitate gas exchange. The diffusivity of  $CO_2$  was larger than that of  $O_2$  and  $N_2$ .

An extended Michaelis–Menten kinetics model was applied to the respiration submodel of the macroscale. The Michaelis–Menten constants were assumed not to depend on temperature and were taken from Ho *et al.* (2008). Only the maximal  $O_2$  consumption rate  $V_{m,O_2}$  and maximal  $CO_2$  fermentative production rate  $V_{m,f,CO_2}$  were assumed to vary depending on fruit maturity and differ from batch to batch.

These parameters were determined by fitting the macroscale model prediction to the measured respiration kinetics of intact fruit. The fit is shown in Fig. 2. The estimated values of  $V_{m,O_2}$  and  $V_{m,f,CO_2}$  of tissue for ripe fruit measured at  $-1^\circ\text{C}$  following storage for 7 days at  $20^\circ\text{C}$  in ambient air were considerably larger than those for the control fruit (see Table 3).

The macroscale model parameters were validated by comparing the measured  $O_2$  and  $CO_2$  concentration as a function of time in the jar with simulated values at  $10^\circ\text{C}$ . A good agreement between simulations and measurements was observed, as depicted in Fig. 3.

A simulation result of the respiratory gas distribution inside the fruit under low oxygen conditions is shown in Fig. 4. Due to the diffusion barrier, a concentration gradient was found inside the pear. A decrease of  $O_2$  partial pressure and an increase of  $CO_2$  partial pressure inside the fruit were observed. Ripening of the fruit increased the respiration, leading to much lower levels of oxygen in the centre of fruit compared with the control fruit (Fig. 4b).

**Table 1.** Estimated gas diffusion properties of the macroscale gas transport model and their 95% confidence interval

The number of replicates varied between six and eight. Skin was defined here as the combination of epidermis and hypodermis.

| Parameter       | Units                      | Estimated value                    |
|-----------------|----------------------------|------------------------------------|
| $D_{O_2,skin}$  | $\text{m}^2 \text{s}^{-1}$ | $(1.86 \pm 0.70) \times 10^{-10a}$ |
| $D_{CO_2,skin}$ | $\text{m}^2 \text{s}^{-1}$ | $(5.06 \pm 3.3) \times 10^{-10a}$  |
| $D_{N_2,skin}$  | $\text{m}^2 \text{s}^{-1}$ | $(1.06 \pm 0.29) \times 10^{-10b}$ |
| $K_{skin}$      | $\text{m}^2$               | $(2.17 \pm 1.43) \times 10^{-19b}$ |
| $D_{O_2,r}$     | $\text{m}^2 \text{s}^{-1}$ | $(5.63 \pm 3.09) \times 10^{-10}$  |
| $D_{CO_2,r}$    | $\text{m}^2 \text{s}^{-1}$ | $(5.32 \pm 1.43) \times 10^{-9}$   |
| $D_{N_2,r}$     | $\text{m}^2 \text{s}^{-1}$ | $(6.3 \pm 3.7) \times 10^{-10}$    |
| $K_r$           | $\text{m}^2$               | $(6.23 \pm 8.25) \times 10^{-19}$  |
| $D_{O_2,z}$     | $\text{m}^2 \text{s}^{-1}$ | $(3.18 \pm 1.3) \times 10^{-9}$    |
| $D_{CO_2,z}$    | $\text{m}^2 \text{s}^{-1}$ | $(1.4 \pm 4.3) \times 10^{-8}$     |
| $D_{N_2,z}$     | $\text{m}^2 \text{s}^{-1}$ | $(1.66 \pm 1.11) \times 10^{-9}$   |
| $K_z$           | $\text{m}^2$               | $(9.8 \pm 13.0) \times 10^{-17}$   |

<sup>a</sup> Values measured by Ho *et al.* (2006a).

<sup>b</sup> Values measured by Ho *et al.* (2006b).

**Table 2.** Respiration kinetic parameters of the macroscale gas transport model

| Parameters   | Units                             | Estimated values <sup>a</sup>        |
|--|-----------------------------------|--------------------------------------|
| Maximal $O_2$ consumption rate of tissue $V_{m,O_2,tissue}$ ( $-1^\circ\text{C}$ )                 | $\text{mol m}^{-3} \text{s}^{-1}$ | $(1.1173 \pm 0.0003) \times 10^{-5}$ |
| Maximal fermentative $CO_2$ production rate of tissue $V_{m,f,CO_2,tissue}$ ( $-1^\circ\text{C}$ ) | $\text{mol m}^{-3} \text{s}^{-1}$ | $(1.1148 \pm 0.0002) \times 10^{-5}$ |
| Activation energy of $O_2$ consumption $E_{a,VmO_2}$   | $\text{kJ mol}^{-1}$              | $80.2 \pm 12.3^b$                    |
| Activation energy of $CO_2$ production $E_{a,VmCO_2}$  | $\text{kJ mol}^{-1}$              | $56.7 \pm 13.3^b$                    |
| Michaelis–Menten constant for $O_2$ consumption $K_{m,O_2}$  | kPa                               | $1.00 \pm 0.23^b$                    |
| Michaelis–Menten constant for non-competitive $CO_2$ inhibition $K_{m,CO_2}$                       | kPa                               | $66.4 \pm 21.3^b$                    |
| Michaelis–Menten constant of $O_2$ inhibition on fermentative $CO_2$ production $K_{m,f,O_2}$      | kPa                               | $0.28 \pm 0.14^b$                    |
| Respiration quotient $r_{q,ox}$  |                                   | $0.83 \pm 0.0004$                    |

<sup>a</sup>  $\pm$  95% confidence limits.

<sup>b</sup> Parameters were taken from Ho *et al.* (2008). The other parameters were estimated by fitting the macroscale model to the measured  $O_2$  and  $CO_2$  gas partial pressures in the jars.

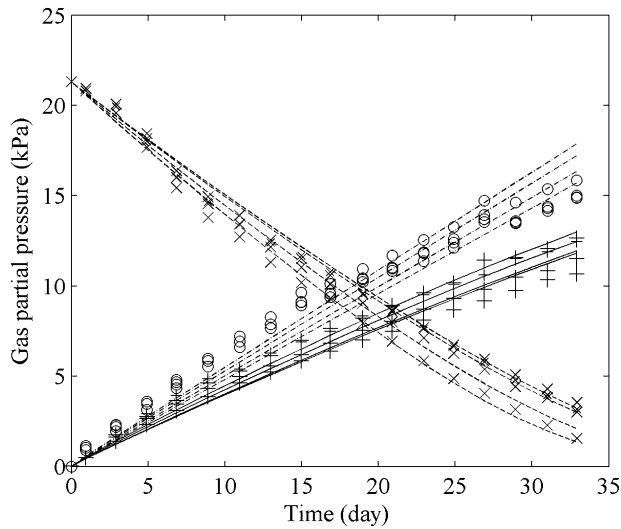
### Microscale gas exchange model

The microscale gas exchange model was applied to the intercellular space (pore), the cell wall network, the cell membrane, and the cytoplasm (Ho *et al.*, 2009). The microscale gas exchange was validated by comparing the macroscopic apparent diffusivity computed from the microscale with the measurement (see Table 4). In addition, good agreement was found between simulated macroscopic gas concentration gradients and the microscale model (Ho *et al.*, 2009). The simulated intracellular  $O_2$  concentration computed in the critical region (lowest  $O_2$  concentration) of the macroscale fruit is shown in Fig. 5. Heterogeneity of intracellular concentrations was found. The results show that the intracellular  $O_2$  concentration of the control fruit was much higher than that of the ripe fruit.

### Multiscale modelling of gas exchange in relation to environmental conditions

In this computational analysis for multiscale gas exchange, the continuum model was first simulated with different external conditions and fruit sizes at a storage temperature of  $-1^\circ\text{C}$ . The critical region is defined as the site where the lowest  $O_2$  and highest  $CO_2$  were computed from the macroscale model. Then, the intracellular level was analysed by simulating gas transport using the microscale model with boundary conditions from the critical values of the macroscale simulation. The results showed that the difference between the lowest concentration of the cells computed from the microscale model and that estimated by the macroscale model of the normal pear at  $-1^\circ\text{C}$  ranged from 1.3% to 6.2% under ultra low  $O_2$  conditions. The corresponding minimal  $O_2$  concentration ( $\mu\text{M}$ ) in the cytoplasm as a function of external  $O_2$  partial pressure and pear radius is shown in Fig. 6. The minimal  $O_2$  concentration increased with increasing external  $O_2$  partial pressure and decreased with increasing radius. With a typical external  $O_2$  partial pressure of 2.5 kPa, the minimal  $O_2$  concentration for the fruit with radius from 2.6 cm to 4.2 cm was  $>1 \mu\text{M}$ .

To study the effect of fruit ripening on the risk of storage disorder development, the measured maximal  $O_2$  consumption rate  $V_{m,O_2}$  and maximal  $CO_2$  production rate  $V_{m,f,CO_2}$



**Fig. 2.** O<sub>2</sub> and CO<sub>2</sub> concentration as a function of time in a closed jar at a storage temperature of  $-1^{\circ}\text{C}$ . Dashed lines and solid lines indicate the O<sub>2</sub> and CO<sub>2</sub> partial pressure in jars fitted by the permeation–diffusion–reaction model. The symbols (x) and (+) indicate the measured O<sub>2</sub> and CO<sub>2</sub> gas partial pressure. The initial condition was set to 20 kPa O<sub>2</sub>, 0 kPa CO<sub>2</sub>. The dash-dotted line and open circles indicate the simulated and measured CO<sub>2</sub> gas partial pressure in the jar with an initial condition of 0 kPa O<sub>2</sub>, 0 kPa CO<sub>2</sub>. Under these conditions the O<sub>2</sub> partial pressure obviously remained equal to 0 kPa.

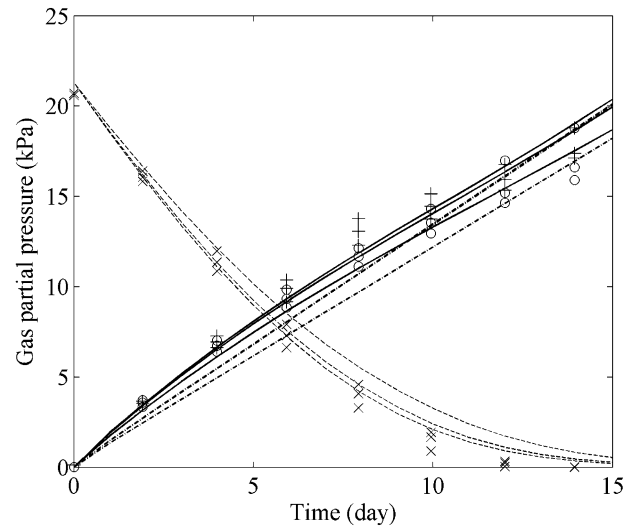
**Table 3.** Maximal O<sub>2</sub> consumption rate  $V_{m,O_2}$ , and maximal CO<sub>2</sub> production rate  $V_{m,f,CO_2}$  of tissue

The values were estimated by fitting the permeation–diffusion–reaction model to the measured data.

| Respiration                     | Maximal O <sub>2</sub> consumption rate of tissue $V_{m,O_2,tissue}$ (mol m <sup>-3</sup> s <sup>-1</sup> ) | Maximal CO <sub>2</sub> production rate of tissue $V_{m,f,CO_2,tissue}$ (mol m <sup>-3</sup> s <sup>-1</sup> ) |
|---------------------------------|---|--|
| At $-1^{\circ}\text{C}$         | $1.12 \times 10^{-5}$   | $1.11 \times 10^{-5}$  |
| Effect of ripening <sup>a</sup> | $2.93 \times 10^{-5}$   | $3.57 \times 10^{-5}$  |

<sup>a</sup> Pear stored at  $20^{\circ}\text{C}$  for 7 d for ripening, then again at  $-1^{\circ}\text{C}$ .

of tissue due to ripening (Table 3) were used for the macroscale simulation. The macroscale model was used to predict the corresponding intracellular concentration at the critical region from the macroscale model. The difference between the lowest concentration of the cells computed from the macroscale model and that estimated by the macroscale model of the ripening pear at  $-1^{\circ}\text{C}$  ranged from 11.4% to 14% under ultra low O<sub>2</sub> conditions. The simulated minimal O<sub>2</sub> concentration ( $\mu\text{M}$ ) in the cytoplasm at  $-1^{\circ}\text{C}$  is shown in Fig. 6. The results demonstrate that the increasing respiration rate due to fruit ripening may lead to anoxia in storage. The multiscale model indicated that the minimal O<sub>2</sub> concentration in ripe fruit was more severe compared with that of control fruit. While control fruit had a minimal O<sub>2</sub> concentration  $>1 \mu\text{M}$ , in ripe and large fruit



**Fig. 3.** Validated O<sub>2</sub> and CO<sub>2</sub> concentration as a function of time in a closed jar at a storage temperature of  $10^{\circ}\text{C}$ . Dashed lines and solid lines indicate the O<sub>2</sub> and CO<sub>2</sub> partial pressure in jars predicted by the permeation–diffusion–reaction model. The symbols (x) and (+) indicate the measured O<sub>2</sub> and CO<sub>2</sub> gas partial pressure. The initial condition was set to 20 kPa O<sub>2</sub>, 0 kPa CO<sub>2</sub>. The dash-dotted line and open circles indicate the simulated and measured CO<sub>2</sub> gas partial pressure in the jar with an initial condition of 0 kPa O<sub>2</sub>, 0 kPa CO<sub>2</sub>. Under these conditions the O<sub>2</sub> partial pressure obviously remained equal to 0 kPa.

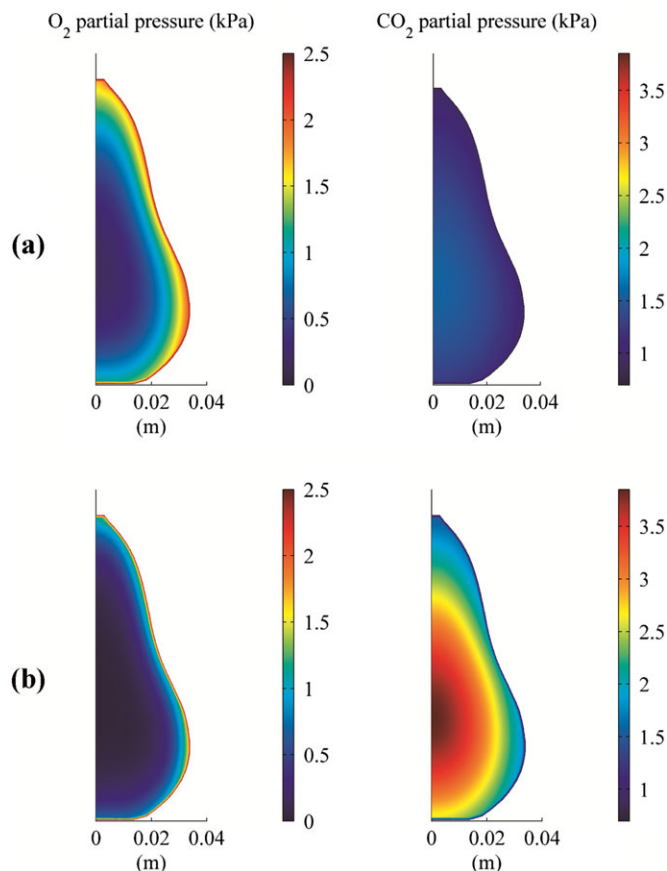
this value decreased to  $<0.1 \mu\text{M}$  with an external O<sub>2</sub> partial pressure of 2.5 kPa.

The maximal CO<sub>2</sub> concentration in the centre of the fruit was computed for different pear radii and ambient O<sub>2</sub> concentrations. The CO<sub>2</sub> concentration in the centre of the fruit is more sensitive to the fruit size (Fig. 7). In small fruit ( $R_{\text{pear}} < 3 \text{ cm}$ ), the CO<sub>2</sub> concentration seemed to be saturated with increasing O<sub>2</sub> concentration. Increasing the fruit size led to a high CO<sub>2</sub> concentration in the centre of the fruit.

## Discussion

Pear fruit are commercially stored at low temperature under CA conditions to retard physiological processes in the fruit by decreasing the O<sub>2</sub> partial pressure and by increasing the CO<sub>2</sub> partial pressure. However, the optimal gas composition is critical, as too low an O<sub>2</sub> partial pressure can induce fermentative metabolism in the fruit (Beaudry, 1999). In other organs, gas availability is also critical. In seeds, oxygen falls to very low levels inside developing embryos (Rolletschek et al., 2002) and maintains a minimum level which has been shown to affect the overall rate of metabolism. Anoxia stress may lead to hydrogen peroxide formation in plant cells and be harmful for cellular metabolic processes (Blokhina et al., 2001). The gas exchange model may be useful to predict the internal gas concentration coupled to metabolic processes, to optimize plant metabolism by changing the oxygen availability.

Cytochrome *c* oxidase has been considered as the rate-limiting enzyme in the oxidative respiration pathway



**Fig. 4.** O<sub>2</sub> and CO<sub>2</sub> distribution of the intact fruit under typical commercial storage conditions (2.5 kPa O<sub>2</sub>, 0.7 kPa CO<sub>2</sub> and -1 °C); (a) control fruit, (b) ripe fruit.

**Table 4.** Macroscopic apparent diffusivity of O<sub>2</sub> and CO<sub>2</sub> in pear parenchyma tissue (Ho *et al.*, 2009)

The values reported for the microscale model are average values for nine different tissue geometries.

|                  | T (°C) | $D_{CO_2,tissue}(m^2 s^{-1})^a$    | $D_{CO_2,tissue}(m^2 s^{-1})$     |
|------------------|--------|------------------------------------|-----------------------------------|
| Microscale model | 20     | $(3.54 \pm 0.68) \times 10^{-10}$  | $(3.13 \pm 0.59) \times 10^{-9}$  |
|                  | 0      | $(3.23 \pm 0.63) \times 10^{-10}$  | $(2.83 \pm 0.45) \times 10^{-9}$  |
| Measurement      | 20     | $(2.87 \pm 0.45) \times 10^{-10a}$ | $(2.6 \pm 0.36) \times 10^{-9 b}$ |
|                  | 12     | $(4.3 \pm 1.7) \times 10^{-10c}$   | $(1.73 \pm 1.15) \times 10^{-9c}$ |
|                  | 20     | $(5.63 \pm 3.09) \times 10^{-10d}$ | $(5.32 \pm 1.43) \times 10^{-9d}$ |

<sup>a</sup> ± 95% confidence limits.

<sup>b</sup> Ho *et al.* (2006a).

<sup>c</sup> Schotsmans *et al.* (2003).

<sup>d</sup> Present experiment (Ho *et al.*, 2009).

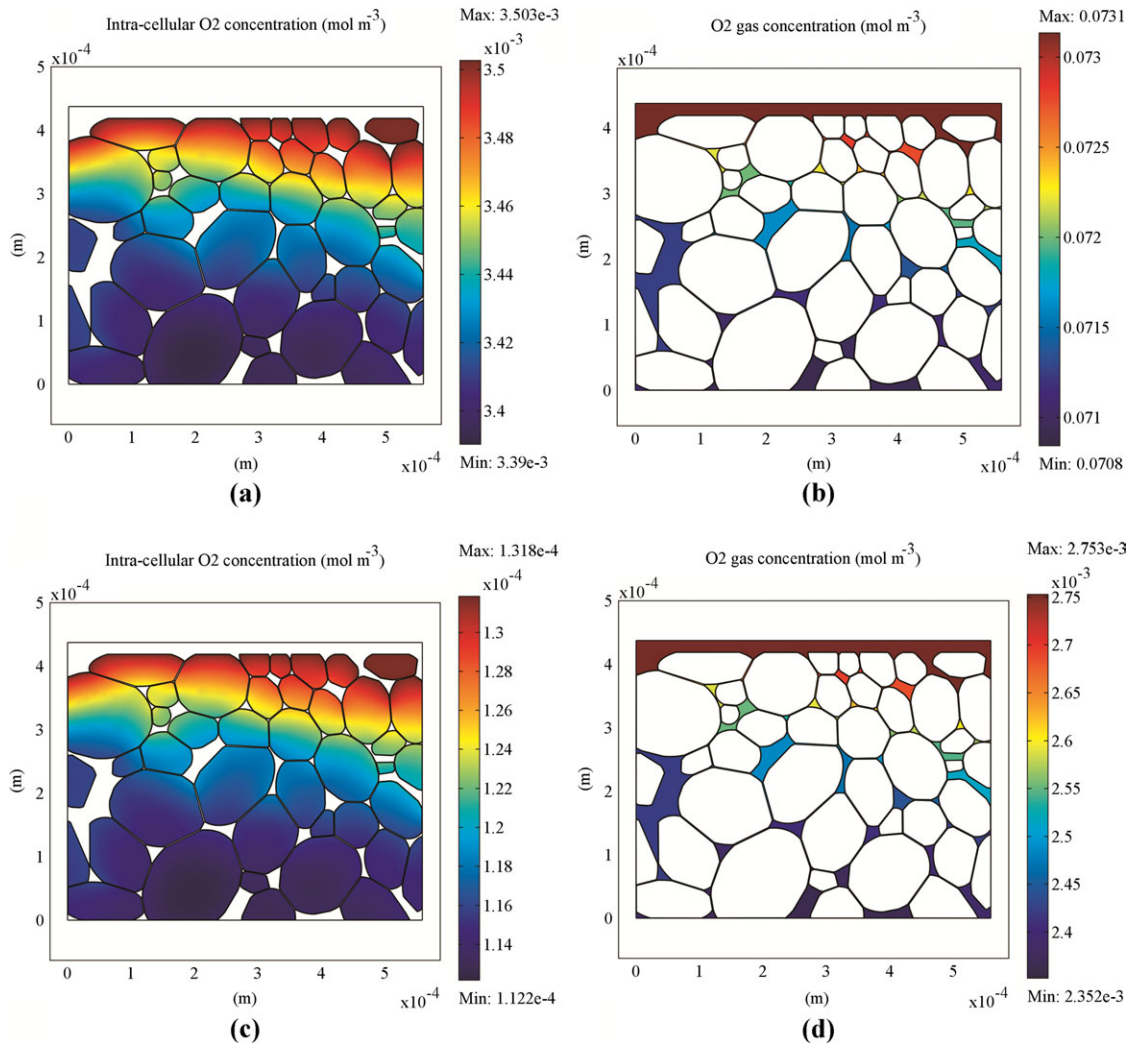
(Chevillotte, 1973). Ludwig *et al.* (2001) considered that oxidative respiration was controlled by cytochrome *c* oxidase activity and ATP synthase. From 80% to 90% of the oxygen consumed by an organism is believed to be reduced to water by cytochrome *c* oxidase, the terminal enzyme of the respiratory chain (Rolfe and Brown, 1997; Gnaiger, 2003). Different values for  $K_{m,O_2}$  of cytochrome *c* oxidase were found in the literature. Solomos (1982) obtained a value of 0.1 μM for the  $K_{m,O_2}$  of isolated cytochrome *c* oxidase for apple. Millar *et al.* (1994) calculated

a  $K_{m,O_2}$  value of 0.14 μM in soybean shoot mitochondria, while Taiz and Zeiger (1993) found a  $K_{m,O_2}$  value of 1 μM for the cytochrome *c* oxidase in plant tissue. The computational analysis presented here revealed that the O<sub>2</sub> concentration of control fruit stored at typical CA conditions (2.5 kPa O<sub>2</sub>, 0.7 kPa CO<sub>2</sub> at -1 °C) was higher than the Michaelis–Menten constant for cytochrome *c* oxidase  $K_{m,c}$ , the rate-limiting enzyme of the respiration pathways. Consequently, the respiratory pathway will be active with O<sub>2</sub> supply. In contrast to small pears, in large pears and under extremely low O<sub>2</sub> storage conditions the oxygen concentration can decrease well below the Michaelis–Menten constant for cytochrome *c* oxidase. This most probably leads to anoxia, and physiological disorders have been observed under such conditions (Lammertyn *et al.*, 2000).

Ripening of the fruit increases the risk of physiological disorders because increasing the respiration rate due to ripening resulted in anoxia in the central region of the fruit even under typical CA conditions (Fig. 6). Depletion of O<sub>2</sub> in the sensitive region was more severe in large fruit compared with small fruit. This corresponds to the observation that late picked fruit was more susceptible to storage disorders described by Lammertyn *et al.* (2000). This is a major step forward in understanding the biophysical processes underlying physiological disorders compared with statistical models such as that developed by Lammertyn *et al.* (2000).

The internal gas partial pressures, which depend on the externally applied gas partial pressures and gas transport properties of the fruit, influence the respiration rate and, hence, the intracellular energy level (Saquet *et al.*, 2003), as well as the antioxidant system (Agar *et al.*, 1997; Veltman *et al.*, 1999; Larrigaudiere *et al.*, 2001; Franck *et al.*, 2003, 2007). It was found here that CO<sub>2</sub> does not have a clear effect on the pear respiration rate (the value of  $K_{m,CO_2}$  is indeed very high). Similar results were also found by Peppelenbos and Van't Leven (1996) for Goldon Delicious apple, Elstar apple, and asparagus. However, an effect of CO<sub>2</sub> was found for broccoli, mungbean sprouts, and cut chicory. There is no clear reason why there should be such a difference; in fact, relatively little is known about the effect of CO<sub>2</sub> on the activity of respiratory enzymes. However, a high CO<sub>2</sub> partial pressure during storage of the fruit was likely to induce brown core development in Conference pears (Veltman *et al.*, 1999; Franck *et al.*, 2003, 2007). Note that the pH of the cytoplasm is controlled by the pH buffering capacity (Smith and Raven, 1979; Boron, 2004) and proton pumps (Nishi and Forgac, 2002); the required ATP energy for the proton transport is provided by the V-ATPases system (Nishi and Forgac, 2002). Increasing the CO<sub>2</sub> level in the pore of fruit tissue may lead to a decreased pH in the cytoplasm. To maintain the pH of the cytoplasm, the intracellular system may need more energy for pumping of protons among the compartments. Shortage of energy could then occur during storage of the fruit to maintain the intracellular pH at high CO<sub>2</sub> concentration levels. Moreover, it is possible that a change in the pH may result in loss of the membrane integrity and formation of reactive oxygen species such as superoxide species during respiration. This may





**Fig. 5.** The simulated intracellular  $O_2$  concentration ( $\mu M$ ) of microscopic tissue. (a) and (c) The intracellular  $O_2$  concentration of control and ripe fruit. (b) and (d)  $O_2$  concentration in the gas phase of control and ripe fruit computed from the critical region (lowest  $O_2$  concentration) of the macroscale simulation.

explain the impairment of the anti-oxidation system (L-ascorbic acid distribution) and brown core development in pear, as was found in the literature (Veltman *et al.*, 1999, 2003; Franck *et al.*, 2003, 2007; Saquet *et al.*, 2003).

The modified Michaelis–Menten kinetics which are now included in the multiscale gas exchange model are incapable of predicting such detailed biochemical information. This kinetic model needs to be updated by a new and more comprehensive model which should describe the pathways of respiration and fermentation.

## Conclusions

A multiscale model was developed to study the effect of ambient air composition on gas exchange of fruit during commercial storage. A computational study revealed that oxidative respiration can be still active at typical CA conditions (2.5 kPa  $O_2$ , 0.7 kPa  $CO_2$  at  $-1^\circ C$ ) since the  $O_2$  concentration inside control fruit stored was higher than the Michaelis–Menten constant for cytochrome *c* oxidase  $K_{m,c}$ , the rate-limiting enzyme of the respiration pathway. In

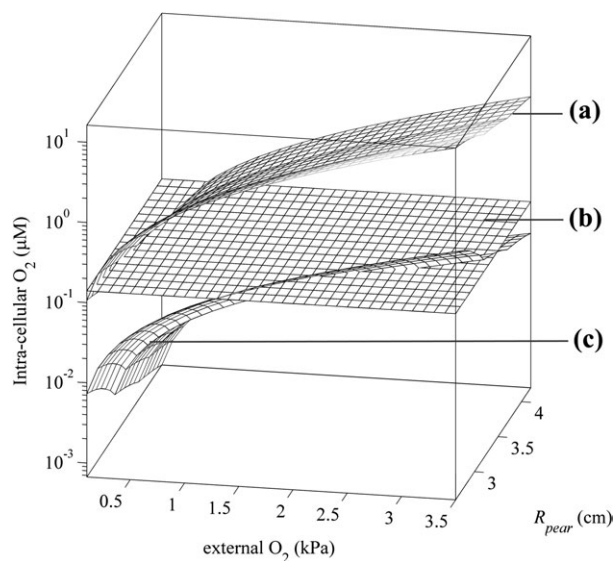
contrast to small pears, in large pears and under very low  $O_2$  storage conditions the oxygen concentration can decrease well below the Michaelis–Menten constant for cytochrome *c* oxidase. This most probably leads to fermentation and physiological disorders which have been observed under such conditions. Ripening of the fruit causes an increased risk of physiological disorders since increasing the respiration rate due to ripening resulted in anoxia in the central region of the fruit even under commercial CA conditions. A multiscale approach can provide a much better insight into the mechanism of gas exchange in pear and in fruit tissue in general, and for the first time a quantitative explanation of the relationship between gas exchange and the development of physiological disorders in fruit has been provided.

## Supplementary data

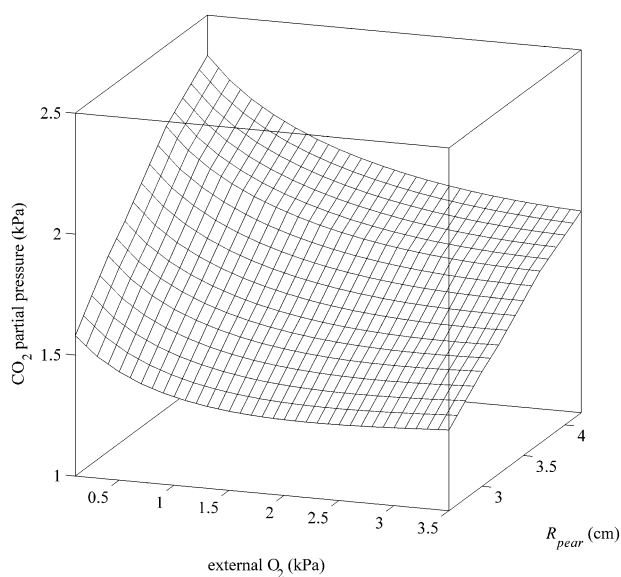
Supplementary data are available at *JXB* online.

**Table S1** Physical parameters of the multiscale gas transport model (Ho *et al.*, 2009).





**Fig. 6.** The intracellular  $O_2$  concentration ( $\mu\text{M}$ ) of the critical region as a function of  $O_2$  partial pressure and pear radius. The storage temperature was  $-1^\circ\text{C}$ . (a) Control fruit; (b)  $O_2$  concentration that is equal to the Michaelis–Menten constant for cytochrome c oxidase  $K_{m,c}$  ( $0.14\ \mu\text{M}$ ) (Millar *et al.*, 1994); (c) ripe fruit.



**Fig. 7.** Maximal  $\text{CO}_2$  concentration (kPa) computed from the macroscale model of control fruit as a function of  $O_2$  partial pressure and pear radius. The storage temperature was  $-1^\circ\text{C}$ .

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## Appendix

### (Nomenclatur)

#### Parameter

|  |   |
|--|---|
| $C_{\text{CO}_2}$                          | $\text{CO}_2$ concentration ( $\text{mol m}^{-3}$ )   |
| $C_{\text{CO}_2}^*$                        | Equilibrium $\text{CO}_2$ concentration in liquid phase of outer membrane ( $\text{mol m}^{-3}$ )                     |
| $C_{\text{HCO}_3^-}$                       | $\text{HCO}_3^-$ concentration ( $\text{mol m}^{-3}$ )  |
| $C_i$                                      | Concentration of gas $i$ ( $\text{mol m}^{-3}$ )  |
| $C_{\text{O}_2}$                           | $\text{O}_2$ concentration ( $\text{mol m}^{-3}$ )  |
| $C_{\text{O}_2}^*$                         | Equilibrium $\text{O}_2$ concentration in liquid phase of outer membrane ( $\text{mol m}^{-3}$ )                      |
| $D_{\text{CO}_2}$                          | $\text{CO}_2$ diffusivity ( $\text{m}^2 \text{s}^{-1}$ )  |
| $D_{\text{CO}_2, \text{tissue}}$           | $\text{CO}_2$ apparent diffusivity of tissue ( $\text{m}^2 \text{s}^{-1}$ )   |
| $D_{\text{HCO}_3^-}$                       | $\text{HCO}_3^-$ diffusivity ( $\text{m}^2 \text{s}^{-1}$ )   |
| $D_i$                                      | Macroscopic apparent diffusivity of gas $i$ ( $\text{m}^2 \text{s}^{-1}$ )  |
| $D_{\text{O}_2}$                           | $\text{O}_2$ diffusivity ( $\text{m}^2 \text{s}^{-1}$ )   |
| $D_{\text{O}_2, \text{mem}}$               | $\text{O}_2$ diffusivity through cell membrane ( $\text{m}^2 \text{s}^{-1}$ )   |
| $E_{a, V_{m, \text{O}_2}}$                 | Activation energy of $\text{O}_2$ consumption ( $\text{kJ mol}^{-1}$ )  |
| $E_{a, V_{m, \text{f}, \text{CO}_2}}$      | Activation energy of $\text{CO}_2$ production ( $\text{kJ mol}^{-1}$ )  |
| $h_{\text{O}_2, \text{mem}}$               | $\text{O}_2$ permeability through cell membrane ( $\text{m s}^{-1}$ )   |
| $h_{\text{CO}_2, \text{mem}}$              | $\text{CO}_2$ permeability through cell membrane ( $\text{m s}^{-1}$ )  |
| $h_{\text{HCO}_3^-, \text{mem}}$           | $\text{HCO}_3^-$ permeability through cell membrane ( $\text{m s}^{-1}$ )   |
| $H_{\text{O}_2}$                           | Henry's constant for $\text{O}_2$ ( $\text{mol m}^{-3} \text{kPa}^{-1}$ )   |
| $H_{\text{CO}_2}$                          | Henry's constant for $\text{CO}_2$ ( $\text{mol m}^{-3} \text{kPa}^{-1}$ )  |
| $[H^+]$                                    | $H^+$ concentration ( $\text{mol l}^{-1}$ )   |
| $J_{\text{CO}_2}$                          | The flux of $\text{CO}_2$ ( $\text{mol m}^{-2} \text{s}^{-1}$ )   |
| $J_{\text{O}_2}$                           | The flux of $\text{O}_2$ ( $\text{mol m}^{-2} \text{s}^{-1}$ )  |
| $k_1$                                      | $\text{CO}_2$ hydration velocity constant ( $\text{s}^{-1}$ )   |
| $k_2$                                      | $\text{CO}_2$ dehydration velocity constant ( $\text{s}^{-1}$ )   |
| $K$  | Permeation coefficient ( $\text{m}^2$ )   |
| $K_a$                                      | Acid dissociation constant for $\text{H}_2\text{CO}_3$ ( $\text{mol l}^{-1}$ )  |
| $K_{m, c}$                                 | Michaelis–Menten constant for cytochrome c ( $\mu\text{M}$ )  |
| $K_{m, \text{f}, \text{O}_2}$              | Michaelis–Menten constant of $\text{O}_2$ inhibition on fermentative $\text{CO}_2$ production ( $\text{mol m}^{-3}$ ) |
| $K_{m, \text{nn}, \text{CO}_2}$            | Michaelis–Menten constant for non-competitive $\text{CO}_2$ inhibition ( $\text{mol m}^{-3}$ )                        |
| $K_{m, \text{O}_2}$                        | Michaelis–Menten constant for $\text{O}_2$ consumption ( $\text{mol m}^{-3}$ )  |
| $P$  | Total pressure (kPa)  |
| $r_{q, \text{ox}}$                         | Respiration quotient  |
| $R$  | Universal gas constant ( $8.314\ \text{J mol}^{-1} \text{K}^{-1}$ )   |
| $R_i$                                      | Effective respiration term of the tissue ( $\text{mol m}^{-3} \text{s}^{-1}$ )  |
| $R_{\text{O}_2}$                           | $\text{O}_2$ consumption rate ( $\text{mol m}^{-3} \text{s}^{-1}$ )   |
| $R_{\text{CO}_2}$                          | $\text{CO}_2$ consumption rate ( $\text{mol m}^{-3} \text{s}^{-1}$ )  |
| $T$  | Temperature (K)   |
| $t$  | Time (s)  |
| $\mathbf{u}$                               | Velocity vector ( $\text{m s}^{-1}$ )   |
| $V_{m, \text{f}, \text{CO}_2}$             | Maximal fermentative $\text{CO}_2$ production rate ( $\text{mol m}^{-3} \text{s}^{-1}$ )                              |
| $V_{m, \text{f}, \text{CO}_2, \text{ref}}$ | Maximal fermentative $\text{CO}_2$ production rate at reference temperature ( $\text{mol m}^{-3} \text{s}^{-1}$ )     |
| $V_{m, \text{O}_2}$                        | Maximal $\text{O}_2$ consumption rate ( $\text{mol m}^{-3} \text{s}^{-1}$ )   |
| $V_{m, \text{O}_2, \text{ref}}$            | Maximal $\text{O}_2$ consumption rate at reference temperature ( $\text{mol m}^{-3} \text{s}^{-1}$ )                  |
| <b>Symbols</b>                             |   |
| $\alpha_i$                                 | Gas capacity of the component $i$   |
| $\mu$                                      | Viscosity (Pa.s)  |
| $\epsilon$                                 | Porosity of tissue  |
| $\nabla$                                   | Gradient operator ( $\text{m}^{-1}$ )   |
| $\Delta$                                   | Difference  |
| <b>Subscripts</b>                          |   |
| g  | Gas phase   |
| i  | $\text{O}_2$ , $\text{CO}_2$ or $\text{N}_2$  |
| l  | liquid phase  |
| r  | Radial direction  |
| w  | Cell wall   |
| z  | Vertical axis   |
| $\infty$                                   | Ambient atmosphere  |

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