The TeV emission of Ap Librae: a hadronic interpretation and prospects for CTA

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ABSTRACT
Ap Librae is one out of a handful of low-frequency peaked blazars to be detected at TeV γ-rays and the only one with an identified X-ray jet. Combined observations of Fermi-LAT at high energies (HE) and of H.E.S.S. at very high energies (VHE) revealed a striking spectral property of Ap Librae; the presence of a broad high-energy component that extends more than nine orders of magnitude in energy and is, therefore, hard to be explained by the usual single-zone synchrotron self-Compton model. We show that the superposition of different emission components related to photohadronic interactions can explain the γ-ray emission of Ap Librae without invoking external radiation fields. We present two indicative model fits to the spectral energy distribution of Ap Librae where the VHE emission is assumed to originate from a compact, sub-pc scale region of the jet. A robust prediction of our model is VHE flux variability on time-scales similar to those observed at X-rays and HE γ-rays, which can be further used to distinguish between a sub-pc or kpc scale origin of the TeV emission. We thus calculate the expected variability signatures at X-rays, HE and VHE γ-rays and show that quasi-simultaneous flares are expected, with larger amplitude flares appearing at γ-rays. We assess the detectability of VHE variability from Ap Librae with CTA, next generation of IACT. We show that ~h time-scale variability at $E_\gamma > 0.1\ TeV$ could be detectable at high significance with shorter exposure times than current Cherenkov telescopes.

Key words: astroparticle physics – radiation mechanisms: non-thermal – galaxies: active – gamma-rays: galaxies.

1 INTRODUCTION
Blazars with extremely weak optical emission lines or, in many cases, featureless optical spectra, are classified as BL Lac objects. The majority of BL Lac objects that are detected at very high energies (VHE, $E_\gamma > 100\ GeV$) by ground-based Cherenkov telescopes belongs to the high-frequency peaked (HBL) subclass (e.g. Wakely & Horan 2008; Hinton & Hofmann 2009) that is characterized by a low-energy spectral component peaking at frequencies $\nu_p > 10^{15}\ Hz$ (Padovani & Giommi 1995). The quiescent emission as well as individual flares from TeV-detected blazars have been successfully explained by the synchrotron self-Compton (SSC) model (e.g. Maraschi, Ghisellini & Celotti 1992; Bloom & Marscher 1996; Mastichiadis & Kirk 1997; Konopelko et al. 2003; Celotti & Ghisellini 2008; Weidinger & Spanier 2010; Böttcher et al. 2013; HESS Collaboration et al. 2013). In this scenario, electron synchrotron radiation is invoked to explain the low-energy hump of the spectral energy distribution (SED), while it serves as the seed photon field for inverse Compton (IC) scattering, which, in turn, results in the observed high-energy emission. Despite its success the SSC model faces difficulties in explaining the observed emission from certain low-frequency peaked (LBL; $\nu_p < 10^{14}\ Hz$) and intermediate-frequency peaked (IBL; $10^{14} < \nu_p < 10^{15}\ Hz$) sources. Examples of VHE emitting LBL that challenge the SSC interpretation are BL Lacartae (Ravasio et al. 2002) and W Comae (Acciari et al. 2009) (see also Böttcher et al. 2013). One of the most representative sources though is the LBL Ap Librae (alternative name QSO B1514-24).

Ap Librae, lying at a redshift $z = 0.049 \pm 0.002$ (Disney, Peterson & Rodgers 1974; Jones et al. 2009), belongs to a handful of LBL that have been detected at VHE, such as BL Lacartae (Albert et al. 2007) and S5 0716+714 (Anderhub et al. 2009), while it is the only TeV BL Lac object with a detected X-ray jet (Kaufmann 2011; Kaufmann, Wagner & Tibolla 2013). The first detection of Ap Librae at $E_\gamma > 100\ GeV$ by H.E.S.S. was reported in 2010 (Hofmann 2010) while the resulting observations have been recently presented in

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H.E.S.S. Collaboration et al. (2015). These, in combination with the X-ray and high-energy (HE) Fermi-LAT observations (100 MeV to 300 GeV), revealed an unexpected broad high-energy hump, spanning more than nine orders of magnitude in energy (from X-rays to TeV γ-rays). As first noted by Fortin et al. (2010), Tavecchio et al. (2010) and later by Sanchez, Giebels & Fortin (2012), the SED of Ap Librae cannot be explained by the usual SSC model due to the extreme broadness of the high-energy component.

As the SSC model falls short in explaining the broad-band spectrum of Ap Librae, alternative scenarios have been proposed (Hervet, Boisson & Sol 2015; Sanchez et al. 2015; Zacharias & Wagner 2016). In general terms, these models invoke IC scattering of external photons fields (EC) in order to fill in the gap between the hard X-rays and VHE γ-rays, caused by the SSC cutoff at energies below the Fermi-LAT band. In particular, Hervet et al. (2015) showed that photons from the Broad Line Region (BLR) may be upscattered by electrons in the jet at sub-pc scales (blob) making a significant contribution to the Fermi-LAT band, while the external IC emission from the interaction of the blob electrons with the pc-jet radiation contributes the most at the H.E.S.S. energy band. The SED of Ap Librae was successfully described from GHz frequencies up to VHE γ-rays at the cost, however, of increased complexity and number of free parameters.

A second scenario invokes the kpc-scale jet of Ap Librae that has been observed both in radio and X-rays (Kaufmann et al. 2013). In this case, the VHE emission is explained by IC scattering of the cosmic microwave background (CMB) radiation by relativistic electrons of the kpc jet (Sanchez et al. 2015; Zacharias & Wagner 2016). A robust prediction of this model is therefore the lack of variability at VHE in Ap Librae. In this scenario the jet is assumed to remain highly relativistic, i.e. with bulk Lorentz factors \( \Gamma \gg 1 \), even at kpc scales. It is noteworthy that Fermi-LAT observations have recently ruled out the IC/CMB interpretation of the X-ray emission from the kpc jets of other powerful AGN (Meyer & Georganopoulos 2014; Meyer et al. 2015).

Recently, Petropoulou & Mastichiadis (2015, hereafter PM15) showed that broad HE spectra with significant curvature can be obtained outside the usual SSC and EC framework, if protons are accelerated at moderate energies \( \sim 10^{16} - 10^{17} \) eV, i.e. just above the ‘knee’ of the cosmic ray spectrum (for possible particle acceleration mechanisms in blazars, see e.g. Biermann & Strittmatter 1987; Giansivili 2010; Sironi, Spitkovsky & Arons 2013; Sironi, Petropoulou & Giansivili 2015). The broadness of the spectra produced in this scenario can be understood as follows. In BL Lacs, the most important target photon field for photohadronic (\( p\gamma \)) interactions with the relativistic protons is the synchrotron radiation of the co-accelerated (primary) electrons, which emerges as the low-energy hump of their SED. The \( p\gamma \) interactions are comprised of two processes of astrophysical interest, namely the Bethe–Heitler pair production (\( pe \)) and the photopion production (\( p\gamma \)). Moreover, high-energy photons produced by the decay of neutral pions can be absorbed in the source, thus giving rise to an electromagnetic cascade which peaks at lower energies (Mannheim, Biermann & Kruell 1991; Mannheim 1993). Both processes increase the relativistic pair content of the emission region by injecting electron–positron pairs (\( e^- e^+ \)), which, in turn, undergo synchrotron and IC cooling as primary electrons. Their radiative signatures will be, in principle, imprinted on the blazar’s SED (see also Petropoulou et al. 2015).

PM15 showed, in particular, that the synchrotron emission from \( pe \) pairs may have important implications for blazar emission. The broad injection energy distribution of \( pe \) pairs (e.g. Kelner & Aharonian 2008) is also reflected at their synchrotron spectrum, which also appears extended and curved. The \( pe \) synchrotron spectrum might appear as a broad component in the range of hard X-rays (\( \gtrsim 40 \) keV) to soft γ-rays (\( \lesssim 400 \) MeV) for certain parameter values (see e.g. figs 4 and 5 in PM15). Given that the secondary pairs from \( p\gamma \) interactions are injected with a different rate and at different energies than the Bethe–Heitler secondaries (Kelner & Aharonian 2008; Dimitrakoudis et al. 2012), a broad range of HE spectra is expected (e.g. Cerruti et al. 2015; Petropoulou et al. 2015).

In this paper, we show that the superposition of different emission components related to \( p\gamma \) interactions can explain the HE and VHE γ-ray emission of Ap Librae without invoking external radiation fields. Most important is, though, that VHE variability is a robust prediction of our model that can be used to distinguish between a sub-pc or kpc-scale origin of the VHE emission in Ap Librae. Being an important diagnostic tool, we calculate first the expected variability signatures at different energy bands (X-rays, HE and VHE γ-rays) and then focus on VHE γ-rays. In this paper we assess the detection of VHE variability from Ap Librae with the future TeV Cherenkov Telescope Array (CTA; Actis et al. 2011) which is designed to surpass the sensitivity of current imaging air Cherenkov telescopes (IACT) and water Cherenkov telescopes (see fig. 10 in Lemoine-Goumard 2015).

This paper is structured as follows. In Section 2 we present the multi-wavelength data used for the SED compilation and in Section 3 we outline the adopted model. The results of our model application to Ap Librae are presented in Section 4. In the same section we present the model predictions on the multi-wavelength variability, while focusing on the VHE γ-rays. The prospects for CTA are presented in Section 5. We continue in Section 6 with a discussion of our results and conclude in Section 7 with a summary. For the required transformations between the reference systems of the blazar and the observer, we have adopted a cosmology with \( \Omega_m = 0.3 \), \( \Omega_{\Lambda} = 0.7 \) and \( H_0 = 70 \) km s\(^{-1}\) Mpc\(^{-1}\). The redshift of Ap Librae \( z = 0.049 \) corresponds to a luminosity distance \( D_L = 217.7 \) Mpc. The extragalactic background light (EBL) model of Franceschini, Rodighiero & Vaccari (2008) was used for the attenuation of the model-derived γ-ray spectra.

2 DATA
The high-energy spectrum of Ap Librae composed by Fermi-LAT and H.E.S.S. observations has recently been presented by H.E.S.S. Collaboration et al. (2015). The authors analysed 5 yr of Fermi-LAT data (MJD 54682-56508) and divided their analysis into a quiescent period (MJD 54682-56305 and MJD 56377-56508) and a flaring period (MJD 56306-56376). The VHE observations by H.E.S.S. were performed during the period MJD 55326-55689, i.e. within the quiescent period of Fermi-LAT observations. No H.E.S.S. data have been presented for the period of the Fermi-LAT flare and no results regarding the variability at VHE have been published by the time of writing. We complement our analysis and SED modelling with multi-wavelength observations that were also temporally coincident with the Fermi-LAT quiescent period. Data from the flaring period of Ap Librae in GeV energies are therefore excluded from this analysis.

We searched the HEASARC archive\(^2\) for available X-ray observations of Ap Librae, during the quiescent period of Fermi-LAT observations (MJD 54682-56305). The source was observed seven times.

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\(^{2}\) http://heasarc.gsfc.nasa.gov/docs/archive.html
times by Swift (obs-ids: 0003641005-11, MJD 55247-55783) and four times by RXTE (MJD 55387.9-55391.8) during the quiescent period defined above. Swift/XRT products were downloaded from the HEASARC archive and analysed following the standard procedures described in the Swift data analysis guide.\(^3\) Swift/XRT products were generated with the xrtpipeline and the events were extracted using the command line interface xselect. The auxiliary response files were produced with xrtmkarf. For the Swift/XRT analysis the latest response matrix was used, as provided by the Swift calibration data base caldb. RXTE publication-grade data products were downloaded by the HEAVENS webpage.\(^3\) The X-ray spectra were analysed with xspec (version 12.8.2, Arnaud 1996). The spectra were fitted simultaneously with an absorbed power-law model with the addition of a scaling factor to account for variability and instrumental differences. The X-ray absorption was modelled using the tbnew code, a new and improved version of the X-ray absorption model tbabs (Wilms et al. 2000), while the atomic cross-sections were adopted from Verner et al. (1996). The column density was fixed based on the value provided by the Leiden/Argentine/Bonn (LAB) Survey of Galactic HI (NH,GAL = 0.81 × 10\(^6\) cm\(^{-2}\)). Kalberla et al. 2005).\(^4\) Swift/XRT spectral fitting showed evidence of small flux variability (<20 per cent) but no signs of spectral variability, with the average photon index of the absorbed power-law fit being \(\Gamma = 1.61 \pm 0.09\). All the above are consistent with the findings of Kaufmann et al. (2013). For the SED presentation, we plot the Swift/XRT spectra with the minimum (4.6 \(×\) 10\(^{-12}\) erg cm\(^{-2}\) s\(^{-1}\)) and maximum (5.4 \(×\) 10\(^{-12}\) erg cm\(^{-2}\) s\(^{-1}\)) derived fluxes from all the available Swift/XRT observations.

Ap Librae was observed by the Swift ultraviolet and optical telescope (UVOT) with all its available filters. We analysed the Swift/UVOT images and derived the corresponding magnitudes of Ap Librae. Additional optical observations of the system were performed by the FERMI/SMARTS project (Bonning et al. 2012). We used the averaged \(B, R, J\) and \(K\) magnitudes provided by the SMARTS data base\(^5\) for the quiescent period of Ap Librae. All the observed fluxes were corrected for extinction following Cardelli, Clayton & Mathis (1989) where the reddening was set to \(E(B-V) = 0.1177\) (Schlafly & Finkbeiner 2011). For consistency, we cross-checked our results for the Swift/XRT, UVOT and SMARTS fluxes with the published values reported by Sanchez et al. (2015) and found that they are compatible.

Ap Librae has been monitored at 15 GHz by the Very Long Baseline Array (VLBA) as part of the MOJAVE programme.\(^6\) The radio emission originates from the pc-scale jet and shows no signs of variability within the period MJD 53853-55718 covered by the MOJAVE observations (Sanchez et al. 2015). In our analysis we adopt the time-averaged flux at 15 GHz as obtained by Sanchez et al. (2015). At higher radio frequencies (30–353 GHz) we used the Planck measurements from the Early Release Compact Source Catalog (ERCSC; Planck Collaboration VII 2011) and we included the data at 3.4, 4.6, 12 and 22 \(\mu\)m from the Wide-field Infrared Survey Explorer (WISE; Wright et al. 2010).

The compilation of the multi-wavelength SED of Ap Librae was completed with the inclusion of archival data from the NED data base (Dixon 1970; Kuehr et al. 1981; Wright & Otrupcek 1990; Wright et al. 1994; Condon et al. 1998; Voges et al. 1999; Healey et al. 2007; Casulano et al. 2010a,b; Murphy et al. 2010; Bianchi et al. 2011; Giommi et al. 2012; D’Elia et al. 2013; Planck Collaboration XXVIII 2014; Evans et al. 2014; Boller et al. 2016).

3 http://www.swift.ac.uk/analysis/xrt/
4 http://www.isdc.unige.ch/heavens/
5 http://www.astro.yale.edu/smarts/glast/home.php
6 http://www.physics.purdue.edu/MOJAVE/

3 Henceforth, quantities measured in the rest frame of the blob are denoted with a prime.
4 Henceforth, we refer to electrons and positrons commonly as electrons.
time of the source, i.e. $t_{\text{sec}}' = r_{\text{sec}}'/c$. This energy-independent term mimics the adiabatic expansion of the source, since the steady-state particle distributions derived by solving a kinetic equation containing a physical escape term or an adiabatic loss term are similar.

The interplay of the processes governing the evolution of the energy distributions of the five stable particle populations is formulated with a set of five time-dependent, energy-conserving kinetic equations. To simultaneously solve the coupled kinetic equations for all particle types we use the time-dependent code described in Dimitrakoudis et al. (2012).

### 3.2 Radio emitting region

As we show in Section 4 the emission from the compact emitting region of Ap Librae cannot explain the Planck and MOJAVE radio observations, as the synchrotron spectrum is self-absorbed at $v \lesssim 10^{12}$ Hz; this is a common feature of single-zone models for blazar emission (see e.g. figs 7–10 in Celotti & Ghisellini (2008) for leptonic models and Böttcher et al. (2013); Petropoulou et al. (2015) for hadronic models). Radio emission at GHz frequencies can be more naturally explained as synchrotron radiation produced from a larger and less compact region, such as the base of the pc-scale jet, i.e. the radio core (Lister et al. 2013). The pc-scale jet can be modelled using a series of a (large ~50) number of slices, where the magnetic field strength and particle distributions are assumed to evolve self-similarly along the jet (see e.g. Hervet et al. 2015). As our focus is the broad HE spectrum of Ap Librae, we do not adopt a sophisticated jet model for the radio emission (e.g. Potter & Cotter 2012, 2013). Instead, we assume that the radio emission is produced by a spherical region of pc-scale size, further away from the central engine. Our choice and a possible physical interpretation are discussed in Section 6. We have also verified that the external Compton scattering of the synchrotron radiation field from the extended radio blob by the electrons in the sub-pc blob can be neglected for the adopted parameters (see Tables 1 and 2 and appendix in Petropoulou 2014). On the other way around, the radiation produced by the sub-pc blob is negligible for EC by the electrons in the pc-scale region, as long as their separation distance is $\gtrsim 0.3$ pc.

### 3.3 Host galaxy radiation

The host galaxy of Ap Librae has been clearly detected in the (near-infrared) $H$-band (Kotilainen, Falomo & Scarpa 1998) and in the (blue) $B$-band (Hyvönen et al. 2007). The multi-colour imaging results suggest that the host galaxy of Ap Librae, as for most low-redshift BL Lac objects, is a luminous and massive elliptical galaxy; its mass has been estimated to be $10^{11.4\pm0.03}$ M$_\odot$ (Woo et al. 2005). Hyvönen et al. (2007) showed that the luminosity ratio between the nuclear region and the host galaxy is 1.7 and 0.58 in the $U$ and $B$ bands. Since the contribution of the host galaxy cannot be neglected we will model it based on an appropriate galaxy template. In particular, we use the template of an elliptical galaxy produced by a single episode of star formation with age 13 Gyr, total mass $6 \times 10^{11}$ M$_\odot$, and solar metallicity (Silva et al. 1998). The normalization of the spectrum has been adjusted to fit the data. In particular, the fluxes of the template were multiplied by a factor of 2.5/6 to account for the mass difference between the real and simulated host galaxy.

### 3.4 Accretion disc and BLR radiation

The accretion disc can illuminate the gas in close proximity of the black hole, thus giving rise to the emission from the BLR. These two external radiation fields can serve as target photons for inverse Compton scattering by the electrons of the sub-pc scale region. Different analyses of the faint Hα emission lines result in different estimates of the BLR luminosity, ranging between $L_{\text{BLR}} = 2.2 \times 10^{41}$ erg s$^{-1}$ (Stickel, Fried & Kuehr 1993) and $9.5 \times 10^{41}$ erg s$^{-1}$ (Morris & Ward 1988). Nevertheless, both estimates suggest a low-luminosity BLR. Assuming a BLR covering factor of 0.01.

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>$B'$ (G)</td>
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</tr>
<tr>
<td>$r'$ (cm)</td>
<td>$1.9 \times 10^{18}$</td>
</tr>
<tr>
<td>$\delta_p$</td>
<td>12.2</td>
</tr>
<tr>
<td>$\theta (\circ)$</td>
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</tr>
<tr>
<td>$\Gamma$</td>
<td>7.7</td>
</tr>
<tr>
<td>$\epsilon_e$</td>
<td>$6.3 \times 10^{-7}$</td>
</tr>
<tr>
<td>$\epsilon_\gamma$</td>
<td>$2 \times 10^{2}$</td>
</tr>
<tr>
<td>$\epsilon_\nu$,min</td>
<td>$8 \times 10^{3}$</td>
</tr>
<tr>
<td>$\epsilon_\nu$,br</td>
<td>$3 \times 10^{4}$</td>
</tr>
<tr>
<td>$\epsilon_\nu$,max</td>
<td>$0.03$</td>
</tr>
<tr>
<td>$p_e$,1</td>
<td>1.8</td>
</tr>
<tr>
<td>$p_e$,2</td>
<td>4.0</td>
</tr>
<tr>
<td>$b_\gamma$</td>
<td>$\gg 1$</td>
</tr>
</tbody>
</table>

$^a$Same as in Table 1.
4 RESULTS

4.1 The core emission of Ap Librae

Aim of this paper is to demonstrate the possibility of producing broad HE non-thermal spectra from a single compact emitting region instead of deriving a unique parameter set as determined by the best χ² fit to the data. We, therefore, present two indicative model fits to the SED of Ap Librae that differ only in the properties of the compact component. We will refer to these as models A and B (see Table 1). The parameter values that describe the radio-emitting region are summarized in Table 2. The parameters describing the particle distributions in Table 1 refer to those at injection. The electron Lorentz factor γ_e,br does not correspond to the cooling break of the particle distribution, as it is also suggested by the large difference between the power-law indices of the distribution before and after the break (if this was due to cooling, one would expect p_e,2 − p_e,1 = 1). In our modelling, the shape of the particle distribution at injection is not the result of a self-consistent treatment of the acceleration process. Thus, it is treated as a free parameter which is determined by the fit to the observations. However, the steepness of the particle distribution above the break could be interpreted in terms of efficient escape of the highest energy particles from the acceleration region.

Our results for models A and B are presented, respectively, in the left-hand and right-hand panels of Fig. 1. The total multi-wavelength spectrum (thick gold line) is composed of the emission from the pc-scale radio emitting region (grey solid line), the host galaxy (magenta solid line), and the emission from the sub-pc region. The latter is decomposed into the following emission components: the SSC radiation of primary electrons (orange dashed line), the proton synchrotron radiation (dark cyan dotted line) and the synchrotron radiation from secondary electrons produced by the \( p\gamma \) and \( γγ \) processes (red dash–dotted line). The spectrum without taking the EBL absorption into account is overplotted with a black dashed line. The results for models A and B are displayed in the left-hand and right-hand panels, respectively. For interpretation of the references to colour in this figure legend, the reader is referred to the web version of this article.

The X-ray emission in model A is mainly produced by the SSC radiation of primary electrons (orange dashed line), the proton synchrotron radiation (dark cyan dotted line) and the synchrotron radiation from secondary electrons produced by the \( p\gamma \) and \( γγ \) processes. The black dashed curve shows the spectrum before the attenuation on the EBL and indicates the degree of the internal to the source \( γγ \) absorption. Both models provide a satisfactory representation of the source’s SED without the need of external photon sources to account for the Fermi-LAT and H.E.S.S. data. The broad and curved \( γ\)-ray spectra obtained in both models are a natural outcome of the leptohadronic scenario, despite the fact that the radiative processes responsible for the X-ray and \( γ\)-ray emission are different. This can be understood by inspection of the various emission components that comprise the total emission from the sub-pc scale region.

The \( γ\)-ray emission in model A is mainly produced by the SSC emission of primary electrons (orange dashed line) and, in this regard, it resembles the pure leptonic SSC models (see e.g. fig. 3 in Sanchez et al. 2015). Note, however, that at \( 10^{7}–10^{15} \) Hz (~0.4–4 keV) the synchrotron emission from Bethe–Heitler pairs (red dash–dotted line) is comparable to the SSC one. The synchrotron emission from secondary pairs produced by the \( p\gamma \) and \( γγ \) processes dominates the \( γ\)-ray emission in the Fermi-LAT and
H.E.S.S. energy bands, similar to what have been shown for several other HBL (e.g. Petropoulou et al. 2015; Petropoulou, Coenders & Dimitrakoudis 2016). While in HBL the target photons for $p\pi$ interactions belong to the low-energy component of the SED, in the case of Ap Librae, which is an LBL, the photons of the low-energy hump are less energetic and typically cannot satisfy the energy threshold condition for pion production. In particular, for protons with Lorentz factors $\gamma_p$, the energy threshold condition for pion production is satisfied by photons with observed energies $\epsilon \gtrsim \delta_{0,1}\gamma_{p}/\gamma_{0}$, where $\delta_{0,1} = 145$ MeV. Given that the maximum energy of the protons is $\gamma_{p,\text{max}} \sim 10^{6}$ (10$^{7}$) in model A (model B), hard X-ray photons ($\gtrsim 1$ keV) will serve as targets for photopion interactions with the less energetic protons. As the energy threshold for Bethe–Heitler pair production is lower, protons with Lorentz factors $\gamma_{0}$ will interact with $\sim$keV (eV) photons. These simple estimates indicate that the resulting $\gamma$-ray emission is a non-linear combination of various radiative processes.

In model B, because of the larger $\gamma_{p,\text{max}}$ and stronger magnetic field, the proton synchrotron component dominates the soft-to-hard X-ray band (right-hand panel in Fig. 1), while the synchrotron radiation from Bethe–Heitler and $\gamma\gamma$ interactions produces a component to the observed photon spectrum (red dash–dotted line). Electrons produced by Bethe–Heitler interactions much above the threshold attain a maximum Lorentz factor $\gamma_{e,\text{pe}} \approx 4\gamma_{p}^{2}/\epsilon_{i}$, where $\epsilon_{i}$ is the energy of the target photon (e.g. Kelner & Aharonian 2008). Thus, the characteristic synchrotron photon energy is $\propto B\gamma_{p}^{2}$ (see also PM15). Based on the parameter values listed in Table 1 and Fig. 1 (right-hand panel), the peak energy of the Bethe–Heitler component in model B is expected to be $\sim 3500$ larger than in model A, i.e. $\sim 0.1$ GeV.

Thus, the theoretical spectra differ significantly in the relative importance of the various emission processes, despite the small differences in the adopted parameter values of models A and B. Our results reflect the non-linearity of the radiative processes that have to be present in a system that contains relativistic electrons and protons.

### 4.2 Variable VHE core emission

The decomposition of the SED obtained in models A and B revealed their differences in the origin of the X-ray and $\gamma$-ray emission. Different X-ray and $\gamma$-ray variability signatures are, therefore, expected. Regardless, both models predict variable $\gamma$-ray emission on time-scales similar to those in X-rays, in contrast to the scenarios that attribute the TeV emission to the kpc-scale jet of Ap Librae.

To illustrate the model predictions on the variability and the broad-band spectral evolution we present an indicative example of a flaring event. An increase of the observed flux (i.e. flare) can be attributed, in general, to a higher injection rate of radiating particles at the dissipation region, which, in turn, may be caused by temporal modulations of the jet power. In the following, we model a fiducial flare caused by an increase in the injection compactness (or, equivalently luminosity) of primary electrons and protons given by

$$f_{i}(t) = f_{i}^{(0)} + \frac{A}{(t - \tau_{pk})^{2} + (A/2)^{2}},$$

where $t = t'/t_{\text{dyn}}$, $A = 2$, and $f_{i}^{(0)}$ is the value derived from fitting the SED (see Table 1). Here, the starting time $\tau = 0$ corresponds to the time that is needed to establish the steady-state emission shown in Fig. 1 and $\tau_{pk}$ is the peak time where $f_{i}(t_{pk}) = 2f_{i}^{(0)}$. We define $\Delta t_{\text{inj}}$ as A, i.e. the time interval where $f_{i}(\tau_{pk}) = 0.75f_{i}^{(0)}$, to be the measure of the injection’s duration. This correspond to $\Delta t_{\text{inj,par}} = t_{\text{inj}}(1 + z)/\delta_{D} = 1.9 h_{8}b_{1.3}^{2}/\delta_{D}$. Fig. 2 shows, in total, 20 snapshots (grey thin lines) of the broad-band emission during the flaring episode described above. Left-hand and right-hand panels correspond to models A and B, respectively. The time-averaged spectrum is also plotted (black dashed line), while no attempt in fitting the Fermi-LAT flare (red points) has been made. We find that changes in the luminosity of radiating particles alone do not affect the spectral shape either in the X-ray or the $\gamma$-ray bands. Interestingly, no significant spectral change was detected during the Fermi-LAT flare of 2013 (MJD 56306-56376).
Model-derived light curves for the fiducial flare described in text. The results obtained in models A and B are shown with solid and dashed lines, respectively. Here, $F$ is the integrated flux at different energy bands marked on the plot and $F_{\text{min}}$ is the respective value prior to the flare. The injection luminosity of particles (normalized to its minimum value) is also shown as a function of time (blue coloured lines).

**Table 3.** Amplitude and duration of the fiducial flare described in text at X-rays (2–10 keV), HE (0.1–300 GeV) and VHE (0.1–6 TeV) γ rays. The respective fluxes prior to the flare ($F_{\text{min}}$) are also listed.

<table>
<thead>
<tr>
<th>Energy Bands</th>
<th>Pre-flare flux: $F_{\text{min}}$ (erg cm$^{-2}$ s$^{-1}$)</th>
<th>Amplitude: $F_{\text{pk}}/F_{\text{min}}$</th>
<th>Duration: $\Delta t_{75%}$ (h)</th>
</tr>
</thead>
<tbody>
<tr>
<td>2–10 keV</td>
<td>Model A: 6.8 × 10$^{-12}$</td>
<td>Model A: 2.4</td>
<td>Model A: 3.0</td>
</tr>
<tr>
<td></td>
<td>Model B: 3.7 × 10$^{-12}$</td>
<td>Model B: 1.8</td>
<td>Model B: 8.6</td>
</tr>
<tr>
<td>0.1–300 GeV</td>
<td>4.8 × 10$^{-11}$</td>
<td>3.2</td>
<td>2.3</td>
</tr>
<tr>
<td>0.1–6 TeV</td>
<td>5.2 × 10$^{-12}$</td>
<td>3.6</td>
<td>2.6</td>
</tr>
<tr>
<td></td>
<td>4.1 × 10$^{-12}$</td>
<td>3.6</td>
<td>2.6</td>
</tr>
</tbody>
</table>

(H.E.S.S. Collaboration et al. 2015). The flux variations in the optical/UV energy bands are less pronounced than these at higher energies, although the radiating primary electrons are more energetic than those emitting at ~0.1–1 keV X-rays. The reason is that the observed optical/UV emission has a significant contribution from the host galaxy itself, while the primary synchrotron component is sub-dominant (see Fig. 1).

The integrated flux in different energy bands, normalized to its pre-flare value ($F_{\text{min}}$), is presented as a function of time in Fig. 3. For comparison reasons, the ratio $\ell_i/\ell_0^{(0)}$ is also shown (blue coloured lines). In both models, we find no time-lag between the X-ray and γ-ray energy bands. Unless there is a time-lag in the injection of accelerated electrons and protons, the flares predicted by the models are (quasi)-simultaneous. The properties of the light curves obtained in models A and B, namely peak flux $F_{\text{pk}}$ and duration are summarized in Table 3. The amplitude of the flare is larger at higher energies and its shape becomes more symmetric, i.e. the rise and decay time-scales are similar. In both models, the rise time-scales of the flares in X-rays and γ-rays are similar. On the contrary, the γ-ray flares appear to be shorter in duration compared to those in X-rays. In particular, we find that the X-ray flare is twice as long as the injection episode, namely $\Delta t_{75\%} \sim 4t_{\text{dyn}}$, where $t_{\text{dyn}} \simeq 0.75$ h (2.11 h) is the crossing time of the source in the observer’s frame for Model A (Model B). The γ-ray flare is shorter than the X-ray flare by one $t_{\text{dyn}}$ in both models. Because of the superposition of various emitting components at different energy bands, it is not straightforward to provide an explicit expression for the expected flare duration. This can be, however, qualitatively understood; the faster decay time-scale of the γ-ray flares reflects the shorter cooling time-scale of the radiating (secondary) electrons, which are typically more energetic than those emitting in X-rays (see section 3.1 in PM15).

Although the injection luminosity function for primary electrons and protons is the same in models A and B, the obtained peak fluxes are lower in the latter. The differences are related to the underlying physical process responsible for the X-ray and γ-ray emission. For example, the X-ray emission in model B is expected to be $\propto t_{\text{dyn}}$, since it is dominated by the proton synchrotron radiation. On the contrary, the X-ray variability amplitude in model A is expected to be larger than in model B, since the X-ray emission is a superposition of the SSC and Bethe–Heitler components that respectively depend on the varying $\ell_\gamma$ and $\ell_\gamma$.

An interesting point to be considered is the detectability of the X-ray flux variability with *Swift*/XRT during a fiducial γ-ray flare, as shown in Fig. 3. The source has been so far observed with *Swift*/XRT for a few ks, with single observations being usually split to several (two to four) snapshots with exposure times less than 1 ks. Based on the count rate of the existing *Swift*/XRT observations, a one ks exposure would deliver approximately 100 counts. A flux increase by a factor of two, as shown in Fig. 3, would be detectable with *Swift*/XRT above a 3σ level. This could be achieved with multiple observations (of at least 1 ks exposure time) spanning over the duration of the fiducial flare. The detectability of a TeV flare with the next generation of IACTs is discussed in the following section.

5 PROSPECTS FOR CTA

Ap Librae has been one of the few VHE emitting LBL objects and it was first discovered by H.E.S.S. (Hofmann 2010; H.E.S.S. Collaboration et al. 2015). As discussed by the authors, H.E.S.S. was able to detect the system with a significance of 6.6σ during an integrated exposure time of 14 h. The Cherenkov Telescope Array (CTA, Actis et al. 2011; Acharya et al. 2013) is a next-generation observatory of IACT. It is planned to cover more than 1 km$^2$ area and will be composed of an array of large, middle, and small-sized telescopes. When completed, CTA is expected to reach an effective area larger than the Cherenkov light pool size, and deliver a sensitivity about an order of magnitude better than that of current IACT and water Cherenkov telescopes. In principle, CTA will be therefore able to detect Ap Librae at a fraction of the time needed by H.E.S.S.

In order to test this we created simulated light curves of the VHE flares (0.1–6 TeV) predicted by the models A and B (Fig. 3) using the software package *ctools*\(^9\) (Knödlseder et al. 2016). Our simulated events are drawn from three components (i) a point source with the spectral properties of Ap Librae, (ii) an isotropic CR background that was modelled as a diffuse isotropic source with a spectral shape and flux adopted by Silverwood et al. (2015) (see Fig. 2 therein) and (iii) an instrumental background of the detector (see *ctarrbackground* of *ctools*). We used the task *ctobssim* to simulate the event files, and the *ctlike* tool to perform a maximum likelihood fitting of a power-law model (photons index 2.65) to the unbinned simulated data. Finally the *ctisomap* tool was used to confirm the significance

9 http://cta.irap.omp.eu/ctools/
of the detection. The procedure was repeated for various flux levels of the models shown in Fig. 3. The simulated data were binned in intervals of 0.5 h for model A and 5 h for model B. In both cases, the adopted bin size is less than the maximum visibility of the system during a single day.

The results of our simulations are presented in Fig. 4. For a TeV flare with ~2.3 h duration and flux increase by factor of 2 compared to the quiescent flux level (model A; see Table 3), we find that such variability would be detected by CTA even with short exposure times (0.5 h). In particular, at the peak time of the flare the significance of the detection would exceed 15σ (see left-hand panel in Fig. 4). A detection significance similar to that of H.E.S.S. (~6σ) would be achieved for the quiescent flux levels but at a fraction of the integrated exposure time of H.E.S.S. A longer exposure time (5 h) was adopted for the longer duration flare predicted by model B. Despite the lower peak flux of the flare (see also Table 3), the expected number of counts at the peak time of the flare is six times larger than that of flare A due to the larger exposure time. For a 5 h exposure time, the lowest significance that can be reached is still above 15σ.

6 DISCUSSION

We have presented two indicative models for explaining the broad high-energy spectrum of Ap Librae with their parameters listed in Table 1. Both models are viable alternatives, when only considering their ability of reproducing the observed SED. However, they differ in terms of energetic requirements. The power of a two-sided jet can be written as (e.g. Ghisellini et al. 2014)

\[ P_j = 2 \pi r_c^2 c^2 \sum u_i \left( \frac{8}{3} \frac{\Gamma^2}{\beta^2} \right) L_{ph}, \]

where \( u_i (i = e, p, B) \) is the energy density as measured in the respective rest frame, \( L_{ph} \) is the apparent photon luminosity and the last term in the right-hand side of the equation is the bolometric absolute photon power (e.g. Dermer, Murase & Takami 2012). The inferred jet power for models A and B is respectively \( 10^{46} \) erg s\(^{-1}\) and \( 10^{47} \) erg s\(^{-1}\) to be compared to the jet radiation power \( P_j \sim 3 \times 10^{42} \) erg s\(^{-1}\) and the Eddington luminosity of Ap Librae \( L_{Edd} \sim 3 \times 10^{46} \) erg s\(^{-1}\), for a black hole mass \( M_{BH} = 10^{3.4 \pm 0.6} M_\odot \) (Woo et al. 2005). It is interesting to note that even in scenarios that invoke the presence of relativistic electrons alone, the jet power may be as high as \( 10^{47} \) erg s\(^{-1}\) (see e.g. Hervet et al. 2015).

If the accretion operates in the magnetically arrested (MAD) regime (Narayan, Igumenshchev & Abramowicz 2003), the jet power may be related to the accretion power, \( M c^2 \), where \( \eta_j \sim 1.5-3 \) ( McKinney, Tchekhovskoy & Blandford 2012; Tchekhovskoy & McKinney 2012) with higher \( \eta_j \) values obtained for faster spinning black holes and thicker discs. Adopting \( \eta_j = 2 \), the accretion power for models A and B is, respectively, \( 5 \times 10^{47} \) erg s\(^{-1}\) and \( 5 \times 10^{48} \) erg s\(^{-1}\). The luminosity of the accretion flow can be estimated from the BLR luminosity assuming a covering factor \( \xi \), i.e. \( L_{disc} \lesssim \frac{2}{3} L_{BLR, k} \xi_L \), and the radiative efficiency is given by \( \epsilon = L_{disc}/M c^2 = 2 \times 10^{-3} \) (2 \( \times 10^{-3} \)) for model A (model B). The low radiative efficiency in this source is not a feature unique to our model (see also Hervet et al. 2015).

Assuming that the magnetic field is mostly toroidal at pc scales it can be written as \( B' = (4P_m/c)^{1/2}(R \Gamma \theta_j)^{-2} \), where \( P_m \) is the jet power carried by the magnetic field, \( R \simeq r_j/\theta_j \) is the distance from the black hole and \( \theta_j \) is the opening angle of the jet. At sub-pc scales we found that most of the contribution to the jet power comes from the relativistic proton component, i.e. \( P_j \simeq P_p \). Assuming that the ratio \( P_j/P_p \) remains constant from the sub-pc to the pc scales and equal to \( \sim 10^{-4} \) for model B (model A), the magnetic field at \( R = 5 \) pc is estimated to be \( 16 \) mG (3 mG) for \( \Gamma \theta_j \sim \Gamma \theta_p \sim 0.5 \) (see Table 1). Thus, the magnetic field strengths in both models is comparable to the adopted value for the pc-scale emitting region in this work (see Table 2). Alternatively, it could be that \( P_j \leq P_p \) at the pc scales of the jet. However, the estimated magnetic field would be then close to 1 G, i.e. larger than the adopted value at Table 2 (see also Pushkarev et al. 2012).

In general, the energetic comparison of the two models suggests that solutions with higher magnetic field strengths in the (sub-pc) emitting region are favoured. Here, we did not aim at finding the most ‘economic model’ that describes the SED of Ap Librae, so we

Figure 4. Simulated CTA light curves for models A (left-hand panel) and B (right-hand panel). The event files were generated according to the 0.1–6 TeV light curves shown in Fig. 3. A time binning of 0.5 and 5 h was used for the simulated light curves of models A and B, respectively. The expected number of source counts is shown in the top panel of both plots. Colour coding is used for the significance of the detection (in Gaussian σ) as obtained by the analysis of the simulated event files.
cannot exclude models with sub-Eddington accretion and jet powers (see e.g. Petropoulou & Dermer 2016). Other solutions characterized by lower jet powers, higher magnetic field strengths and larger blobs are also expected to be closer to equipartition ($P_e \sim P_B$). We plan to search for the model that minimizes the jet power by scanning the available parameter space in the future. In summary, our results outline a physical picture where the jet is initially Poynting-flux dominated, it dissipates a significant fraction of its magnetic energy to relativistic protons at sub-pc scale distances, and extends to pc scale distances with a constant ratio of magnetic-to-(relativistic) particle powers.

The low-energy spectrum from the compact, high-energy emitting blob cuts off at $\sim 10^{22}$ GHz, being unable to explain the radio observations at lower frequencies. To account for the radio emission in Ap Librae, we assumed that this originates from a more extended region of the jet, which we approximated by a spherical blob with characteristic radius $r' \sim 1$ pc; a more detailed description of the pc-scale jet lies out the scope of this paper. It is intriguing to discuss the possibility of a physical connection between the sub-pc and pc-scale blobs. On the one hand, the electron and magnetic field energy densities in the pc-scale blob are $\sim 10^{16} \sim 10^9$ times smaller than those inferred for the compact region (see Table 3). Since $r' / r_{\gamma} \sim 10^3$, this is compatible with a scenario of a conical jet where the energy densities are expected to decrease as $\sim 1/r^2$. On the other hand, without new injection of electrons, it is difficult for a blob that produces a high-energy flare (in X-rays and $\gamma$-rays) to also produce a radio flare later, after it has sufficiently expanded. The reason is that the jets that are responsible for the radio emission are typically very energetic and not the result of excessive adiabatic cooling. However, if the electron injection continues from the sub-pc to the pc-scale jet, a delayed radio flare with respect to the $\gamma$-ray one may be expected on a time-scale of $3 \times 10^6 s r_{\gamma} / \delta_0, 1$ (see Table 2). In this scenario, therefore, fast ($\sim h$) X-ray and $\gamma$-ray flares caused by a strong jet episode may be followed by radio flares a few months later (see Hovatta et al. 2015, for Mrk 421).

7 SUMMARY

We have shown that the superposition of different emission components related to photodisproportionate interactions can explain the HE and VHE $\gamma$-ray emission of Ap Librae without invoking external radiation fields. This was exemplified with two indicative model fits to the SED of Ap Librae where the VHE emission was assumed to originate from the core of the jet, i.e. from a compact, sub-pc scale region. Our model for the non-thermal emission of Ap Librae predicts (quasi-)simultaneous flares at X-rays, HE and VHE $\gamma$-rays. The flare duration in the aforementioned energy bands is of the same order of magnitude, with shorter durations and larger variability amplitudes obtained at higher energies. In addition, no spectral changes during the flares are expected, unless the slope of the radiating particles changes. We showed that CTA would be able to detect $\sim h$ time-scale variability at $E_{\gamma} > 0.1$ TeV at high significance with shorter exposure times than existing IACT and water Cherenkov telescopes. Detection of flux variability in GeV $\gamma$-rays and/or X-rays could be therefore used to trigger pointing observations of Ap Librae with CTA. The detection of VHE variability on similar time-scales as those observed in X-rays and GeV $\gamma$-rays would point towards a common emitting region of sub-pc scale. Although it could not rule out a kpc-jet origin of the quiescent VHE emission, as the latter could still be explained by an additional emitting component, a model of a sub-pc scale origin would be preferred in the spirit of Oekham’s razor.

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