

# VDES J2325–5229 a $z = 2.7$ gravitationally lensed quasar discovered using morphology-independent supervised machine learning

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## ABSTRACT

We present the discovery and preliminary characterization of a gravitationally lensed quasar with a source redshift  $z_s = 2.74$  and image separation of 2.9 arcsec lensed by a foreground  $z_l = 0.40$  elliptical galaxy. Since optical observations of gravitationally lensed quasars show the lens system as a superposition of multiple point sources and a foreground lensing galaxy, we have developed a morphology-independent multi-wavelength approach to the photometric selection of lensed quasar candidates based on Gaussian Mixture Models (GMM) supervised machine learning. Using this technique and  $gi$  multicolour photometric observations from the Dark Energy Survey (DES), near-IR  $JK$  photometry from the VISTA Hemisphere Survey (VHS) and WISE mid-IR photometry, we have identified a candidate system with two catalogue components with  $i_{AB} = 18.61$  and  $i_{AB} = 20.44$  comprising an elliptical galaxy and two blue point sources. Spectroscopic follow-up with NTT and the use of an archival AAT spectrum show that the point sources can be identified as a lensed quasar with an emission line redshift of  $z = 2.739 \pm 0.003$  and a foreground early-type galaxy with  $z = 0.400 \pm 0.002$ . We model the system as a single isothermal ellipsoid and find the Einstein radius  $\theta_E \sim 1.47$  arcsec, enclosed mass  $M_{\text{enc}} \sim 4 \times 10^{11} M_\odot$  and a time delay of  $\sim 52$  d. The relatively wide separation, month scale time delay duration and high redshift make this an ideal system for constraining the expansion rate beyond a redshift of 1.

**Key words:** gravitational lensing: strong – methods: observational – methods: statistical – quasars: general.

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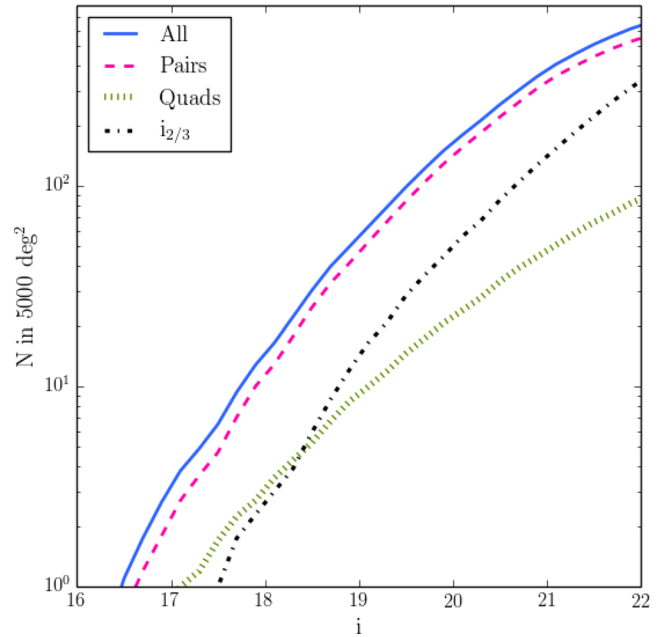
## 1 INTRODUCTION

The discovery of the first strong gravitational lens (Walsh, Carswell & Weymann 1979) brought forth a powerful tool to study cosmology and astrophysics. Systems where the background source is a quasar can be used to map the dark matter substructure (e.g. Mao & Schneider 1998; Kochanek & Dalal 2004; Vegetti et al. 2012; Nierenberg et al. 2014), to determine the mass (e.g. Morgan et al. 2010) and spin (Reynolds et al. 2014) of black holes, to measure the properties of distant host galaxies (e.g. Kochanek, Keeton & McLeod 2001; Claeskens et al. 2006; Peng et al. 2006) and to measure the value of the Hubble constant  $H_0$ . The constraints on cosmological parameters in particular are comparable in precision to baryonic acoustic oscillation methods (e.g. Suyu et al. 2010, 2013; Bonvin et al. 2016). In addition to that, the effects of microlensing of the quasar induced by the stars in the lens galaxy can be used to probe the physical properties of quasar accretion discs such as the wavelength dependence of the size of the accretion disc (e.g. Poindexter, Morgan & Kochanek 2008).

Large samples of new quasar lens systems were discovered through dedicated surveys in radio, like the Cosmic Lens All Sky Survey (CLASS; Myers et al. 2003; Browne et al. 2003), which, in combination with the Jodrell Bank VLA Astrometric Survey (JVAS; King et al. 1999), found 21 new lens systems, and in the optical, such as the SDSS (Sloan Digital Sky Survey) Quasar Lens Search (SQLS; Oguri et al. 2006, 2008; Inada et al. 2008, 2010, 2012), which discovered 49 new lensed systems.<sup>1</sup> The future of the field is currently hindered by the need for more lenses. This can be achieved, according to Oguri & Marshall 2010 (hereafter OM10), not by increasing the depth of the searches, but the area. Therefore, surveys such as the Dark Energy Survey (DES; DES Collaboration 2005; DES Collaboration et al. 2016) and, in the future, the Large Synoptic Survey Telescope (LSST; Ivezić et al. 2008) are capable of more than doubling the current quasar lens sample size.

The chance of a given quasar being lensed was determined by OM10 to be  $\sim 10^{-3.5}$ , which is comparable to what was obtained with SQLS. (It shows a rate of quasar lensing of  $\sim 10^{-3.3}$ .) In Fig. 1 we show the expected number of lenses in the full DES survey area as a function of  $i$ -band magnitude according to the predictions by OM10. We show the expected numbers for pairs and quads (lenses with four quasar images) according to the magnitude of the brightest image in the system ( $i_1$ ). For comparison, we also plotted the expected number of lenses according to the magnitude of the fainter image (for pairs) or the third brightest image (for quads),  $i_{2/3}$ , which is the limit used by OM10.

With 50 lensed quasar systems with  $i_1 < 19.0$  expected in DES, the challenge becomes how to identify them. SQLS started from a spectroscopic sample of quasars. However, the relatively low numbers of confirmed quasars in the Southern hemisphere sky, and the fact that a large spectroscopic survey is not planned for the next few years, requires a method to photometrically select quasars to look for lenses. Traditionally, that selection would rely on the use of the  $u$  band to look for UVX objects (e.g. Croom et al. 2001; Richards et al. 2002). The lack of this band in DES requires the use of the near- and mid-IR to make the selection. The use of mid-IR has been applied efficiently for flux-limited quasar selection (e.g. Stern et al. 2012; Assef et al. 2013) and DiPompeo et al. (2015) have shown that the use of SDSS+WISE photometry provided results similar to those obtained with SDSS+UV+near-IR data.



**Figure 1.** Expected number of quasar lenses in the full DES area as a function of the magnitude of the brightest quasar image. The blue solid line shows the overall expected number of systems, while the dashed pink line and the dotted green line show the number of pairs and quads, respectively. The dot-dashed black line shows the expected number of lenses as a function of the magnitude of the second brightest quasar image for pairs and third brightest image for quads.

Here, we present results of a search for gravitationally lensed quasars from DES Year 1 observations (Diehl et al. 2014), obtained between 2013 August 31 and 2014 February 10, combined with  $JK$  near infrared observations from the VISTA Hemisphere Survey (VHS; McMahon et al. 2013; ESO Observing Programme 179.A-2010) and Wide Infra-red Survey Explorer (WISE; Wright et al. 2010). All magnitudes are quoted on the AB system. The conversions from Vega to AB that have been used for the VISTA data are:  $J_{AB} = J_{\text{Vega}} + 0.937$  and  $K_{sAB} = K_{s\text{Vega}} + 1.839$ . These are taken from the Cambridge Astronomical Survey Unit's website.<sup>2</sup> The conversions for the ALLWISE data are  $W1_{AB} = W1_{\text{Vega}} + 2.699$  and  $W2_{AB} = W2_{\text{Vega}} + 3.339$  which are given in Jarrett et al. (2011) and in the ALLWISE explanatory supplement.<sup>3</sup> When required, a flat cosmology with  $\Omega_m = 0.3$  and  $H_0 = 70.0 \text{ km s}^{-1} \text{ Mpc}^{-1}$  was used unless otherwise specified.

## 2 CANDIDATE SELECTION AND MODELLING

### 2.1 Photometric data

Our selection strategy is based on the identification of objects with quasar-like colours that either appear as close pairs or exhibit shape parameters that differ from single point sources. While the motivation for the first criterion is obvious: lensed quasars will appear as multiple images in the sky; the reasoning for the second criterion arises from the fact that, with a median seeing varying between 0.87

<sup>2</sup> <http://casu.ast.cam.ac.uk/surveys-projects/vista/technical/filter-set>

<sup>3</sup> The ALLWISE explanatory supplement, [http://wise2.ipac.caltech.edu/docs/release/allwise/expsup/sec5\\_3e.html](http://wise2.ipac.caltech.edu/docs/release/allwise/expsup/sec5_3e.html), directs the reader to the WISE All-Sky explanatory supplement for the conversions; [http://wise2.ipac.caltech.edu/docs/release/allsky/expsup/sec4\\_4h.html#summary](http://wise2.ipac.caltech.edu/docs/release/allsky/expsup/sec4_4h.html#summary).

<sup>1</sup> <http://www-utap.phys.s.u-tokyo.ac.jp/sdss/sqls/lens.html>

and 1.17 arcsec across bands, only wider separation lensed quasars in DES will appear as deblended sources. This becomes an even greater problem if the lensing galaxy is bright enough to contaminate the quasar images, posing a complex problem for source segmentation. Even if the individual components of a lensed quasar system are deblended, the pixel assignment to each segmented source is uncertain and the measured catalogue parameters for each quasar image might not manifest as a canonical point source.

One can define morphology as the difference between *psf* and *model* magnitudes in one or more bands:  $\text{mag}_{\text{psf}} - \text{mag}_{\text{model}}$ . Effectively, this is the difference between the best-fitted local point spread function and the radial light profile of a galaxy. When compared to  $\text{mag}_{\text{psf}}$ , the value of  $\text{mag}_{\text{model}}$  for extended objects will show an excess since their light profiles will extend beyond what is enclosed by the PSF modelling. However, pixel assignment may wrongly distribute flux from companion sources and hence lead to an overestimation of  $\text{mag}_{\text{model}}$  and subsequently cause two adjacent point sources to appear non-stellar in the catalogue. Tests performed with lenses simulated according to OM10 mock catalogue of lensed quasars confirm this result. With 4400 lenses with separations varying between 0.5 and 4.0 arcsec and with  $i < 21.5$  for the input magnitudes for the source quasar, we find that no system with image separation less than 1.5 arcsec is segmented and only 23 per cent of pairs are deblended into separate sources. Out of those, only 32 per cent are deblended into point sources. For wider separation lenses, where more massive lensing galaxies can be expected, the contamination by the lensing galaxy on the *model* magnitude of the quasar images is evident, with only 9 per cent of the systems where  $i_{\text{lens}} < 20.0$  deblending into point source quasar images. When one looks at systems where  $z_{\text{lens}} < 1.0$ , where the lens galaxy makes a bigger contribution, only 25 per cent of the lenses show point source quasar images.

This calls for a search for objects with quasar colours regardless of image morphology. Ideally, such a technique would also include objects where lensing galaxy flux is present but this is beyond the scope of this paper and will be presented elsewhere (Ostrovski et al., in preparation). Previous quasar selection work such as was done by SDSS focused on selection of point sources prior to the colour selection criterion. Extended sources were selected only if they showed colours that were very different from those of quiescent galaxies (Richards et al. 2002). Thus lensed quasar surveys such as SQLS will be biased against unresolved candidates. Difference imaging, as suggested by Kochanek et al. (2006), could also be used with DES multi-epoch observations to identify lensed quasars in those cases where a lensed quasar component exhibits variability.

In our selection we use DES Y1 data from the first annual release (Y1A1) co-added catalogue, which cover an area of approximately 1800 deg<sup>2</sup> in the Southern hemisphere sky (Bechtol et al. 2015). DES images are obtained using the Dark Energy Camera (Flaugher et al. 2015) and reduced through the DES Data Management system (Mohr et al. 2012) using the source extraction code *SEXTRACTOR* (Bertin & Arnouts 1996). Candidates are selected from an input sample composed of the set of all objects brighter than  $i_{\text{auto}} < 19.0$  in the DES Y1 co-added catalogue which have valid photometry in the *g* band and are a match to WISE within a 2 arcsec search radius. Objects are also matched to VHS, which includes  $\sim 1700$  deg<sup>2</sup> of overlap area with DES, to obtain photometry in *J* and *K* using a 1.44 arcsec search radius. Given the bright limit in our sample, the selection will be performed on a high signal-to-noise ratio (S/N) regime and as such it should lead to good performance. The final *giJKW1W2* photometric sample on which the gravitationally lensed quasar selection will be performed contains  $\sim 4.2 \times 10^6$  objects.

The quasar-like colour similarity is calculated in a five-dimensional colour space composed of  $g - i$ ,  $i - W1$ ,  $J - K$ ,  $K - W1$  and  $W1 - W2$ . For the DES bands we use *auto* magnitudes. The *auto* magnitudes are intended as an estimate of the total flux given by a Kron-like (Kron 1980) automatic aperture. While *psf* magnitudes are optimized to measure the fluxes of stars and *model* magnitudes are well suited for galaxies, blended quasar lenses would not be well represented by either model. By using a magnitude defined by an elliptical aperture based on the second-order moments of the object's light distribution, at least 90 per cent of the flux should be included and we hope to get well-represented colours independent of object shape. For lensed systems in particular, we want to avoid losing light from one of the components, i.e. having a *psf* magnitude centred on the lensing galaxy only, and a subsequent misclassification. For the VHS bands we use aperture magnitudes (with an aperture radius  $r = \sqrt{2}$  arcsec), analogous to the DES *SEXTRACTOR auto* magnitudes. For the lower resolution (FWHM = 6 arcsec) WISE bands we use the profile-fitting photometry made available in the catalogues. Given the low resolution of the survey, all objects regardless of morphology appear as point sources.

## 2.2 Supervised machine learning

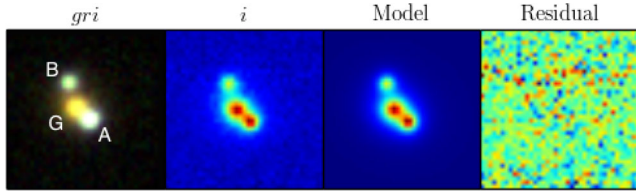
We apply supervised machine learning to select the candidates. In this work, we use Gaussian Mixture Models (GMM) implemented using *astroML* (Vanderplas et al. 2012) and *scikit-learn* (Pedregosa et al. 2011) tools and trained on objects from the Stripe-82 area (S82), a 2:5 wide stripe along the Celestial Equator in the Southern Galactic Cap imaged multiple times by SDSS (Abazajian et al. 2009) and other surveys of varying wavelengths. In DES Y1, S82 covers an area of  $\sim 167$  deg<sup>2</sup>. The S82 sample was selected in a similar way to our input sample, but we required all five DES bands to have valid photometry. The resulting sample contains 258 267 objects, 836 of which are spectroscopically confirmed type 1 quasars from the training set used by Richards et al. (2015) in their classifier. Given the  $i < 19.0$  mag limit we are using and the multi-survey spectroscopic follow-up in S82, we believe we have a complete type 1 quasar sample to train on. Objects in the training set are separated into two classes, quasars and non-quasars, and the GMM method models each class as a set of 10 Gaussians.

Tests to evaluate the method's performance with different combinations of colours were conducted by separating 25 per cent of this training set into a testing sample. Results show that  $\sim 88.8$  per cent of the quasars are recovered and the rate of false positives, that is sources that are classified as quasars but are not quasars, is  $\sim 27.0$  per cent. The classes are assigned based on the highest probability and no minimal thresholds were required. A paper detailing this method is under preparation (Ostrovski et al., in preparation).

The GMM returns 19 651 quasar candidates from the input sample, out of which 70 are pairs within 10 arcsec of each other. As expected, most of those objects ( $\sim 61$  per cent) are point sources. We consider an object to be stellar-like if  $i_{\text{psf}} - i_{\text{model}} < 0.1$ , a more conservative approach than what was done in the SDSS photometric survey (Stoughton et al. 2002). By removing point sources from our candidate list, we reduce it to 7634 objects. A quick visual inspection of some of the candidates shows that low-redshift galaxies are the most obvious contaminants. This group includes starburst galaxies and  $z < 0.8$  quasars, where, given DES depth, surface brightness limit and resolution, the host galaxy of the AGN becomes prominent. Table 1 summarizes the cleaning and selection steps applied to the original DES Y1 sample down to the final visual inspection sample containing 4478 objects that led to the

**Table 1.** Candidate selection.

Criterion	Objects remaining
DES Y1: $i_{\text{auto}} < 19.0$	7159 768
Valid $g_{\text{auto}}$	7114 967
Match to WISE	5156 101
Match to VHS	4344 994
Valid <i>JKW1W2</i>	4171 836
GMM quasars	19 651
$i_{\text{psf}} - i_{\text{model}} > 0.1$	7634
Visual inspection (equation 1)	4778

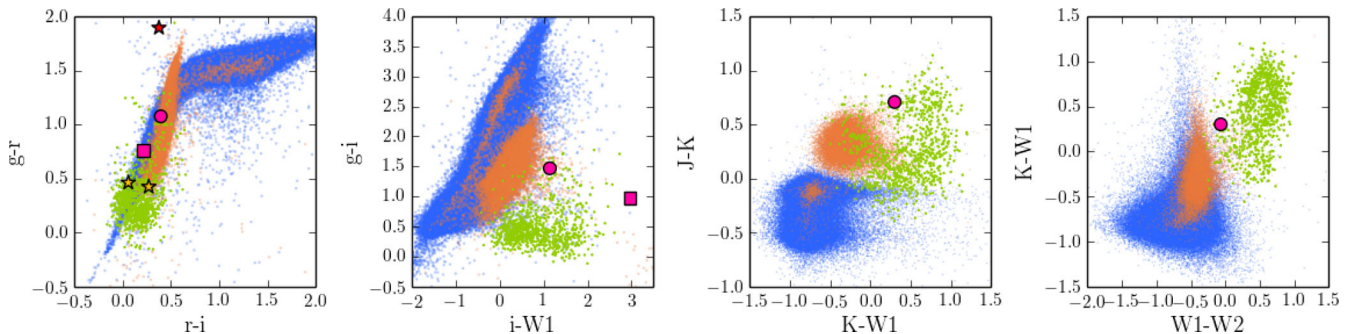
**Figure 2.** J2325–5229 as a  $g$ ,  $r$ , and  $i$  DES Y1 colour composite, an  $i$ -band image, an  $i$ -band image model and the residuals from subtracting the model from the image. All cutouts are 10.0 arcsec in size. North is up and East is left.

discovery of J2325–5229. We list the different criteria applied and the remaining number of objects after each step.

Motivated by the morphologies displayed by the simulated OM10 lenses, we selected for visual inspection objects that displayed the following morphological criteria:

$$\begin{cases} 0.2 < i_{\text{psf}} - i_{\text{model}} < 1.9; \\ \text{ellipticity} < 0.3. \end{cases} \quad (1)$$

Colour composites made of DES  $g$ ,  $r$ , and  $i$  bands were generated and VDES J2325–5229, shown in Fig. 2, stood out. The separation between the two blue components, J2325–5229 is only deblended into a double source in the DES catalogue and appears as a single source in the VHS catalogue. That being the case, the north-most blue object, B, did not match to a VHS counterpart within 1.44 arcsec (0:0004) and therefore was not in the test sample. This is the reason why J2325–5229 was not flagged as a pair. The candidate selection was solely based on the fact that the south-most component of the system, made of A+G, shows quasar colours and an extended

**Figure 3.** Colour–colour plots showing the location of J2325–5229 (pink circle) in different colour spaces. The pink square shows the location of the north-most blue object. We did not assign W1 flux to each counterpart, so values on the second diagram show, for both cases, the sum of all flux in that band. For comparison, the colour locus of quasars (green), point sources (blue) and extended sources (orange) are populated by the objects present in the GMM training set. The lensing galaxy dominates the colours of the system, making J2325–5229 an outlier of the quasar colour locus. In the left-most plot the stars represent each component of the system after 2D modelling for the photometry (quasar images are yellow and lensing galaxy is red). All magnitudes are in the AB system.**Table 2.** J2325–5229 photometry.<sup>a,b</sup>

$g_{A+G;B}$	$20.08 \pm 0.01$	$21.41 \pm 0.01$	$J_{A+G+B}$	$18.48 \pm 0.02$
$r_{A+G;B}$	$19.01 \pm 0.01$	$20.65 \pm 0.01$	$H_{A+G+B}$	$18.06 \pm 0.02$
$i_{A+G;B}$	$18.61 \pm 0.01$	$20.44 \pm 0.01$	$K_{A+G+B}$	$17.78 \pm 0.03$
$z_{A+G;B}$	$18.26 \pm 0.01$	$20.09 \pm 0.01$	$W1_{A+G+B}$	$17.48 \pm 0.03$
$Y_{A+G;B}$	$18.14 \pm 0.04$	$19.95 \pm 0.07$	$W2_{A+G+B}$	$17.54 \pm 0.04$

Notes. <sup>a</sup>All quoted magnitudes are AB.

<sup>b</sup>Magnitudes are auto for DES,  $\sqrt{2}$  arcsec aperture for VHS and measured with profile-fitting photometry for WISE.

morphology and visual inspection was vital. The photometry of this component is dominated by the red central object, as can be seen in the colour–colour plots in Fig. 3. In those plots, the candidate tends to lie closer to the galaxy colour locus, which means that classical colour cuts such as those applied by Agnello et al. (2015) would not have classified this object as one or multiple quasars. This shows the importance of not applying any sort of pruning to the input sample. The photometry for J2325–5229 is detailed in Table 2. In Fig. 3 we also show the photometry for component B, when available.

### 2.3 2D modelling

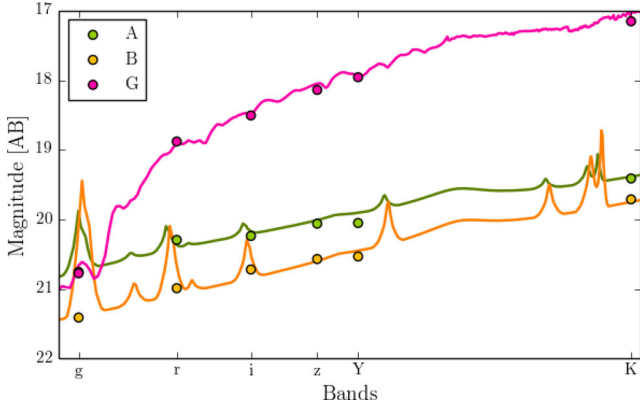
Once a lensed quasar candidate is selected from visual inspection, the next stage is to perform a 2D modelling of the system to ascertain what model the sources are most consistent with and to obtain photometry for each component. We modelled J2325–5229 in all five DES bands and in VHS  $K$  band. Image quality made the modelling in the  $J$  band unreliable and the resolution from WISE makes it impossible to resolve components with these separations. The positions of each component are listed in Table 3.

The modelling, analogous to what was done by Auger et al. (2011), used PYTHON routines to combine two Moffat profile PSFs plus a Sérsic profile galaxy convolved with the PSF for the system’s image. In Fig. 2 the  $i$ -band image, the model image and the residual signal obtained from subtracting the two images are displayed. The ellipticity of the lensing galaxy, according to the best model, is  $q = 0.19 \pm 0.03$  with a position angle of  $70^\circ \pm 5^\circ$ . The Sérsic index is  $3.9 \pm 0.4$ .

For each component, the modelled photometry is listed in Table 3 and from those values it is possible to plot spectral energy distributions (SED) for each component, which can be seen in Fig. 4. As was evident from the colours of the A+G blended component, the

**Table 3.** J2325–5229 modelled positions, photometry and photometric redshift.

Obj	RA	Dec.	$\Delta\alpha$ (arcsec)	$\Delta\delta$ (arcsec)	$\delta R$	PA ( $^\circ$ )	<i>g</i>	<i>r</i>	<i>i</i>	<i>z</i>	<i>Y</i>	<i>K</i>	Photo- <i>z</i>
G	23:25:41.20	−52:29:15.1	0.00	0.00	0.00	00.0	20.77	18.88	18.50	18.14	17.95	17.15	0.302
A	23:25:41.10	−52:29:15.9	−0.94	−0.80	1.23	229.6	20.75	20.29	20.24	20.06	20.05	19.41	2.920
B	23:25:41.25	−52:29:13.5	0.49	1.72	1.79	15.9	21.41	20.99	20.72	20.57	20.53	19.71	2.960
A-B	—	—	−1.43	−2.52	2.90	29.6	−0.66	−0.70	−0.48	−0.51	−0.48	−0.30	—


**Figure 4.** SEDs of the three components of the J2325–5229 system after modelling the photometry. The continuous lines show the best-fitting SED template fitted by LePHARE.

lensing galaxy is brighter than the quasar images. The difference is of approximately 1 mag in the bluer bands and it can reach almost 3 mag in the redder bands.

The modelled colours, displayed on the *gri* colour–colour diagram in Fig. 3, show that the two blue components are indeed consistent with the quasar locus. The difference between the colours of the quasar-like components can be explained by contamination from the galaxy-like component on the bright counterpart that is projected closer to it. That is supported by the fact that the biggest colour difference is seen in  $r - i$ , where the galaxy is brighter, and not in  $g - r$ . It is also clear, by comparing the modelled photometry of B to that available in the DES catalogue, that despite being segmented, it still contains part of the lensing galaxy flux, particularly in the red bands.

The modelled photometry enables us to calculate photometric redshifts (photo-*z*) for each component. This was done using the SED fitting code LePHARE (Arnouts et al. 1999; Ilbert et al. 2006). The method compares, through  $\chi^2$  minimization, the observed magnitudes of a given object with those predicted by the SED which has been convolved with the filter transmission curves. Reddening, interstellar extinction and the opacity of the intergalactic medium are taken into account.

We used two sets of SED libraries made available with the code: one for galaxy fitting and one for quasars. The first is composed of four observed spectra from Coleman, Wu & Weedman (1980) (linearly extrapolated into ultraviolet and near-IR wavelengths) representing elliptical, irregular, Sbc and Scd galaxies, plus six observed starburst SEDs from the Kinney atlas described in Calzetti, Kinney & Storchi-Bergmann (1994). The second library is composed of seven synthetic quasar spectra with varying equivalent widths for the Lyman  $\alpha$  and N  $\nu$  lines and both with and without contribution from a blackbody ( $T = 24\,000$  K) component. A power-law com-

ponent with spectral indexes of  $\alpha = -1.0$  for  $597 < \lambda < 10\,000$  Å and  $\alpha = -0.7$  for  $10\,000 < \lambda < 25\,000$  Å was used on all quasar spectra.

For the photometric errors, we estimated 0.1 in each band as an approximation. The best-fitting photo-*z* results for each component are listed in Table 3. The lensing galaxy was best fitted with an elliptical template. Synthetic spectra with different equivalent widths for spectral lines were used to best fit each quasar image, which is not surprising, given that object A is likely to be more heavily contaminated by the lensing galaxy light. The best-fitting templates are over-plotted in Fig. 4 for each component.

### 3 SPECTROSCOPIC OBSERVATIONS

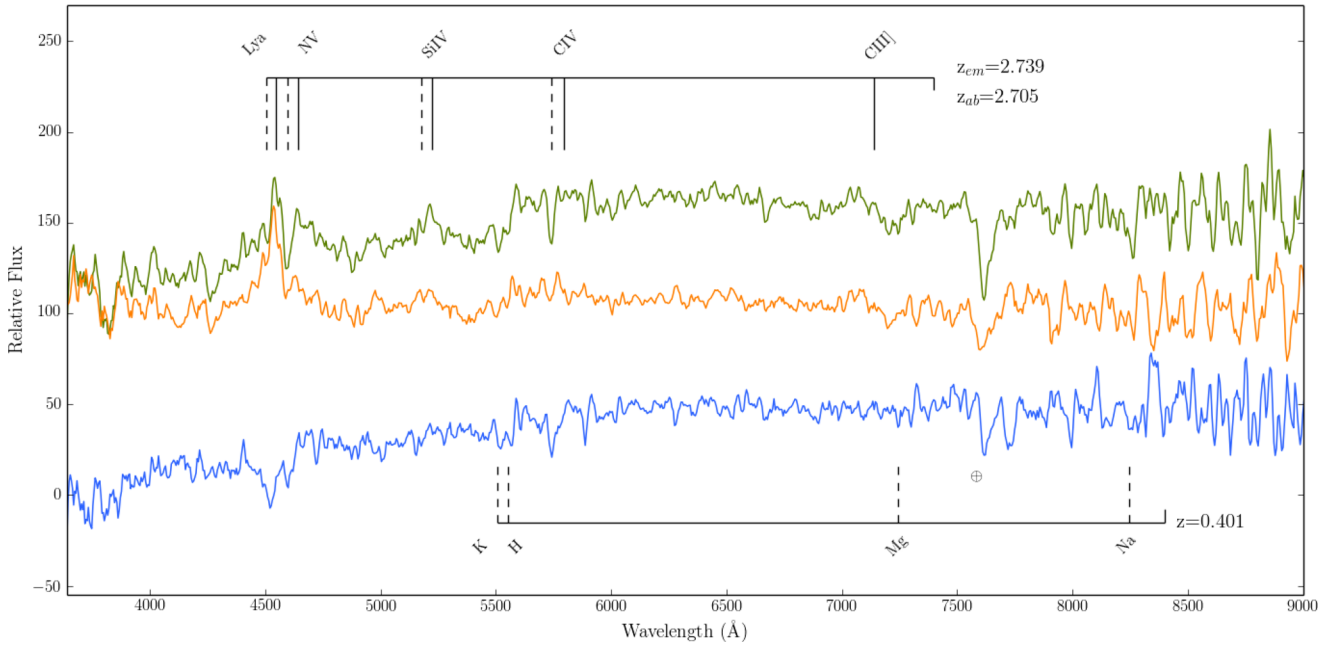
#### 3.1 NTT

Observations were carried out with the ESO Faint Object Spectrograph and Camera 2 (EFOSC2; Buzzoni et al. 1984) mounted at the f/11 nasmyth focus on the 3.6-m NTT on the night of 2015 October 7/8th UT as part of ESO observing programme 096-A-041. The 236 lines/mm Grism 13 blazed at 4400 Å was used giving a  $5.54$  Å pixel $^{-1}$  (binned  $2 \times 2$ ) and a spectral resolution of  $23.0$  Å for 1 arcsec seeing (FWHM). The full spectral coverage was  $3700$ – $9315$  Å with a delivered spectral resolution (FWHM) of  $34.5$  Å (6 pixels) and 1.5 arcsec seeing during the observations. The spectroscopic slit was aligned with PA =  $214^\circ$  so that both candidate quasar components were centred in the slit. No order blocking filter (e.g. GG475) was used since the largest wavelength range was required for redshift determination and hence there will be some second-order contamination at wavelengths longer than  $2 \times 3700$  Å =  $7400$  Å.

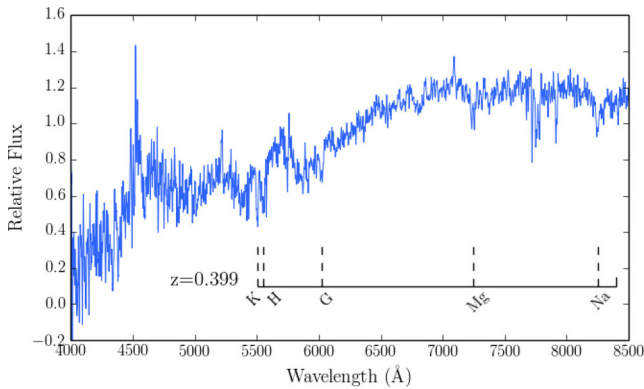
The 2D data were reduced following the guidelines of the PESSTO project (Smartt et al. 2015) using a set of custom PYTHON routines with bias frames and flat-fields taken during the afternoon prior to the observations. 1D spectra were extracted centred on the two quasar locations with wavelength calibration applied using Arc lamp observations that were taken immediately after the spectroscopic observations of the science target. The separation of the two quasars is 2.9 arcsec with the galaxy lying between the two quasars and separated 1.2 arcsec from the brighter quasar component A and 1.7 arcsec from component B. Therefore, the galaxy contributes to the spectra of both quasars and is unresolved with respect to quasar component A in the seeing of 1.5 arcsec. The resultant 1D extracted spectra are shown in Fig. 5.

#### 3.2 AAT archival data

A search for J2325–5229 in other data archives showed it was part of the XXL survey that used the *XMM–Newton* X-ray telescope to image  $50$  deg $^2$  in two fields between 2011 and 2013



**Figure 5.** 1D NTT spectra. The top (green) spectrum is the brighter component A and the lower (yellow) spectrum is component B. On top, we have marked the location of the source quasar emission lines at  $z_{\text{em}} = 2.739$  (solid lines) and absorption lines at  $z_{\text{ab}} = 2.705$  (dashed lines). On the bottom are the lensing galaxy absorption lines at  $z_{\text{ab}} = 0.401$ . In blue, we show A–B after scaling the flux of image B by the median flux ratio between the two quasars bluewards of 4000 Å.



**Figure 6.** 1D AAT spectrum from archival data. The dashed lines show the location of typical galaxy absorption lines at the given AAT  $z = 0.399$  redshift.

(Pierre et al. 2016). The total X-ray flux for the source is  $3.70 \pm 1.10 \times 10^{-14} \text{ erg cm}^{-2} \text{ s}^{-1}$ . The Anglo-Australian Telescope (AAT) was one of the facilities to provide spectroscopic follow-up for the southern XXL field. The follow-up is detailed in Lidman et al. (2016), where they describe the use of the two-degree field (2dF) fibre positioner in conjunction with the AAOmega spectrograph with a spectral coverage of 3700–8900 Å and spectral resolution of about 1500 or 4 Å at 6000 Å. The data processing is also described.

Data for J2325–5229 were obtained between 2013 September 08 and 09 and the 1D spectrum can be seen in Fig. 6. The data were processed with 2dfdr<sup>4</sup> through the Australian Dark Energy Survey (OzDES) pipeline (Yuan et al. 2015). Because the fibre diameter on the sky is  $\sim 2$  arcsec and the separation between the quasar images is  $\sim 2.9$  arcsec, most of the flux arises from the lensing galaxy, and the

galaxy spectral features are much more prominent in this spectrum than in the NTT spectra. For this reason, the object was not flagged as an AGN in the AAT catalogue. There is, however, clear evidence for quasar features, Lyman  $\alpha$  in particular at  $\lambda \sim 4600$  Å.

### 3.3 Redshift determination

We measured the wavelength of prominent emission and absorption features in the NTT spectra using the IRAF (v2.16; Tody 1993) SPLIT software. The peak or minimum and centroids were measured for each feature. The two measurements generally agreed to within 5 Å which is consistent with the spectral resolution (FWHM) of 35 Å i.e. 0.2 pixels. Throughout, unless specified, we use rest-frame laboratory wavelengths from Morton (1991) and Tytler & Fan (1992).

Both spectra show evidence of a strong emission feature at  $\sim 4540$  Å which we initially identified as redshifted hydrogen Lyman  $\alpha$  ( $\lambda_{\text{rest}} = 1215.7$  Å) at an emission line redshift of  $z = 2.73$ . At this redshift, one expects to see broad N V (1240.1 Å) C IV (1549.1 Å) and C III] (1908.7 Å) within the observed spectral window at 4631 Å, 5778 Å and 7119 Å respectively. Both spectra have potential lines at these wavelengths. In addition, there is evidence of absorption lines blueward of the N V and C IV permitted lines. No absorption is expected for C III] since this is a semi-forbidden transition. The observed wavelengths of these features are tabulated in Table 4 for each spectrum. We also calculate average emission line and absorption line redshifts excluding the tentative C III] line. We determine emission line redshifts of  $2.739 \pm 0.003$  for component A and  $2.732$  for component B. The absorption line redshifts are  $2.705 \pm 0.001$  for component A and  $2.698 \pm 0.004$  for component B, corresponding to a blueshift with respect to the emission line redshifts of 0.034 or 2700 km s<sup>-1</sup> which is within the range of associated absorption seen in many quasars including mini-BALs. The study of the absorption line velocity and intensity profiles in two sightlines can

<sup>4</sup> <http://www.aao.gov.au/science/instruments/AAOmega/reduction>

**Table 4.** Quasar redshift measurements.

Line	$\lambda_{\text{rest}}(\text{\AA})^a$	A		B	
		$\lambda_{\text{obs}}(\text{\AA})$	$z$	$\lambda_{\text{obs}}(\text{\AA})$	$z$
$\text{Ly}\alpha_{\text{em}}$	1215.7	4542.8	2.737	4536.8	2.732
$\text{N V}_{\text{ab}}$	1240.1	4596.5	2.706	4583.3	2.696
$\text{N V}_{\text{em}}$	1240.1	4639.8	2.741	—	—
$\text{C IV}_{\text{ab}}$	1549.1	5737.8	2.704	5733.6	2.701
$\text{C III}_{\text{em}}$	1908.7	7057.2(?)	2.697	7066.8(?)	2.703
		$\bar{z}_{\text{em}} = 2.739 \pm 0.003^b$		$\bar{z}_{\text{em}} = 2.732^b$	
		$\bar{z}_{\text{ab}} = 2.705 \pm 0.001$		$\bar{z}_{\text{ab}} = 2.698 \pm 0.004$	

Notes. (?): identification uncertain.

<sup>a</sup>Rest frame laboratory wavelengths from Tytler & Fan (1992).

<sup>b</sup>C III] was not used to calculate average redshifts.

**Table 5.** Lensing galaxy redshift measurements.

Line	$\lambda_{\text{rest}}(\text{\AA})$	NTT		AAT	
		$\lambda_{\text{obs}}(\text{\AA})$	$z$	$\lambda_{\text{obs}}(\text{\AA})$	$z$
Ca K	3933.7	5510.8	0.401	5506.0	0.400
Ca H	3968.5	—	—	5552.5	0.399
G band	4304.0	—	—	6018.7	0.398
Mg I	5175.0	7244.5	0.400	7268.5	0.404(?)
Na D	5892.9	8260.4	0.402	8229.5	0.397
		$\bar{z} = 0.401 \pm 0.001$		$\bar{z} = 0.400 \pm 0.003$	

Notes. (?): identification uncertain.

Combined average redshift:  $0.400 \pm 0.002$ .

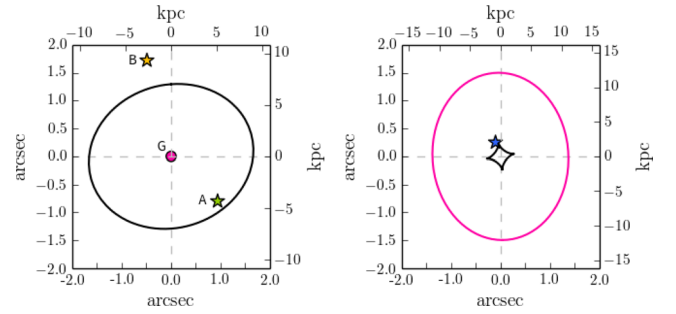
be used to probe the out-flowing winds of quasars (e.g. Misawa et al. 2013).

Based on the photometric redshift of 0.302 from Section 2.3, we expect the Calcium K and H to have observed wavelengths of 5121.68 Å and 5166.99 Å, respectively. In order to make the galaxy absorption lines more evident in the NTT spectra, we tried to remove the quasar contribution by subtracting the two spectra. But first, we scaled the flux of the fainter image by using the median flux ratio between the two quasars blueward of 4000 Å where the galaxy contamination would be negligible. The subtracted spectrum is shown in Fig. 5. There is evidence of a doublet at  $\sim 5530$  Å in both spectra and we identify this as calcium H and K. We also identify absorption lines consistent with Mg I and NaD. The average redshift derived from these lines is  $0.401 \pm 0.001$ . We make similar measurements from the AAT spectrum and derive a redshift of  $0.400 \pm 0.003$  as can be seen in Table 5.

Subsequent to our measurements of the AAT spectrum, Lidman et al. (2016) published their independent analysis of these data and report a redshift of  $0.3996 \pm 0.0003$ . We take the redshift to be the average of our NTT and AAT analysis at  $0.400 \pm 0.002$  which is consistent within 0.0004 with the Lidman et al. (2016) determination.

## 4 LENS MODELLING

Due to the low number of constraints in a double image system, we can only investigate simple lens models, in particular the singular isothermal ellipsoid (SIE). We model the lens system using the public lensing software, GLAFIC (Oguri 2010a,b). There are eight constraints from observations (positions of the two quasar images and their fluxes, and the position of the lensing galaxy) and eight model parameters (position and flux of the source quasar, position of



**Figure 7.** Caustics and critical lines obtained after the mass distribution modelling of J2325. On the left is the image plane, where the black curve indicates the tangential critical line and the pink circle marks out the radial critical curve. Images A and B are the green and yellow stars, respectively. On the right is the source plane, with the radial caustic in pink and the tangential caustic in black. The source quasar is denoted by the blue star.

**Table 6.** Parameters of J2325–5229.

	Lens model	2D model
$R_E$	$1.47'' \pm 0.03$	
$q$	$0.23 \pm 0.06$	$0.19 \pm 0.03$
PA	$97^\circ \pm 4^\circ$	$70^\circ \pm 5^\circ$
$\Delta t^a$	$52 \pm 11$ d	
$M_{\text{enclosed}}$	$(4.04 \pm 0.15) \times 10^{11} M_\odot$	
$\mu$	$10 \pm 3$	

Note. <sup>a</sup> Time delays are positive if A follows B.

the lensing galaxy, its mass, ellipticity and position angle). Hence, the model has zero degrees of freedom and we expect solutions to converge to  $\chi^2 \sim 0$ . To estimate uncertainties on the model parameters, we generated 2000 data sets from the constraints and their errors (as in Table 3), including a deviation in the mass density power law of an SIE of 0.1, which covers the observed density distribution in early-type galaxies (Auger et al. 2010). We use the *i*-band magnitudes as image fluxes and increase the uncertainty on the fluxes by 0.1 mag because of possible contaminations, such as microlensing, dust extinction and intrinsic quasar variability over the time delay (e.g. Hook et al. 1994; MacLeod et al. 2012).

In Fig. 7 we show the diagrams of critical lines and caustics in both the image and the source planes, obtained using GRAVLENS (Keeton 2001). The results are in agreement with the GLAFIC model. The source quasar is close to the inner caustic but not inside it, which is the reason why the quasar is only doubly lensed. Summarized in Table 6 are the modelling results for Einstein radius ( $R_E$ ), ellipticity ( $q$ ), position angle, time delay ( $\Delta t$ ), enclosed mass ( $M_{\text{enclosed}}$ ) and magnification ( $\mu$ ). Images A and B are magnified by  $-6.5 \pm 2.2$  and  $3.8 \pm 1.0$ , respectively, where the negative sign denotes a parity flip. The time delay was found to be  $\Delta t = 52 \pm 11$  d (A follows B), given a Hubble constant  $H_0 = 68 \text{ km s}^{-1} \text{ Mpc}^{-1}$ . The discrepancy between position angles measured through the light profile (2D modelling) and mass modelling seen in Table 6 is possibly due to the unknown external shear (Keeton, Kochanek & Falco 1998).

## 5 DISCUSSION AND CONCLUSIONS

We have identified a high-redshift lensed quasar, VDES J2325–5229, by applying GMM supervised machine learning to select the candidates in a colour space defined by DES+VHS+WISE photometric bands. Since the selection does not depend on the

*u* band, we are capable of selecting candidates at higher redshifts. For comparison, amongst the 49 new lenses found by SQLS, only six have source redshifts greater than J2325, three of which were serendipitously discovered (Johnston et al. 2003; Pindor et al. 2004; McGreer et al. 2010). Two more lenses with source redshifts greater than J2325 were discovered in SDSS-III BOSS quasar lens survey (More et al. 2016), including the highest redshift multiply lensed quasar known, with  $z_s = 4.819$ .

Given the geometry of the system, with the presence of an obvious LRG galaxy, and an angular separation between the quasars that converts to a physical distance of  $\sim 23.2$  kpc, it is unlikely that we are looking at distinct binary quasars. The quasar SEDs are considerably similar, with emission line redshifts that differ by  $562 \pm 240$  km s<sup>-1</sup> in the quasar rest frame. Given the poor seeing during the NTT spectroscopic observations and the contamination from the lensing galaxy particularly in the SED of quasar component A, that discrepancy is not surprising. Both quasar images present an intrinsic absorption line system detected in C IV and N V, blueshifted by  $2739 \pm 254$  km s<sup>-1</sup> in component A and  $2744 \pm 324$  km s<sup>-1</sup> in component B with respect to the emission line redshift, further evidencing the SED similarity.

There is evidence that the C IV absorption line is weaker in image B, which would be consistent with different sightlines in the broad-line region of the source quasar as predicted by Misawa et al. (2014). This can be seen in Fig. 5, where we have scaled the flux of image B by the median flux ratio between the two quasars blueward of 4000 Å, where the contamination of the lensing galaxy is most negligible, and subtracted B from A. A strong absorption feature remains at  $\lambda \sim 5734$  Å, where the C IV absorption is expected to be for  $z_{ab} = 2.7$ . A lesser effect is seen at  $\lambda \sim 4596$  Å, where one expects the N V absorption to be. This is unsurprising giving the ionization potentials of 64.5 and 97.9 eV for C IV and N V, respectively, which means that N V absorbers would be closer to the flux source, and therefore be less likely to be affected by differences in sightlines. Further high-resolution spectroscopy of J2325 would allow for the different sightlines scenario to be confirmed and to constrain the size of the absorber and geometry of the broad-emission line region.

The modelled *i*-band magnitude of the lensing galaxy can be used to estimate the rest-frame *R*-band magnitude. At these redshifts, and given our choice of rest and observed frame filters, the *K*-corrections can be neglected. For the LRG in J2325–5229, we calculate  $M_R = -22.41$ , given  $z = 0.4$  and  $m_i = 18.50$ . We can compare this magnitude to that obtained by using the separation of the quasar images and the lensing Faber–Jackson relation with fit parameters described in Rusin et al. (2003) following what was done in Jackson, Ofek & Oguri (2008). Assuming  $z = 0.400 \pm 0.002$  and  $\theta = 2.90$ ,

$$M_R = M_{*R} + 2.5\gamma_{E+K}z - 1.25\gamma_{FJ} \log \theta \quad (2)$$

yields  $M_R = -23.11 \pm 0.53$ , which is close to the expected value obtained from modelling the data.

The next DES data release will contain data from the full 5000 deg<sup>2</sup> survey area and will provide a rich sample in which to look for lensed quasars. With such a large area, one can expect to find dozens of bright lenses, including those with quadruple images and the technique introduced in this paper should be able to select all of them as candidates.

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<sup>5</sup> <https://github.com/drphilmarshall/OM10>



## REFERENCES

- Abazajian K. N. et al., 2009, *ApJS*, 182, 543
- Agnello A. et al., 2015, *MNRAS*, 454, 1260
- Arnouts S., Cristiani S., Moscardini L., Matarrese S., Lucchin F., Fontana A., Giallongo E., 1999, *MNRAS*, 310, 540
- Assef R. J. et al., 2013, *ApJ*, 772, 26
- Astropy Collaboration et al., 2013, *A&A*, 558, A33
- Auger M. W., Treu T., Bolton A. S., Gavazzi R., Koopmans L. V. E., Marshall P. J., Moustakas L. A., Burles S., 2010, *ApJ*, 724, 511
- Auger M. W., Treu T., Brewer B. J., Marshall P. J., 2011, *MNRAS*, 411, L6
- Bechtol K. et al., 2015, *ApJ*, 807, 50
- Bertin E., Arnouts S., 1996, *A&AS*, 117, 393
- Bonvin V. et al., 2016, *MNRAS*, preprint ([arXiv:1607.01790](https://arxiv.org/abs/1607.01790))
- Browne I. W. A. et al., 2003, *MNRAS*, 341, 13
- Buzzoni B. et al., 1984, *The Messenger*, 38, 9
- Calzetti D., Kinney A. L., Storchi-Bergmann T., 1994, *ApJ*, 429, 582
- Claeskens J.-F., Sluse D., Riaud P., Surdej J., 2006, *A&A*, 451, 865
- Coleman G. D., Wu C.-C., Weedman D. W., 1980, *ApJS*, 43, 393
- Croom S. M., Smith R. J., Boyle B. J., Shanks T., Loaring N. S., Miller L., Lewis I. J., 2001, *MNRAS*, 322, L29
- DES Collaboration 2005, preprint ([arXiv:e-prints](https://arxiv.org/abs/e-prints))
- DES Collaboration et al., 2016, *MNRAS*, 460, 1270
- Diehl H. T. et al., 2014, *Proc. SPIE Vol. 9149, Observatory Operations: Strategies, Processes, and Systems V.* p. 91490V
- DiPompeo M. A., Bovy J., Myers A. D., Lang D., 2015, *MNRAS*, 452, 3124
- Flaugher B. et al., 2015, *AJ*, 150, 150
- Hook I. M., McMahon R. G., Boyle B. J., Irwin M. J., 1994, *MNRAS*, 268, 305
- Ilbert O. et al., 2006, *A&A*, 457, 841
- Inada N. et al., 2008, *AJ*, 135, 496
- Inada N. et al., 2010, *AJ*, 140, 403
- Inada N. et al., 2012, *AJ*, 143, 119
- Ivezic Z. et al., 2008, *Serbian Astron. J.*, 176, 1
- Jackson N., Ofek E. O., Oguri M., 2008, *MNRAS*, 387, 741
- Jarrett T. H. et al., 2011, *ApJ*, 735, 112
- Johnston D. E. et al., 2003, *AJ*, 126, 2281
- Keeton C. R., 2001, *ApJ*, preprint ([astro-ph/0102340](https://arxiv.org/abs/astro-ph/0102340))
- Keeton C. R., Kochanek C. S., Falco E. E., 1998, *ApJ*, 509, 561
- King L. J., Browne I. W. A., Marlow D. R., Patnaik A. R., Wilkinson P. N., 1999, *MNRAS*, 307, 225
- Kochanek C. S., Dalal N., 2004, *ApJ*, 610, 69
- Kochanek C. S., Keeton C. R., McLeod B. A., 2001, *ApJ*, 547, 50
- Kochanek C. S., Mochejska B., Morgan N. D., Stanek K. Z., 2006, *ApJ*, 637, L73
- Kron R. G., 1980, *ApJS*, 43, 305
- Lidman C. et al., 2016, *PASA*, 33, e001
- MacLeod C. L. et al., 2012, *ApJ*, 753, 106
- McGreer I. D. et al., 2010, *AJ*, 140, 370
- VHS Collaboration McMahon R. G., Banerji M., Gonzalez E., Koposov S. E., Bejar V. J., Lodieu N., Rebolo E., 2013, *The Messenger*, 154, 35
- Mao S., Schneider P., 1998, *MNRAS*, 295, 587
- Misawa T., Inada N., Ohsuga K., Gandhi P., Takahashi R., Oguri M., 2013, *AJ*, 145, 48
- Misawa T., Inada N., Oguri M., Gandhi P., Horiuchi T., Koyamada S., Okamoto R., 2014, *ApJ*, 794, L20
- Mohr J. J. et al., 2012, *Proc. SPIE Vol. 8451, Software and Cyberinfrastructure for Astronomy II.* p. 84510D
- More A. et al., 2016, *MNRAS*, 456, 1595
- Morgan C. W., Kochanek C. S., Morgan N. D., Falco E. E., 2010, *ApJ*, 712, 1129
- Morton D. C., 1991, *ApJS*, 77, 119
- Myers S. T. et al., 2003, *MNRAS*, 341, 1
- Nierenberg A. M., Treu T., Wright S. A., Fassnacht C. D., Auger M. W., 2014, *MNRAS*, 442, 2434
- Oguri M., 2010a, *glafic: Software Package for Analysing Gravitational Lensing*, Astrophysics Source Code Library ([ascl:1010.012](https://arxiv.org/abs/ascl:1010.012))
- Oguri M., 2010b, *PASJ*, 62, 1017
- Oguri M., Marshall P. J., 2010, *MNRAS*, 405, 2579 (OM10)
- Oguri M. et al., 2006, *AJ*, 132, 999
- Oguri M. et al., 2008, *AJ*, 135, 512
- Pedregosa F. et al., 2011, *J. Machine Learning Res.*, 12, 2825
- Peng C. Y., Impey C. D., Rix H.-W., Kochanek C. S., Keeton C. R., Falco E. E., Lehár J., McLeod B. A., 2006, *ApJ*, 649, 616
- Pierre M. et al., 2016, *A&A*, 592, A1
- Pindor B. et al., 2004, *AJ*, 127, 1318
- Poindexter S., Morgan N., Kochanek C. S., 2008, *ApJ*, 673, 34
- Reynolds M. T., Walton D. J., Miller J. M., Reis R. C., 2014, *ApJ*, 792, L19
- Richards G. T. et al., 2002, *AJ*, 123, 2945
- Richards G. T. et al., 2015, *ApJS*, 219, 39
- Rusin D. et al., 2003, *ApJ*, 587, 143
- Smartt S. J. et al., 2015, *A&A*, 579, A40
- Stern D. et al., 2012, *ApJ*, 753, 30
- Stoughton C. et al., 2002, *AJ*, 123, 485
- Suyu S. H., Marshall P. J., Auger M. W., Hilbert S., Blandford R. D., Koopmans L. V. E., Fassnacht C. D., Treu T., 2010, *ApJ*, 711, 201
- Suyu S. H. et al., 2013, *ApJ*, 766, 70
- Tody D., 1993, in Hanisch R. J., Brissenden R. J. V., Barnes J., eds, *ASP Conf. Ser. Vol. 52. Astronomical Data Analysis Software and Systems II. Astron. Soc. Pac., San Francisco*, p. 173
- Tytler D., Fan X.-M., 1992, *ApJS*, 79, 1
- Vanderplas J., Connolly A., Ivezić Ž., Gray A., 2012, *Proc. Conference on Intelligent Data Understanding (CIDU)*. p. 47
- Vegetti S., Lagattuta D. J., McKean J. P., Auger M. W., Fassnacht C. D., Koopmans L. V. E., 2012, *Nature*, 481, 341
- Walsh D., Carswell R. F., Weymann R. J., 1979, *Nature*, 279, 381
- Wright E. L. et al., 2010, *AJ*, 140, 1868
- Yuan F. et al., 2015, *MNRAS*, 452, 3047

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